

# **NXT HW**

# **Sensors and Actuators**

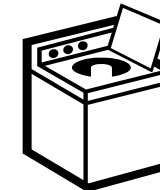
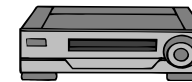
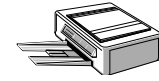
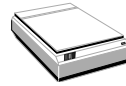
Brian Nielsen

[bnielsen@cs.aau.dk](mailto:bnielsen@cs.aau.dk)

# A “short list” of embedded systems

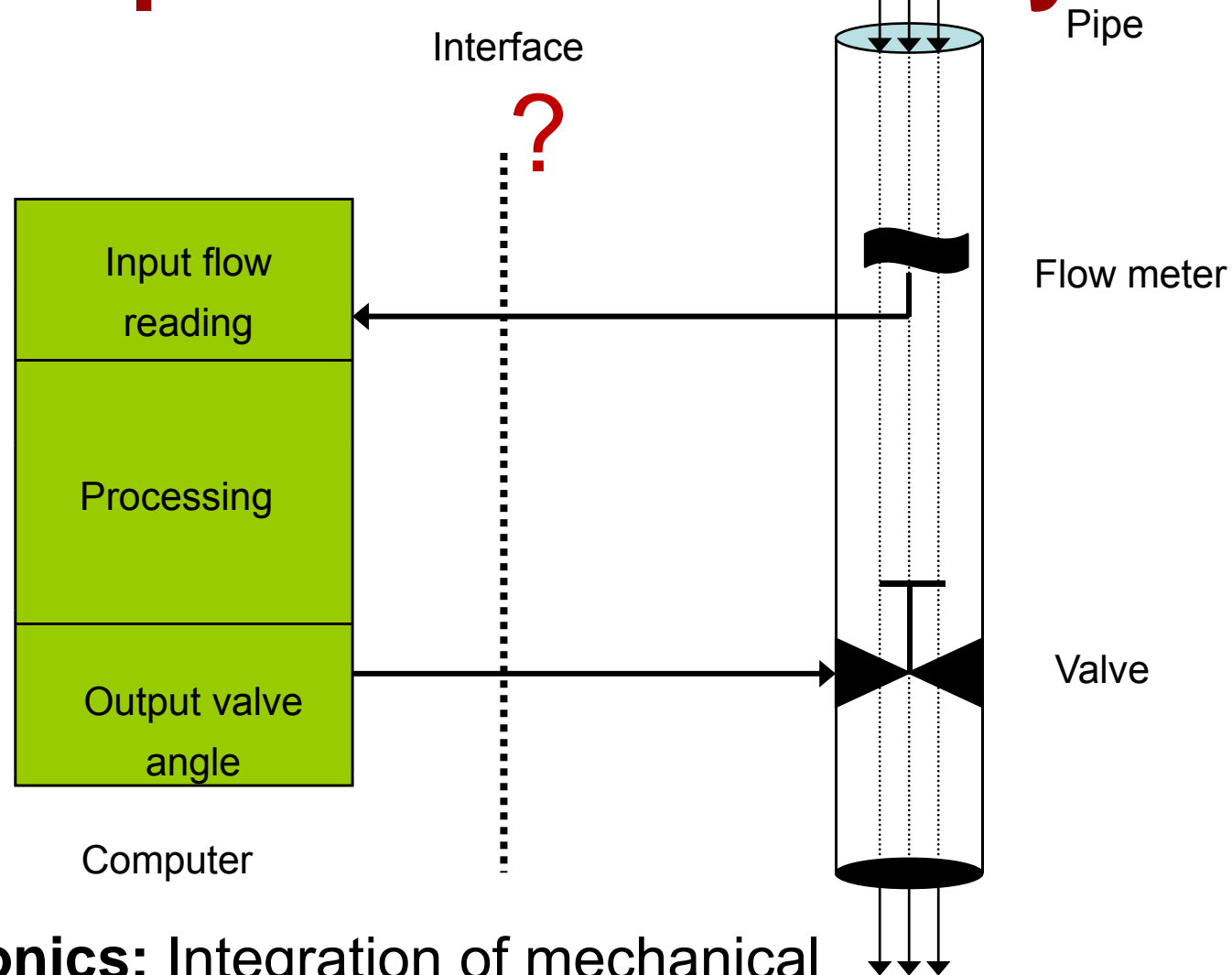
Anti-lock brakes  
Auto-focus cameras  
Automatic teller machines  
Automatic toll systems  
Automatic transmission  
Avionic systems  
Battery chargers  
Camcorders  
Cell phones  
Cell-phone base stations  
Cordless phones  
Cruise control  
Curbside check-in systems  
Digital cameras  
Disk drives  
Electronic card readers  
Electronic instruments  
Electronic toys/games  
Factory control  
Fax machines  
Fingerprint identifiers  
Home security systems  
Life-support systems  
Medical testing systems

Modems  
MPEG decoders  
Network cards  
Network switches/routers  
On-board navigation  
Pagers  
Photocopiers  
Point-of-sale systems  
Portable video games  
Printers  
Satellite phones  
Scanners  
Smart ovens/dishwashers  
Speech recognizers  
Stereo systems  
Teleconferencing systems  
Televisions  
Temperature controllers  
Theft tracking systems  
TV set-top boxes  
VCR's, DVD players  
Video game consoles  
Video phones  
Washers and dryers



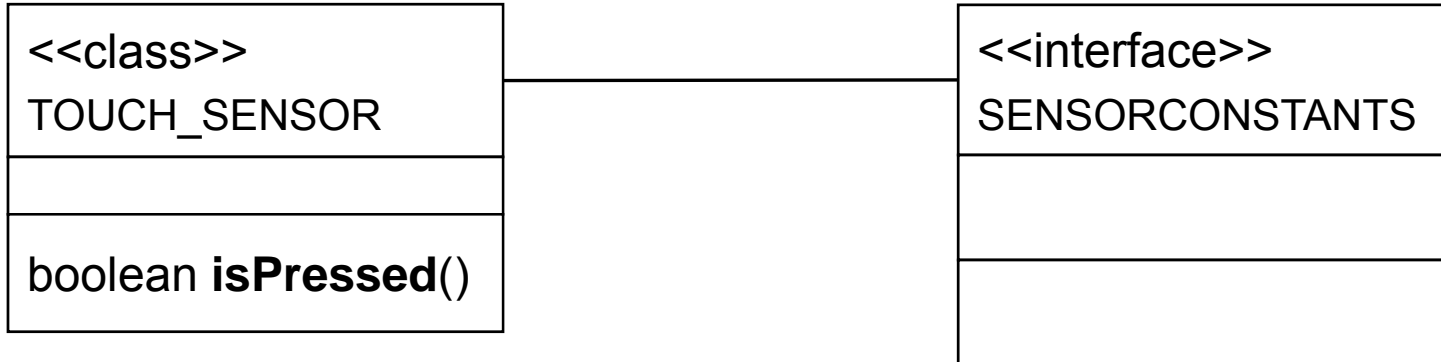
And the list goes on and on

# A simple fluid control system



**Mechatronics:** Integration of mechanical engineering with electronics and intelligent computer control in the design and manufacturing of industrial products and processes

# NXT Sensor API



## JAVADOC

### Constructor Detail

#### TouchSensor

```
public TouchSensor(ADSensorPort port)
```

Create a touch sensor object attached to the specified port.

#### Parameters:

port - port, e.g. Port.S1

### Method Detail

#### isPressed

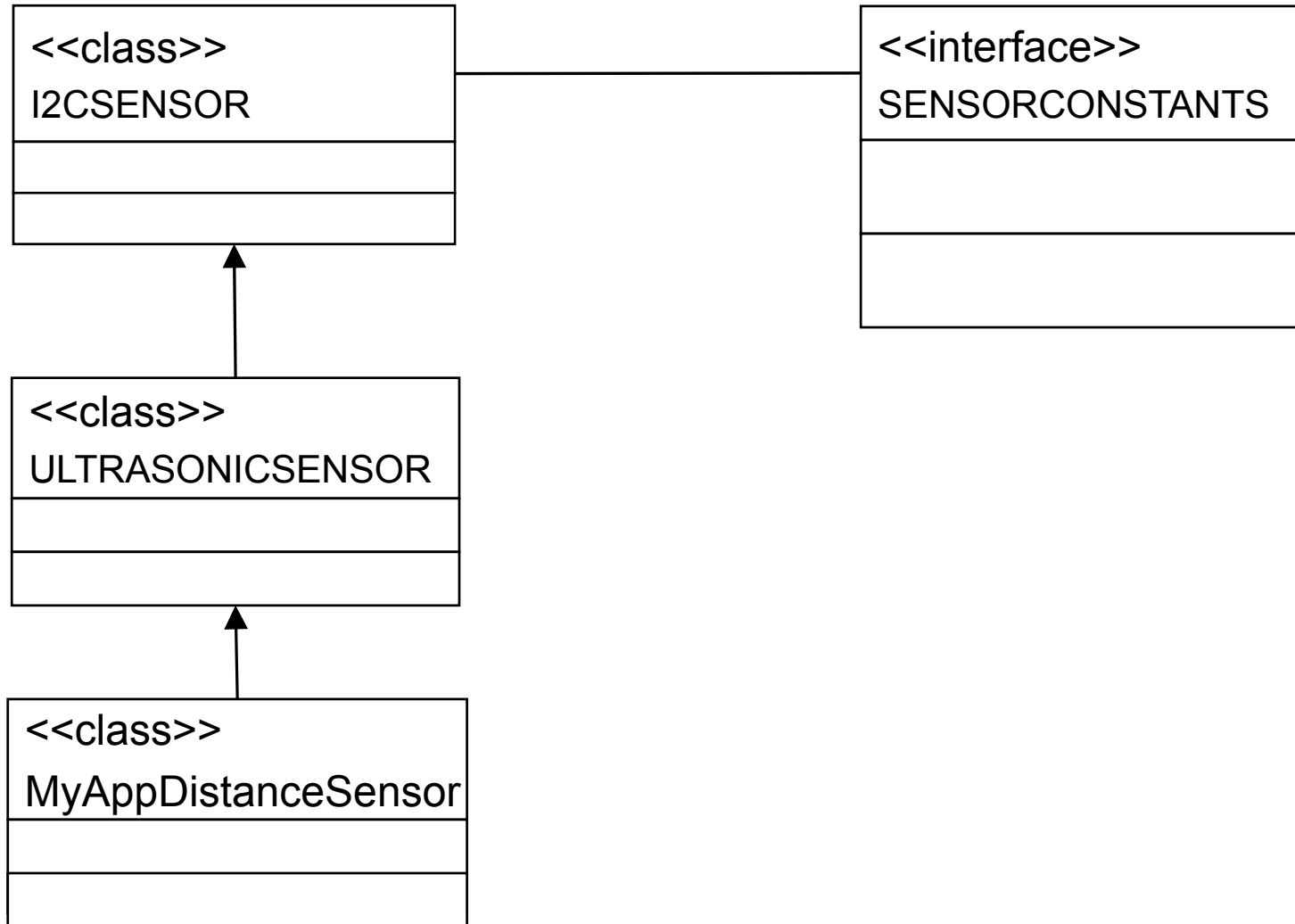
```
public boolean isPressed()
```

Check if the sensor is pressed.

#### Returns:

true if sensor is pressed, false otherwise.

# NXT Sensor API



# UltraSonic Methods

- int [capture\(\)](#) *Set capture mode Set the sensor into capture mode.*
- int [continuous\(\)](#) *Switch to continuous ping mode.*
- int [getCalibrationData](#)(byte[] data) *Return 3 bytes of calibration data.*
- byte [getContinuousInterval](#)() *Return the interval used in continuous mode.*
- int [getData](#)(int register, byte[] buf, int len) *Executes an I2C read transaction*
- int [getDistance](#)() *Return distance to an object.*
- int [getDistances](#)(int[] dist) *Return an array of 8 echo distances.*
- int [getFactoryData](#)(byte[] data) *Return 10 bytes of factory calibration data.*
- byte [getMode](#)() *Returns the current operating mode of the sensor.*
- [String getUnits](#)() *Return a string indicating the type of units in use by the unit.*
- int [off](#)() *Turn off the sensor.*
- int [ping](#)() *Send a single ping.*
- int [reset](#)() *Reset the device Performs a "soft reset" of the device.*
- int [sendData](#)(int register, byte[] buf, int len) *Executes an I2C write transaction.*
- int [setCalibrationData](#)(byte[] data) *Set 3 bytes of calibration data.*
- int [setContinuousInterval](#)(byte interval) *Set the ping interval in continuous mode.*

# Sensors & Actuators

- Acknowledgements

Hardware of the sensor network  
-- Sensors and peripheral hardware

-- Lin Gu

Sept 8, 2003

# Sensors and Actuators

- Transducer: “A device which transforms energy from one domain (magnetic, thermal, mechanical, optical, chemical, electrical) into another”
- **Sensors:** “devices which monitor a parameter of a system, hopefully without disturbing that parameter.”
- **Actuators:** “devices which impose a state on a system, hopefully independent of the load applied to them”



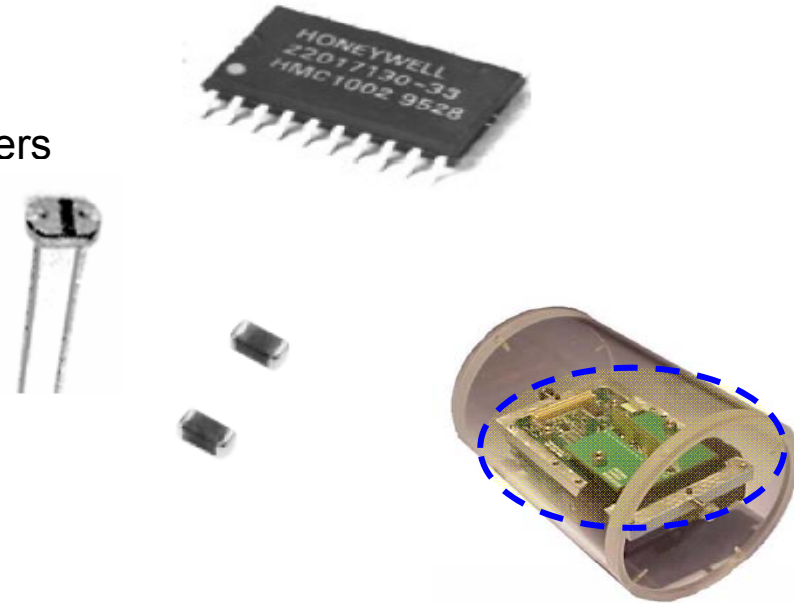
Sensor?

Actuator?



# Sensors Examples

- Example of sensors
  - Magnetic sensors
    - Honeywell's HMC/HMR magnetometers
  - Photo sensors
    - Clairex: CL9P4L
  - Temperature sensors
    - Panasonic ERT-J1VR103J
  - Accelerometers
    - Analog Devices: ADXL202JE
  - Motion sensors
    - Advantaca's MIR sensors
- "Without disturbing that parameter" implies that the sensors must be small and low-power devices in order to reduce energy exchange.



» Sensors: “devices which monitor a parameter of a system, hopefully without disturbing that parameter.”

# Sensors Types

- Motion / Rotation
- Acceleration
- Force, Torque, Pressure
- Flow
- Temperature
- Proximity
- Light
- Image
- ...

# Sensor Technology

- EG. Temperature Sensor



## Temperature sensors

Thermocouples

This is the cheapest and the most versatile sensor

Thermistors

Applicable over wide temperature ranges ( $-200^{\circ}\text{C}$  to  $1200^{\circ}\text{C}$  typical)

Thermodiodes, thermo transistors

Very high sensitivity in medium ranges (up to  $100^{\circ}\text{C}$  typical)

Compact but nonlinear in nature

RTD—resistance temperature detector

Ideally suited for chip temperature measurements

Minimized self heating

More stable over a long period of time compared to thermocouple

Linear over a wide range

---

REMARK: Properties!



# Sensors Properties

- **Range:** Min to Max value
  - Example
    - HMC1053: +/-6 Gauss
  - What decides range?
    - Saturated point
    - Noise
- **Accuracy / Error**
  - Diff. Actual and measured value
  - HMC1002: 0.05% (Hysteresis)
- **Repeatability**
  - HMC1002: 0.05%
- **Linearity**
  - HMC1002: 0.1% (Best fit straight line +/- 1 Gauss)



Magnetic Sensor Technology	Detectable Field Range (gauss)*				
	10 <sup>-8</sup>	10 <sup>-4</sup>	10 <sup>0</sup>	10 <sup>4</sup>	10 <sup>8</sup>
Squid	[Bar from 10 <sup>-8</sup> to 10 <sup>4</sup> ]				
Fiber-Optic	[Bar from 10 <sup>-6</sup> to 10 <sup>0</sup> ]				
Optically Pumped	[Bar from 10 <sup>-6</sup> to 10 <sup>0</sup> ]				
Nuclear Precession	[Bar from 10 <sup>-6</sup> to 10 <sup>0</sup> ]				
Search-Coil	[Bar from 10 <sup>-8</sup> to 10 <sup>8</sup> ]				
<i>Anisotropic Magnetoresistive</i>	[Red bar from 10 <sup>-6</sup> to 10 <sup>0</sup> ]				
Flux-Gate	[Bar from 10 <sup>-6</sup> to 10 <sup>0</sup> ]				
Magnetotransistor	[Bar from 10 <sup>-2</sup> to 10 <sup>2</sup> ]				
Magnetodiode	[Bar from 10 <sup>-2</sup> to 10 <sup>2</sup> ]				
Magneto-Optical Sensor	[Bar from 10 <sup>0</sup> to 10 <sup>8</sup> ]				
Giant Magnetoresistive	[Bar from 10 <sup>0</sup> to 10 <sup>8</sup> ]				
Hall-Effect Sensor	[Bar from 10 <sup>0</sup> to 10 <sup>4</sup> ]				

\* Note: 1gauss = 10<sup>-4</sup>Tesla = 10<sup>5</sup>gamma

Table 1-Magnetic sensor technology field ranges

# Sensors Properties

- **Sensitivity**
  - How output reflects input?
  - HMC1053: 1mV/V/gauss
- **Efficiency**
  - Ratio of the output power to the input power
  - Important for actuators
- **Resolution**
  - Determined by sensitivity and noise level
  - Measuring noise level
    - SNR
    - Noise floor (High noise floor does not mean “useless”)
  - HMC1002: 27uGauss

# Sensors Properties

## – Response time

- How fast the output reaches a fraction of the expected signal level

## – Overshoot

- How much does the output signal go beyond the expected signal level

## – Drift and stability

- How the output signal varies slowly compared to time

## – Offset

- The output when there is no input

# Sensor Properties

*Range*—Difference between the maximum and minimum value of the sensed parameter

*Resolution*—The smallest change the sensor can differentiate

*Accuracy*—Difference between the measured value and the true value

*Precision*—Ability to reproduce repeatedly with a given accuracy

*Sensitivity*—Ratio of change in output to a unit change of the input

*Zero offset*—A nonzero value output for no input

*Linearity*—Percentage of deviation from the best-fit linear calibration curve

*Zero Drift*—The departure of output from zero value over a period of time for no input

*Response time*—The time lag between the input and output

*Bandwidth*—Frequency at which the output magnitude drops by 3 dB

*Resonance*—The frequency at which the output magnitude peak occurs

*Operating temperature*—The range in which the sensor performs as specified

*Deadband*—The range of input for which there is no output

*Signal-to-noise ratio*—Ratio between the magnitudes of the signal and the noise at the output

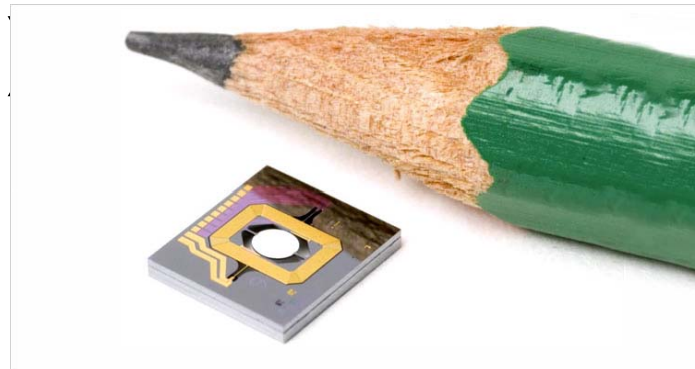
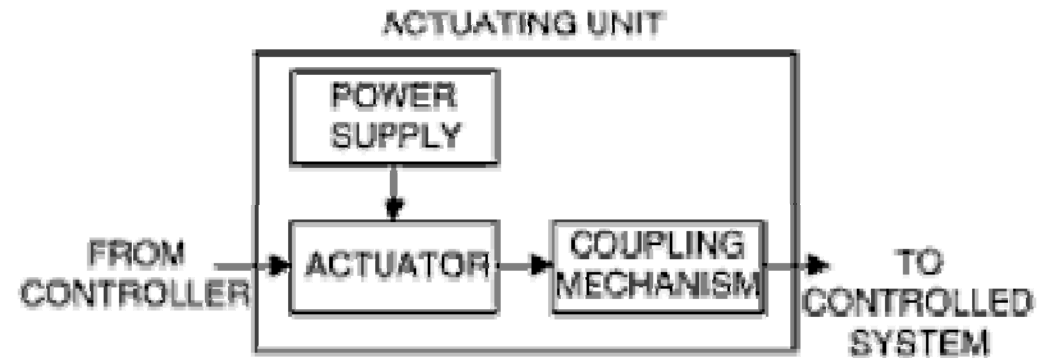
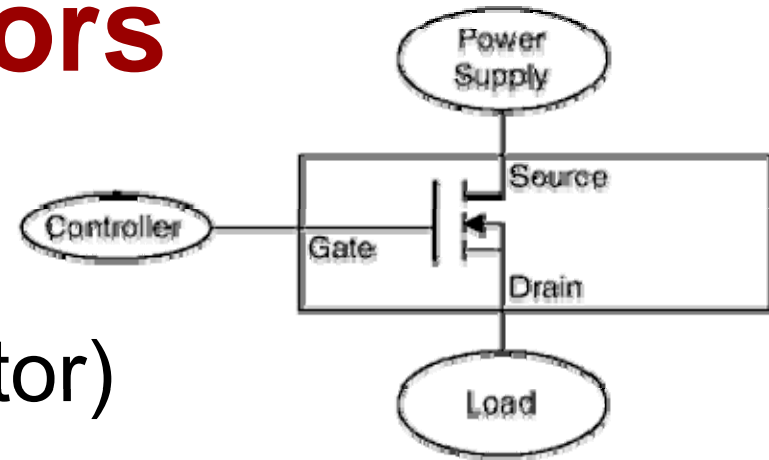
# Actuators

- Examples of Actuators
  - Motor (impose a torque)
  - Pumps (impose pressure or fluid velocity)
- Actuators may be powerful, large, and complicated
  - » Actuators: “devices which impose a state on a system, hopefully independent of the load applied to them”



# Actuators

- Electrical
- Electromechanical (motor)
- Electromagnetic
- Hydraulic
- Pneumatic
- Nano/Micro (MEMS)
- ...



# Actuator Properties

*Continuous power output*—The maximum force/torque attainable continuously without exceeding the temperature limits

*Range of motion*—The range of linear/rotary motion

*Resolution*—The minimum increment of force/torque attainable

*Accuracy*—Linearity of the relationship between the input and output

*Peak force/torque*—The force/torque at which the actuator stalls

*Heat dissipation*—Maximum wattage of heat dissipation in continuous operation

*Speed characteristics*—Force/torque versus speed relationship

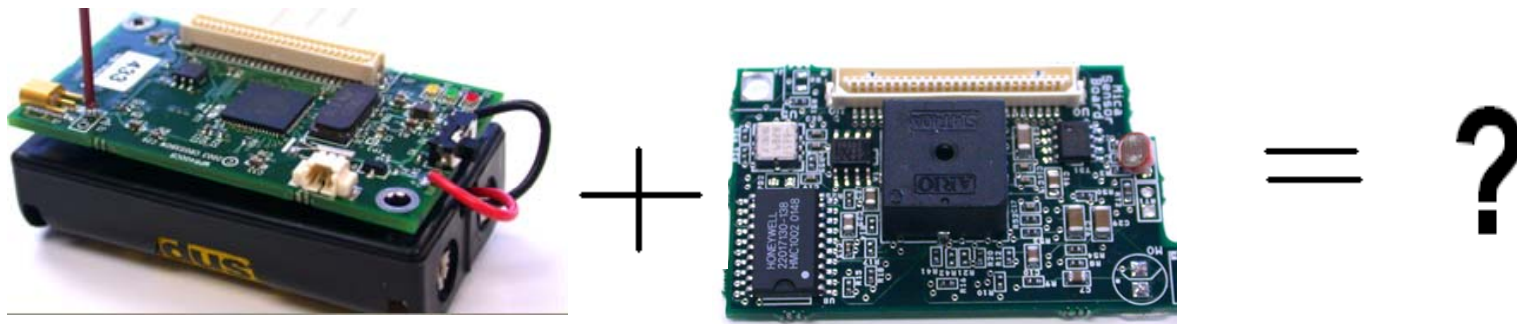
*No load speed*—Typical operating speed/velocity with no external load

*Frequency response*—The range of frequency over which the output follows the input faithfully, applicable to linear actuators

*Power requirement*—Type of power (AC or DC), number of phases, voltage level, and current capacity

# Application Requirements

- What's the implication to the application/middleware?
  - Select the suitable sensors for the target application
  - Imposing three general requirements to the application/middleware



# Application Requirements

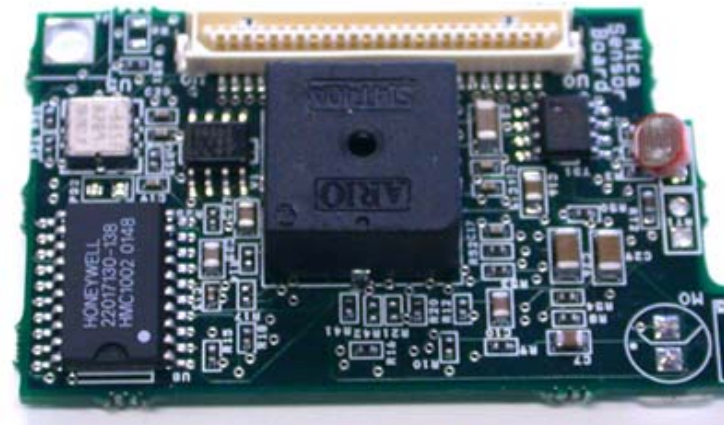
- **Requirement 1: sensor part**
  - Application designer must be aware of the properties of sensors
    - How to handle imperfect sensor devices
      - Error, offset, drift, ...
      - Repeatability
      - Sensors vary
- **Requirement 2: sensor reading**
  - Application designers must be aware of the errors introduced by the mote hardware?
    - The effect of AD converting
    - The effect of signal amplification/distortion

# Application Requirements

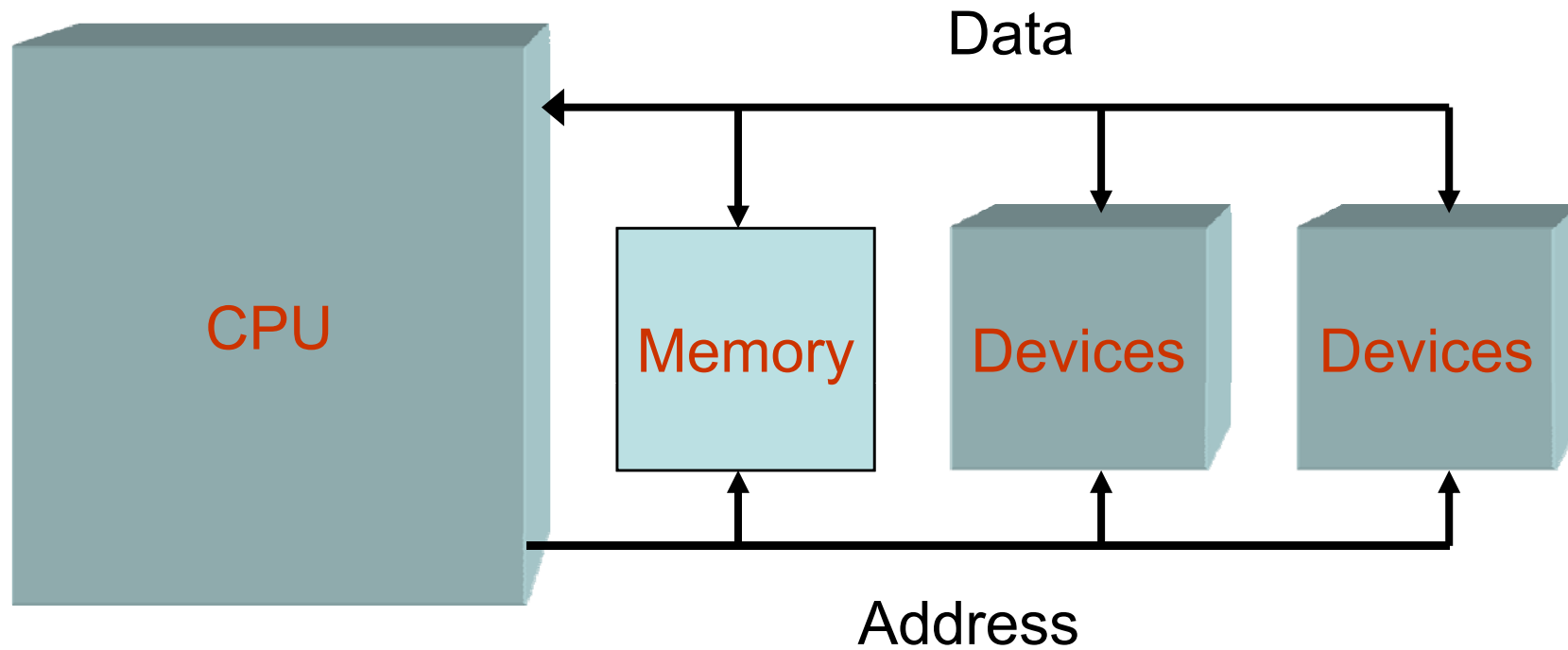
- **Requirement 3: interaction**
  - The application designer must be aware of the interaction of multiple sensors and the mote hardware
    - How to avoid race conditions on hardware wires and software event handlers?
    - How to control the mutual interaction of various hardware components?
      - Example: radio component increases the noise floor of the motion sensor
    - Can we make the sensors complement with each other to achieve better sensing?

# Supporting circuit

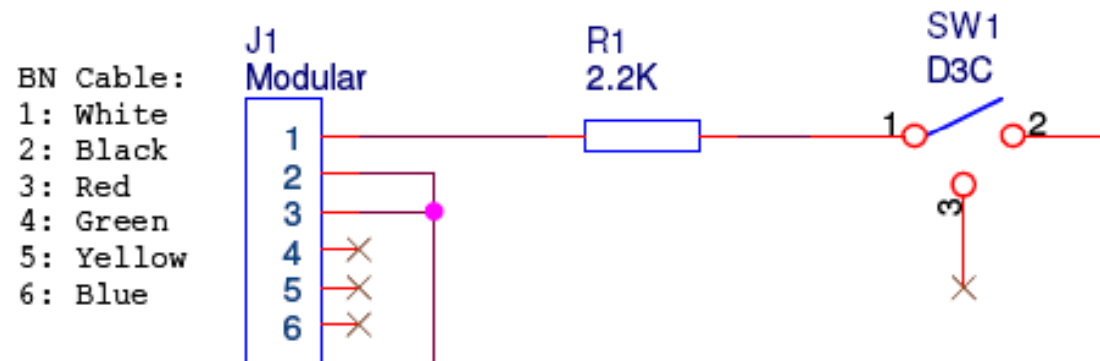
- Sensors may need supporting circuit to integrate with other sensors and the target application platform
  - Makes the electrical features of the computer and the I/O device compatible
  - Provides control and data transfer interface to the I/O device
    - PORT / Memory map
    - BUS
    - Interrupts
- Signal conditioning
  - Filtering
  - Amplification



# Eg. Memory Mapped Architecture

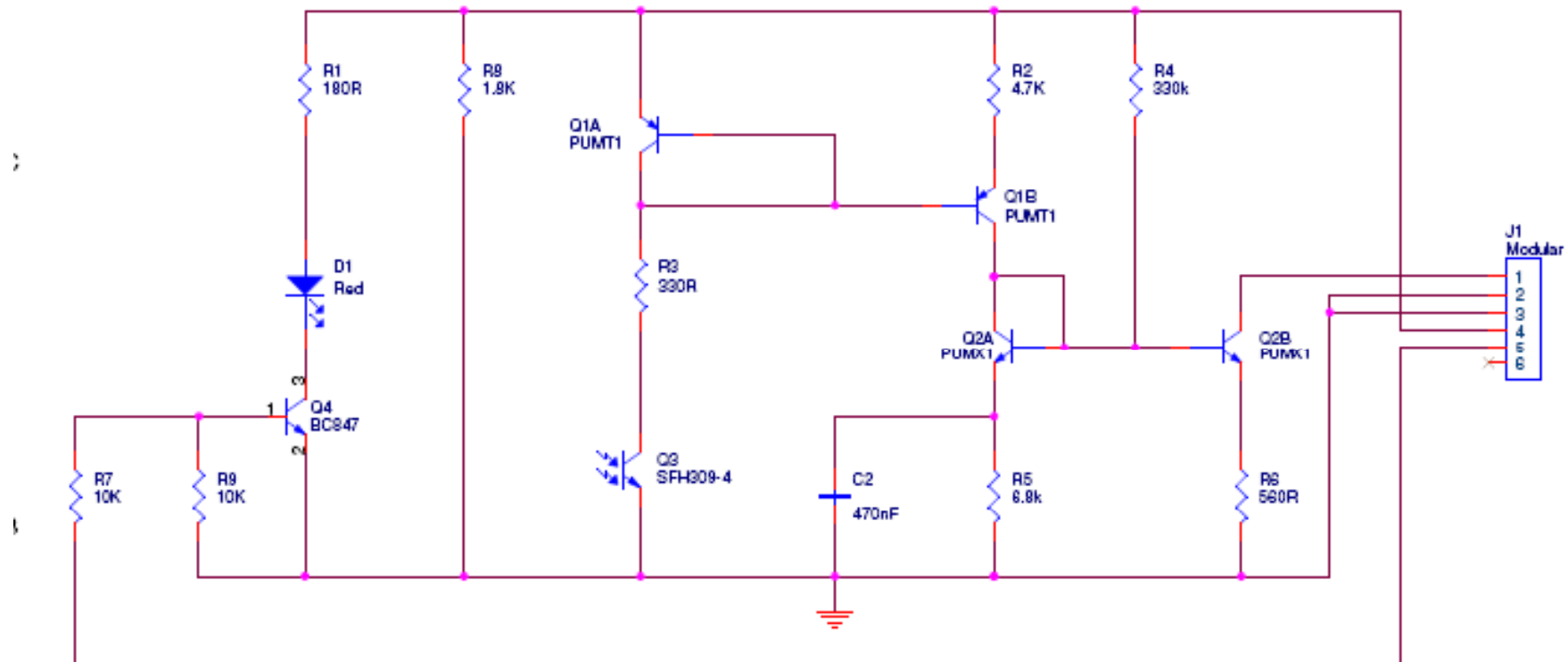


# NXT Touch Sensor





# NXT Light Sensor

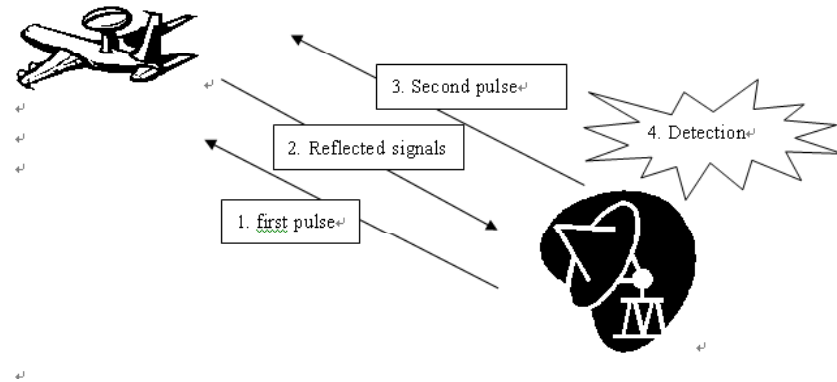


# Device Drivers

- Software that controls the operation of an I/O device
  - Uses port registers or memory map to control (read/write) the electronics of the device
  - Polling vs. Interrupt driven
  - Hardware, device and OS dependent
- [http://en.wikipedia.org/wiki/Device\\_driver](http://en.wikipedia.org/wiki/Device_driver)

# Sensors Data Processing Example

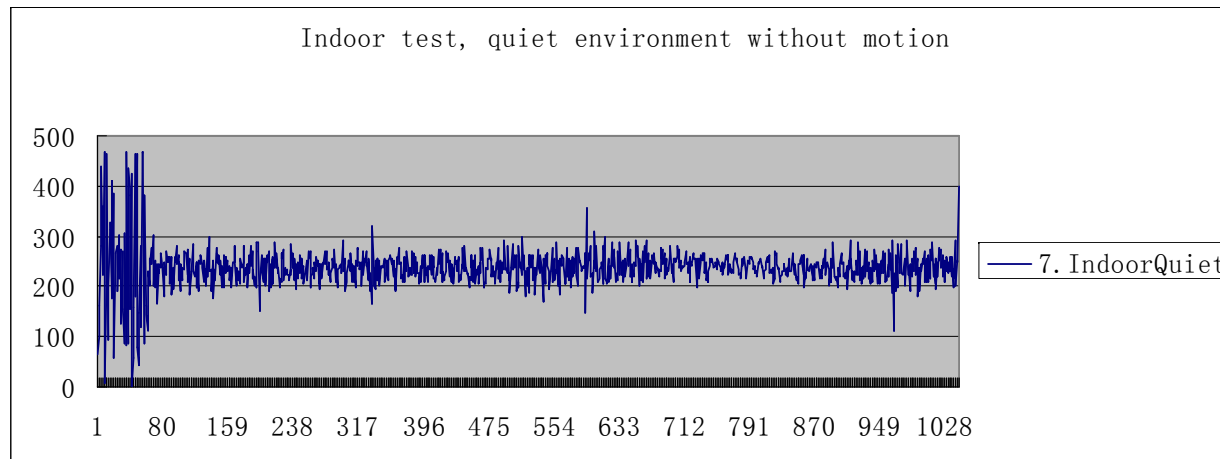
- Motion sensor using MIR
- Micro Impulse Radar
  - TWR-ISM-002
- Output (Advantaca's)
  - Analog
  - Digital
- Packaging
  - 51-pin connector
- Fine tuned receiving gate can potentially detect moving objects at a certain distance
- Is it a typical sensor?



# Post-processing

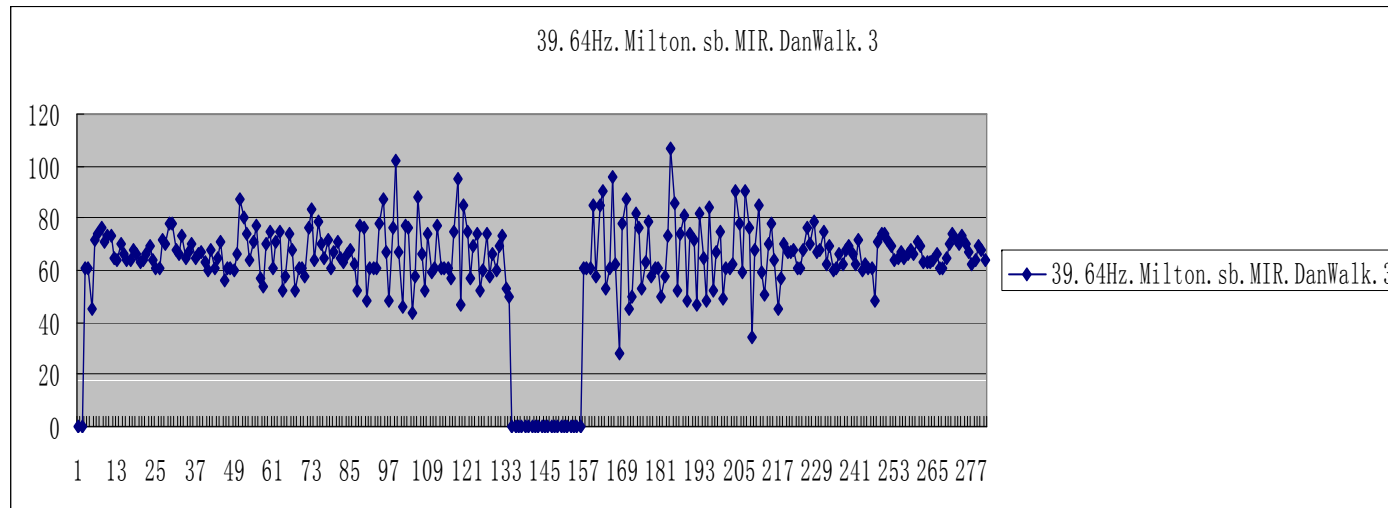
- Post-processing (“POST” ~after raw data has been collected)
  - Process the sensor reading to make it useful to the application
  - The complexity varies from simple threshold algorithm to full-fledged signal processing and pattern recognition
- (but pre – before application decides on actions)

# Post Processing MIR Data



- Raw reading of an MIR sensor in a quiet environment
  - The beginning period represents some unknown noise, possibly due to the positioning of the sensor

# Post Processing MIR Data



- Raw reading of an MIR sensor as a person walked by
  - The all-zero period is due to unreliable UART interface used to collect the reading and can be ignored.

# Post Processing MIR Data

- Use a post-processing algorithm to transform the raw reading to what the application needs
  - The application needs to know whether the motion of interest is detected
  - The post processing needs to filter out noise whenever possible

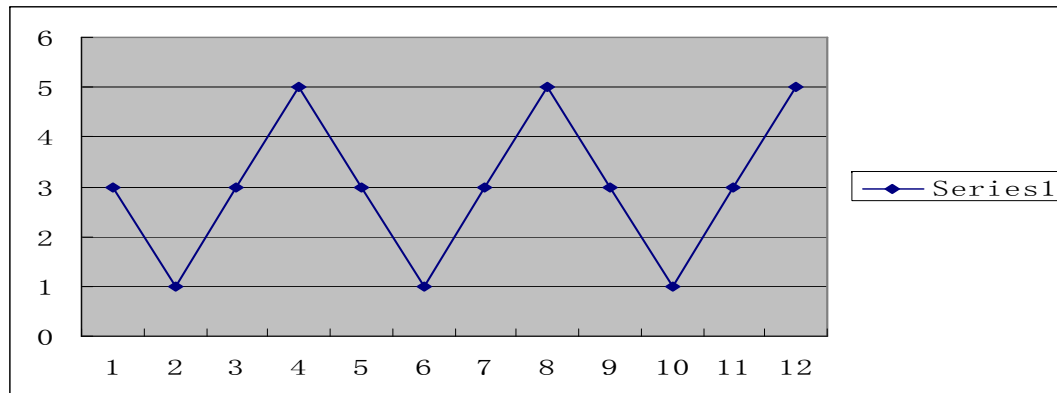
# Post Processing MIR Data

- Post-processing algorithms
  - “Moving variance” algorithm
    - Adapt to the environment dynamically but requires more computation
    - Designed by OSU
    - The basic idea is to track the changes of a statistic variable
    - To avoid the complexity of moving variance computation, another statistics variable was used for mote-based moving object detection
    - If “adapting” feature is not required, offline modeling and online detection can be combined



# Post Processing MIR Data

- More on “Moving variance” algorithm
  - Calculate the variance of the samples
  - Example: Suppose the sensor data in a “quiet” environment is as follows

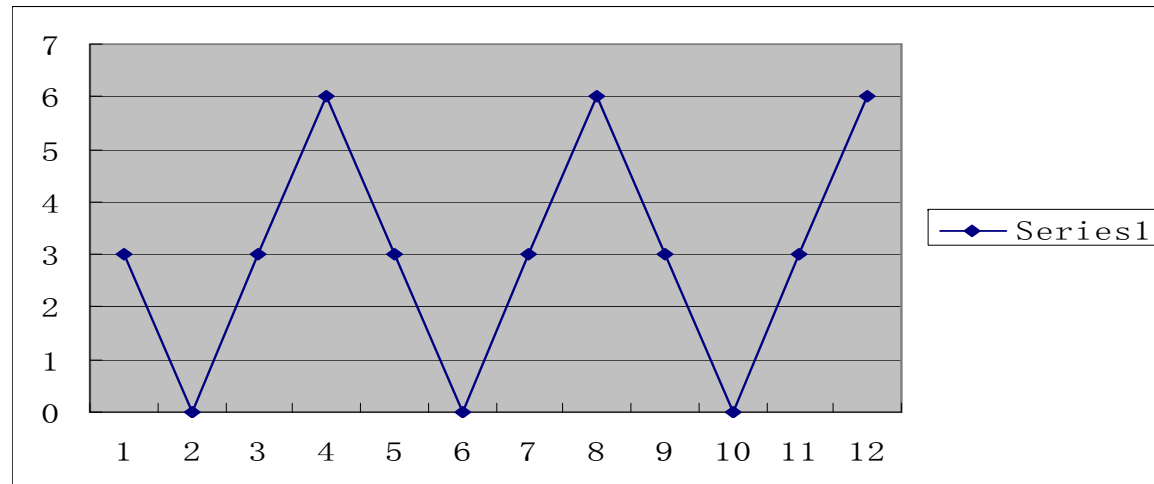


- Mean: 3
- Variance: 2.18

» This is my interpretation of OSU’s algorithm. I have not seen their code or detailed description of it.

# Post Processing MIR Data

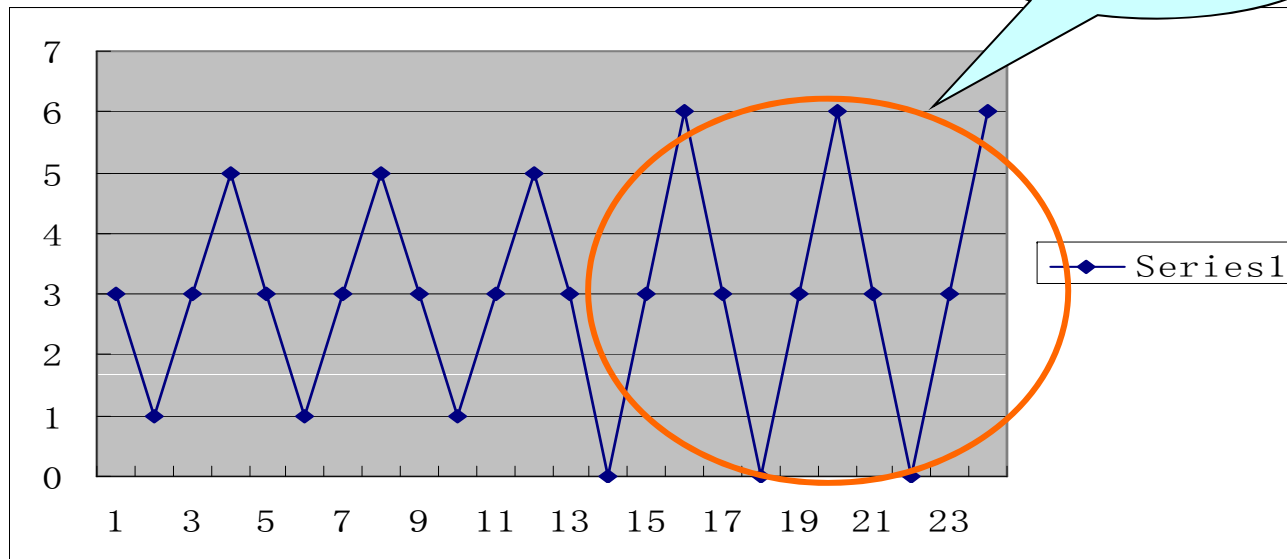
- More on “Moving variance” algorithm
  - Continuously calculate the variance of the recent sampling period
  - When the variance changes, fire a “positive detection” event



- Mean: 3
- Variance: 4.9
  - » This is my interpretation of OSU’s algorithm. I have not seen their code or detailed description of it.

# Post Processing MIR Data

- More on “Moving variance” algorithm
  - Overall, the waveform looks like



- On the right half, a “positive” detection event is fired

# Post Processing MIR Data

- More on “Moving variance” algorithm
  - This technique can be applied to other statistical variables
    - Mean
    - Standard deviation
    - MIN, MAX
  - The main idea is to use the statistics in a recent sampling period to
    - detect “phase change”
    - filter out burst noise reading
- Change in waveform
- **SIGNAL PROCESSING**

# Embedded Systems HW

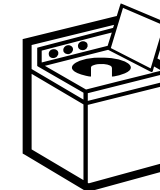
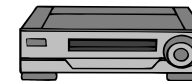
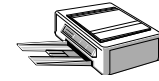
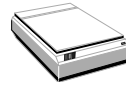
Brian Nielsen

[bnielsen@cs.aau.dk](mailto:bnielsen@cs.aau.dk)

# A “short list” of embedded systems

Anti-lock brakes  
Auto-focus cameras  
Automatic teller machines  
Automatic toll systems  
Automatic transmission  
Avionic systems  
Battery chargers  
Camcorders  
Cell phones  
Cell-phone base stations  
Cordless phones  
Cruise control  
Curbside check-in systems  
Digital cameras  
Disk drives  
Electronic card readers  
Electronic instruments  
Electronic toys/games  
Factory control  
Fax machines  
Fingerprint identifiers  
Home security systems  
Life-support systems  
Medical testing systems

Modems  
MPEG decoders  
Network cards  
Network switches/routers  
On-board navigation  
Pagers  
Photocopiers  
Point-of-sale systems  
Portable video games  
Printers  
Satellite phones  
Scanners  
Smart ovens/dishwashers  
Speech recognizers  
Stereo systems  
Teleconferencing systems  
Televisions  
Temperature controllers  
Theft tracking systems  
TV set-top boxes  
VCR's, DVD players  
Video game consoles  
Video phones  
Washers and dryers



And the list goes on and on

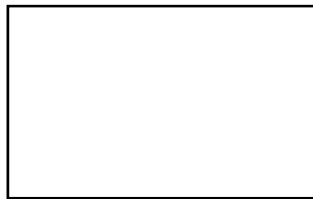
# Processor technology

- Processors vary in their customization for the problem at hand

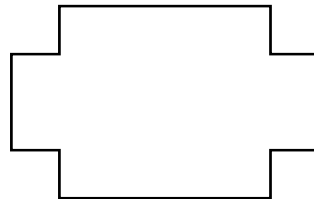


Desired  
functionality

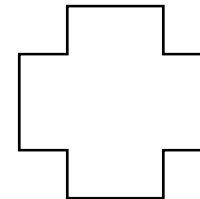
```
total = 0
for i = 1 to N loop
  total += M[i]
end loop
```



General-  
purpose  
processor



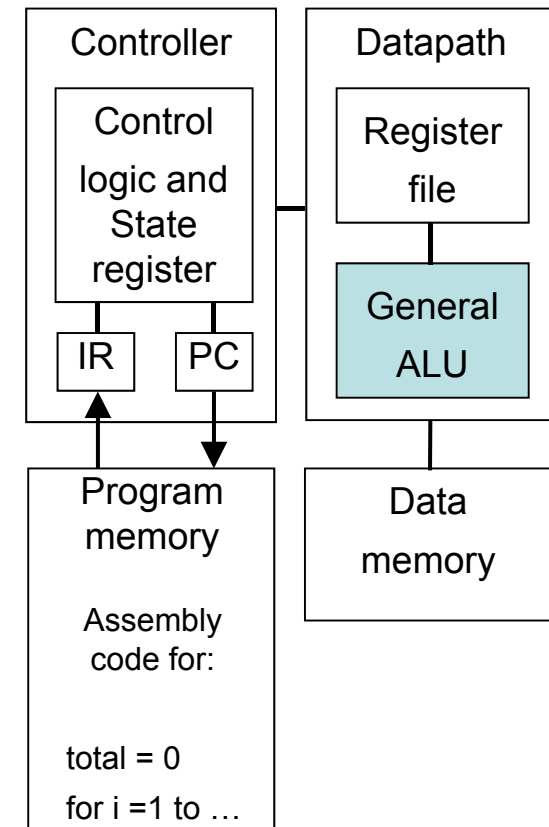
Application-specific  
processor



Single-  
purpose  
processor

# General-purpose processors

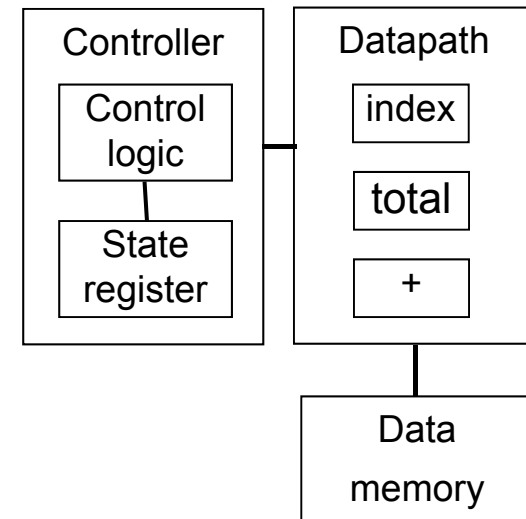
- Programmable device used in a variety of applications
  - Also known as “microprocessor”
- Features
  - Program memory
  - General datapath with large register file and general ALU
- User benefits
  - Low time-to-market and NRE costs
  - High flexibility
- “Pentium” the most well-known, but there are hundreds of others





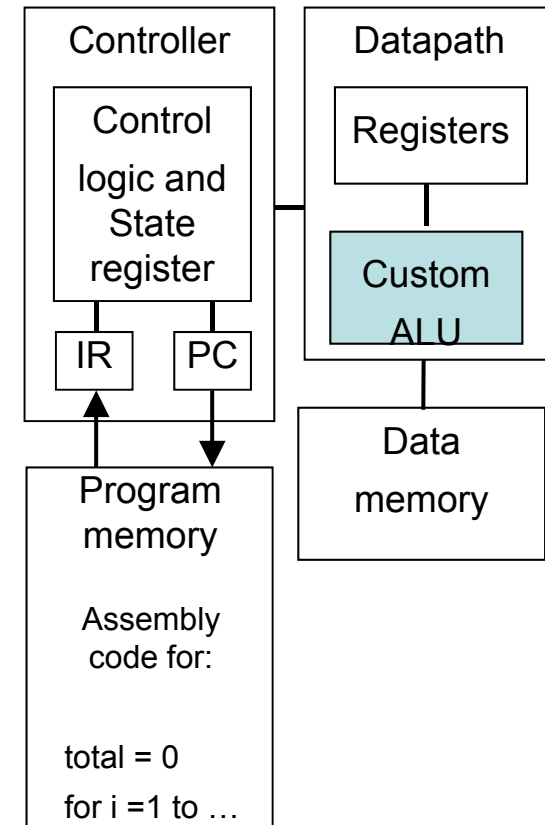
# Single-purpose processors

- Digital circuit designed to execute exactly one program
  - a.k.a. coprocessor, accelerator or peripheral
  - JPEG codec
- Features
  - Contains only the components needed to execute a single program
  - No program memory
- Benefits
  - Fast
  - Low power
  - Small size



# Application-specific processors

- Programmable processor optimized for a particular class of applications having common characteristics
  - Compromise between general-purpose and single-purpose processors
  - EG microController, DSP
- Features
  - Program memory
  - Optimized datapath
  - Special functional units
- Benefits
  - Some flexibility, good performance, size and power

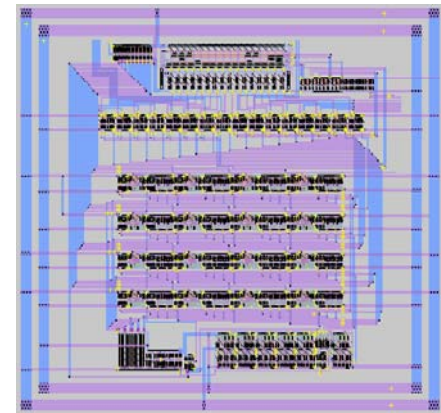


# IC technology

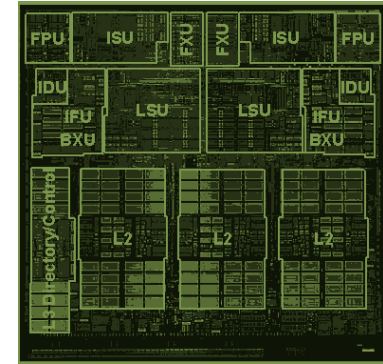
- Three types of IC technologies
  - Full-custom/VLSI
  - Semi-custom ASIC (Application Specific Integrated Circuit)
  - PLD (Programmable Logic Device)

# Full-custom/VLSI

- All layers are optimized for an embedded system's particular digital implementation
  - Placing transistors
  - Sizing transistors
  - Routing wires
- Benefits
  - Excellent performance, small size, low power
- Drawbacks
  - High NRE cost (e.g., \$300k), long time-to-market
  - NRE=Non Recurring Engineering (design)



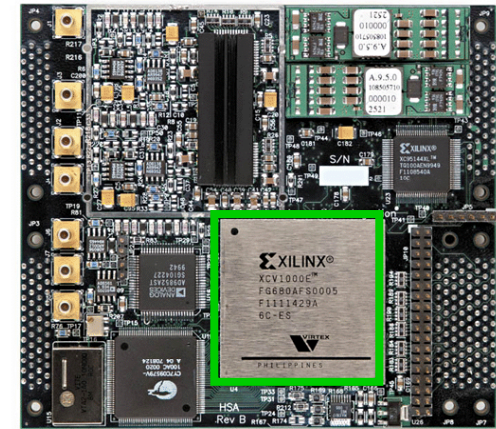
# Semi-custom



- Lower layers are fully or partially built
  - Designers are left with routing of wires and maybe placing some blocks
- Benefits
  - Good performance, good size, less NRE cost than a full-custom implementation (perhaps \$10k to \$100k)
- Drawbacks
  - Still require weeks to months to develop

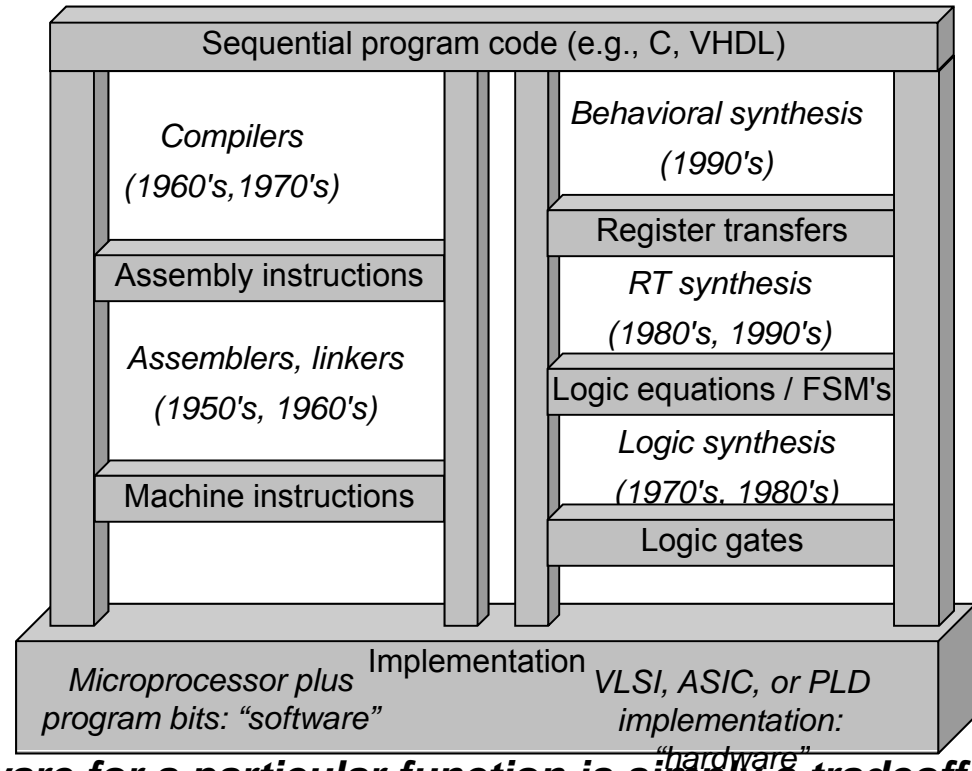
# PLD (Programmable Logic Device)

- All layers already exist
  - Designers can purchase an IC
  - Connections on the IC are either created or destroyed to implement desired functionality
    - Field-Programmable Gate Array (FPGA) very popular
- Benefits
  - Low NRE costs, almost instant IC availability
- Drawbacks
  - Bigger, expensive (perhaps \$30 per unit), power hungry, slower



# The co-design ladder

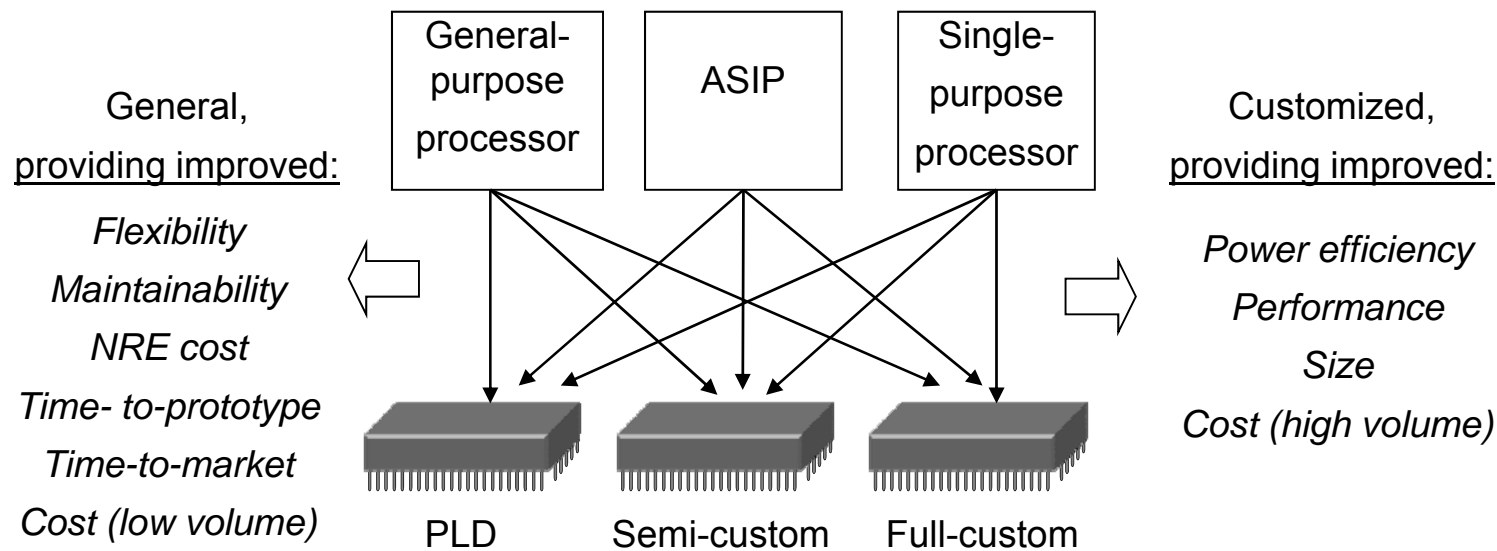
- In the past:
  - Hardware and software design technologies were very different
  - Recent maturation of synthesis enables a unified view of hardware and software
- Hardware/software “codesign”



***The choice of hardware versus software for a particular function is simply a tradeoff among various design metrics, like performance, power, size, NRE cost, and especially flexibility; there is no fundamental difference between what hardware or software can implement.***

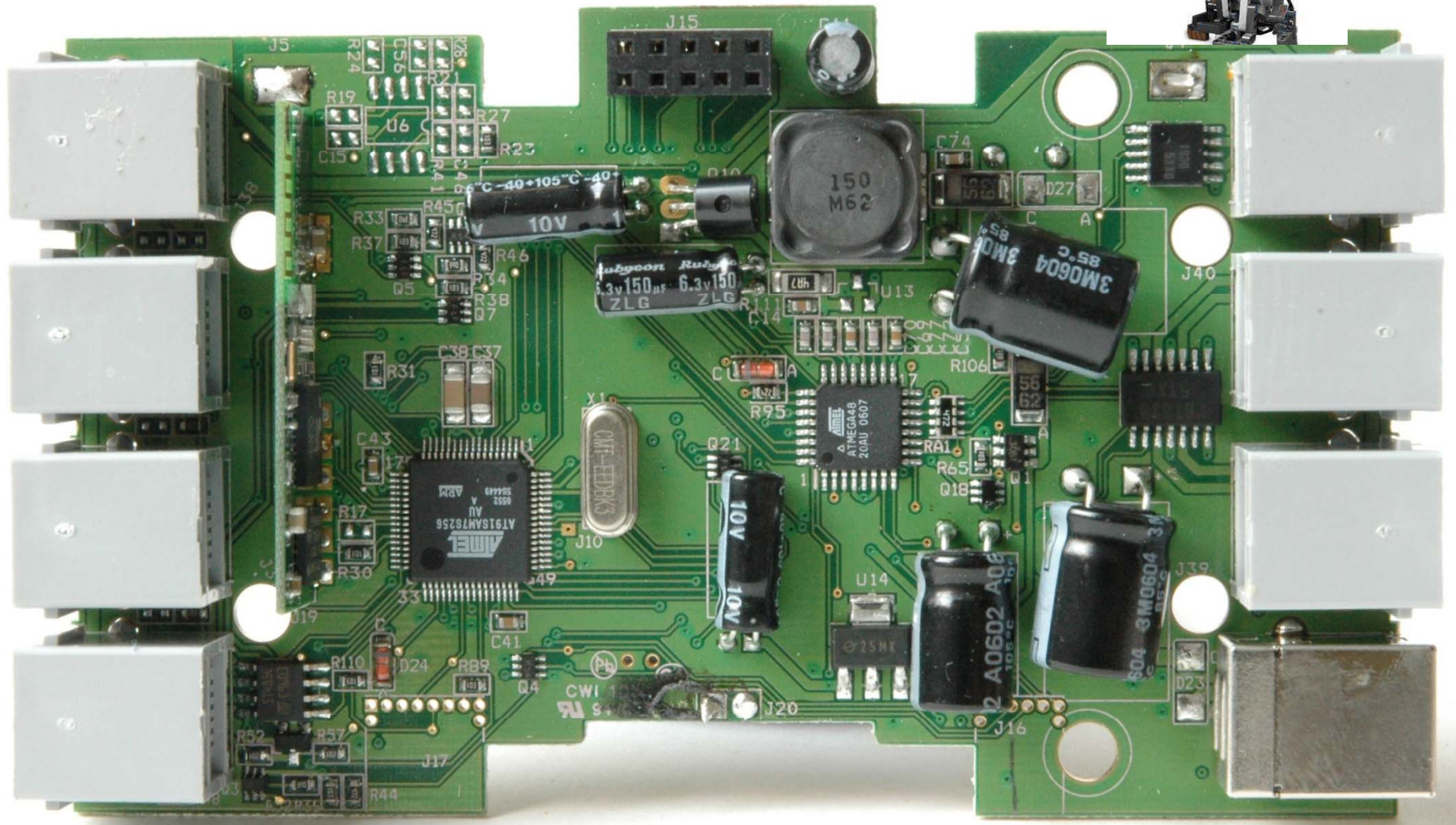
# Independence of processor and IC technologies

- Basic tradeoff
  - General vs. custom
  - With respect to processor technology or IC technology
  - The two technologies are independent

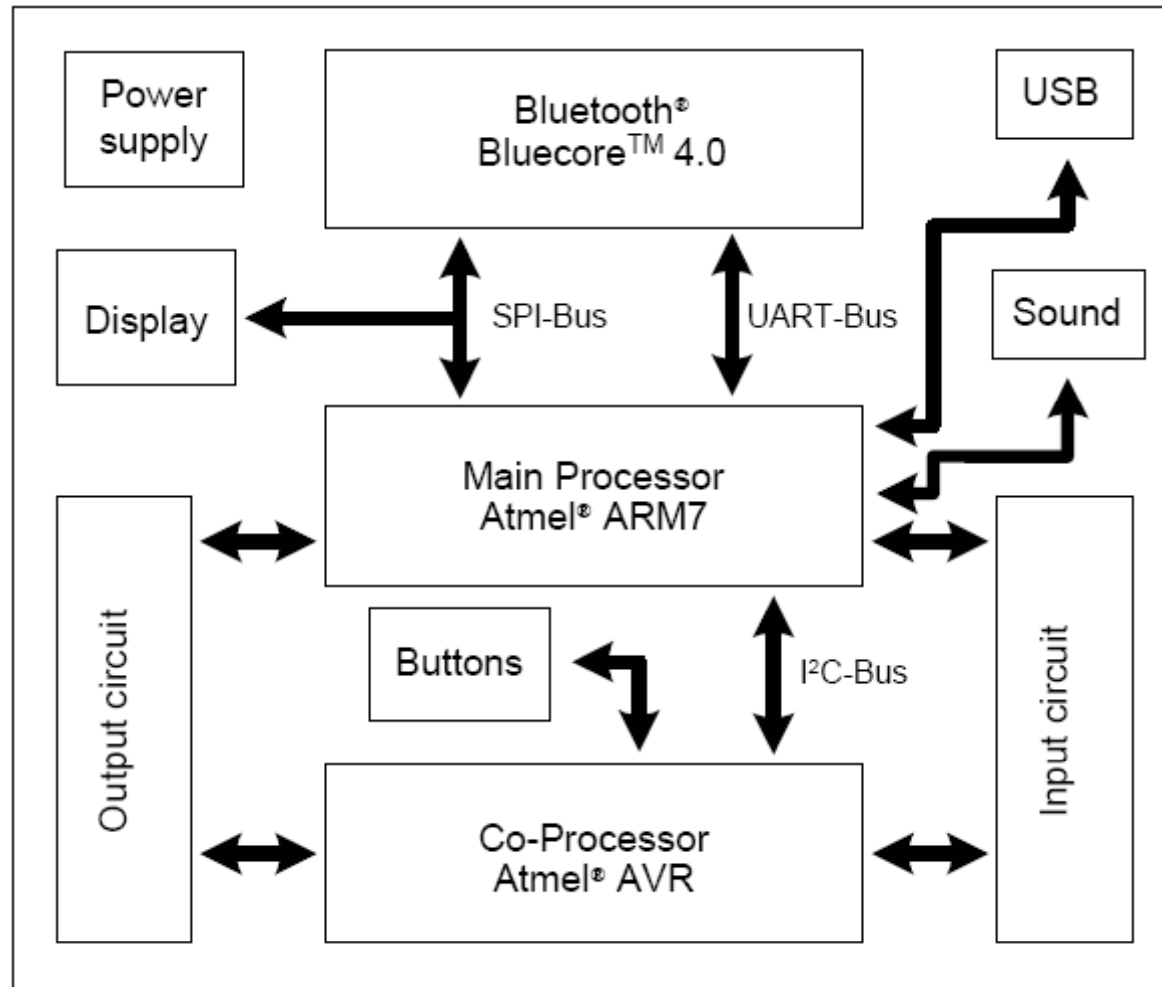




# NXT

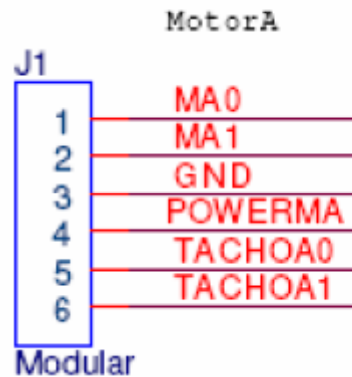


# NXT HW Block Diagram



- **Atmel 32 bit ARM**
- 48 MHz
- 256 KB Flash
- 64 KB RAM
- **8 bit AVR** (ATmega48)
- 4KB FLASH
- 512 B RAM
- 8 MHz

# Output Ports



Pin 1, MA0

PWM output signal for the actuators

Pin 2, MA1

PWM output signal for the actuators

Pin 3, GND

Ground signal related to the output supply

Pin 4, POWERMA

4.3 Volt output supply

Pin 5, TACHOA0

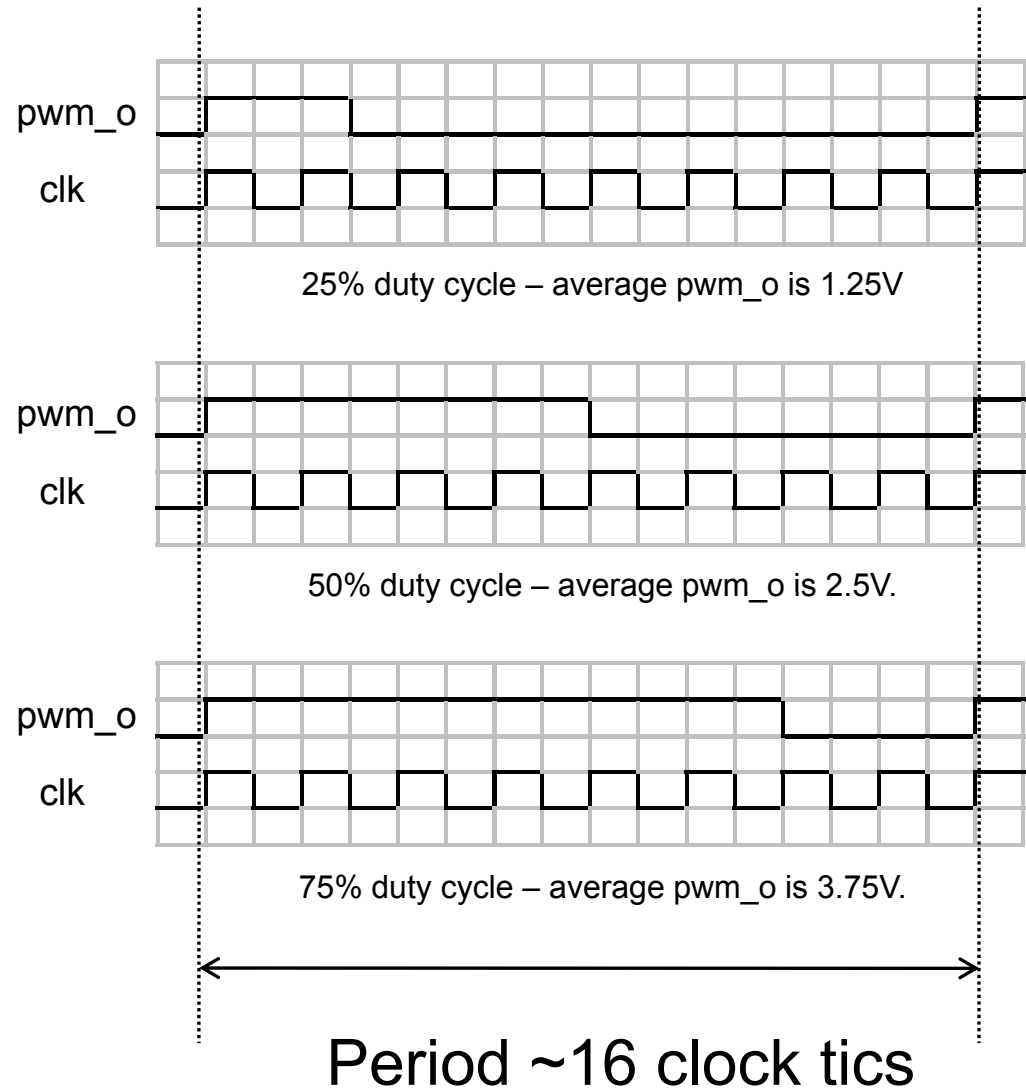
Input value that includes Schmitt trigger functionality

Pin 6, TACHOA1

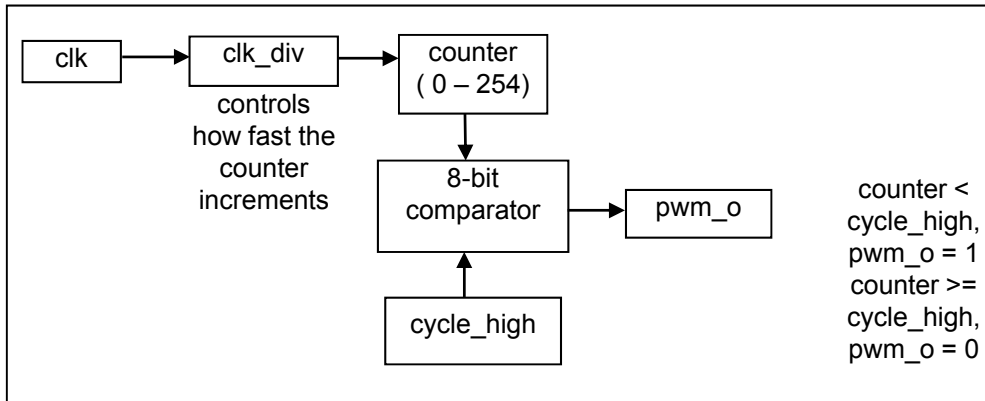
Input value that includes Schmitt trigger functionality

# Pulse width modulator

- Generates pulses with specific high/low times
- Duty cycle: % time high
  - Square wave: 50% duty cycle
- Common use: control average voltage to electric device
  - Simpler than DC-DC converter or digital-analog converter
  - DC motor speed, dimmer lights
- Another use: encode commands, receiver uses timer to decode



# Controlling a DC motor with a PWM



Internal Structure of PWM

Input Voltage	% of Maximum Voltage Applied	RPM of DC Motor
0	0	0
2.5	50	1840
3.75	75	6900
5.0	100	9200

Relationship between applied voltage and speed of the DC Motor

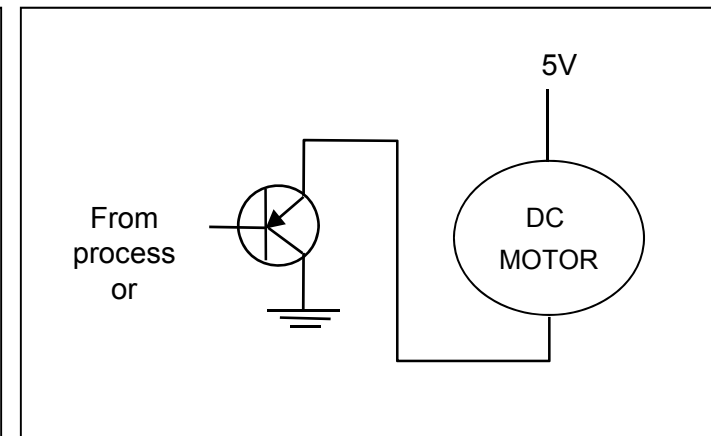
```

void main(void){

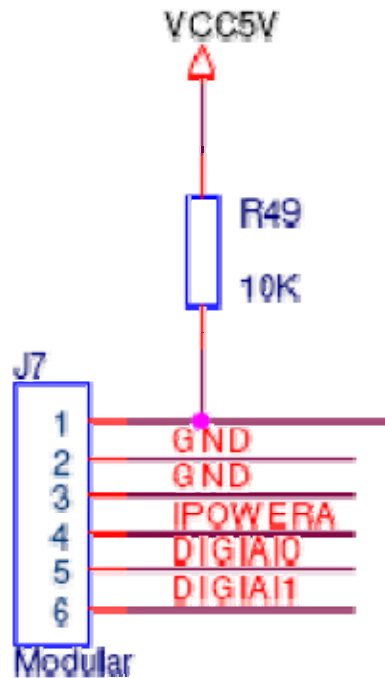
  /* controls period */
  PWMP = 0xff;
  /* controls duty cycle */
  PWM1 = 0x7f;

  while(1){};
}
  
```

The PWM alone cannot drive the DC motor, a possible way to implement a driver is shown below using an MJE3055T NPN transistor.



# Input Ports



- Pin 1, ANA Analog Input and possible current output signal
- Pin 2, GND Ground signal
- Pin 3, GND Ground signal
- Pin 4, IPOWERA 4.8 Volt output supply
- Pin 5, DIGIAIO Digital I/O pin connected to the ARM7 processor
- Pin 6, DIGIAI1 Digital I/O pin connected to the ARM7 processor

- 10 bit AD, 333 Hz (By AVR processor)
- Dig I/O (I2C bus communication -9600bit/s)
- Port 4 - RS484 (921.6 Kbit/s)

# Input Sensors

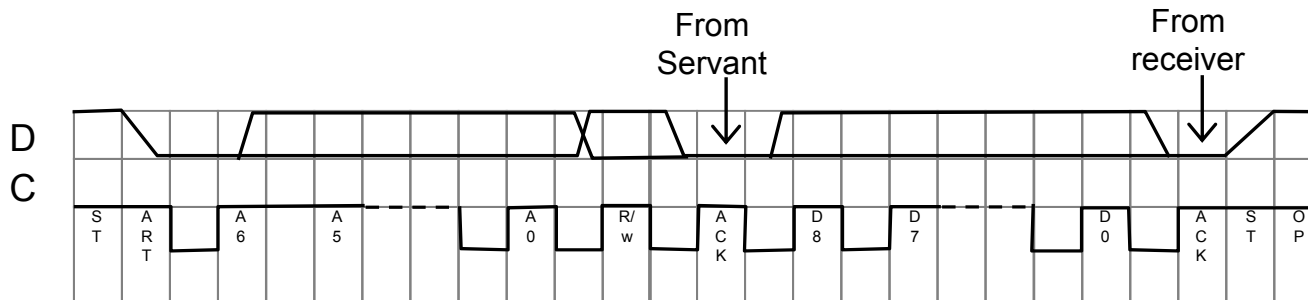
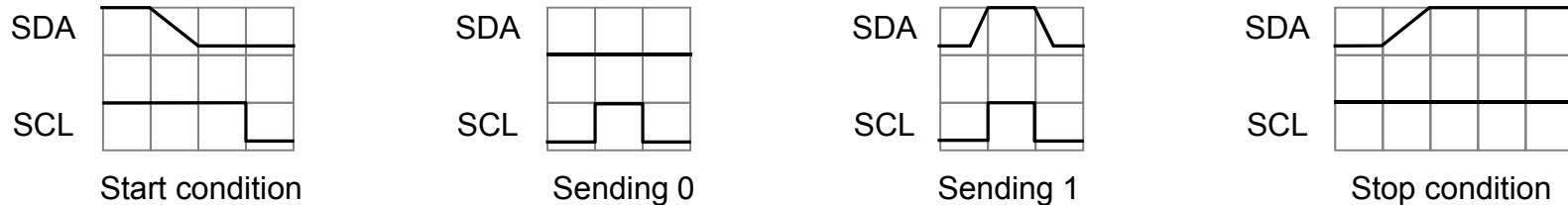
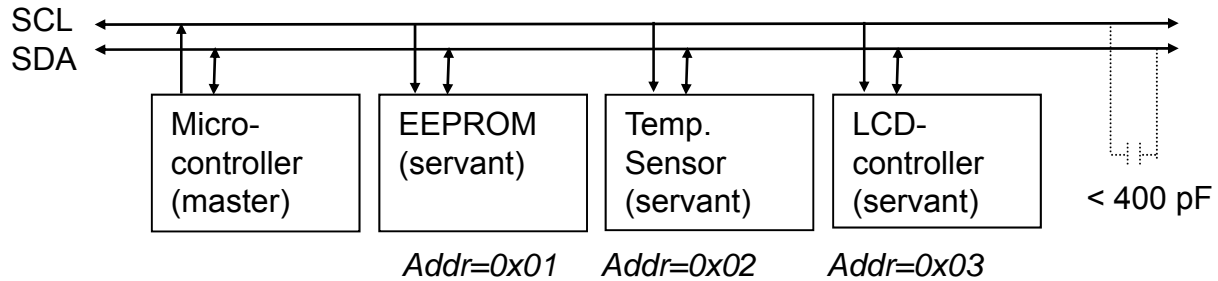
- Passive
  - Light, Touch, Sound, Temp
- Digital
  - UltraSonic
  - I2C
- => Port configuration depends on sensor

# Serial protocols: I<sup>2</sup>C

- I<sup>2</sup>C (Inter-IC)
  - Two-wire serial bus protocol developed by Philips Semiconductors nearly 20 years ago
  - Enables peripheral ICs to communicate using simple communication hardware
  - Data transfer rates up to 100 kbits/s and 7-bit addressing possible in normal mode
  - 3.4 Mbits/s and 10-bit addressing in fast-mode
  - Common devices capable of interfacing to I<sup>2</sup>C bus:
    - EPROMS, Flash, and some RAM memory, real-time clocks, watchdog timers, and microcontrollers



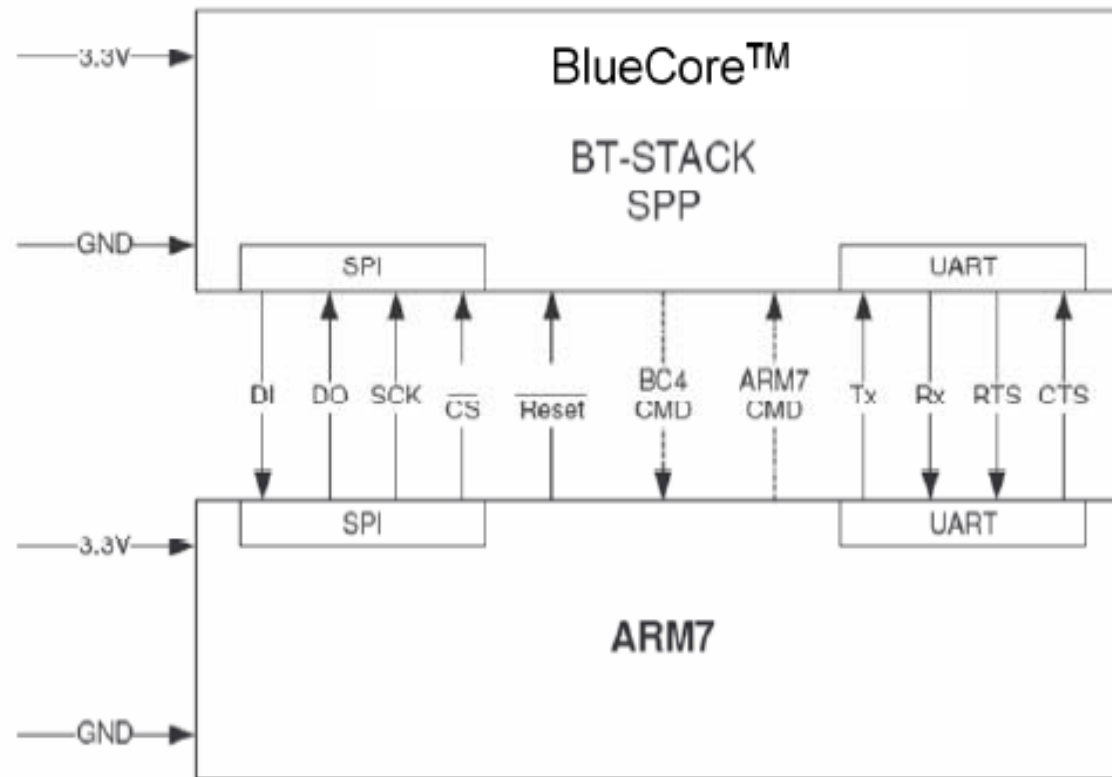
# I2C bus structure



Typical read/write cycle

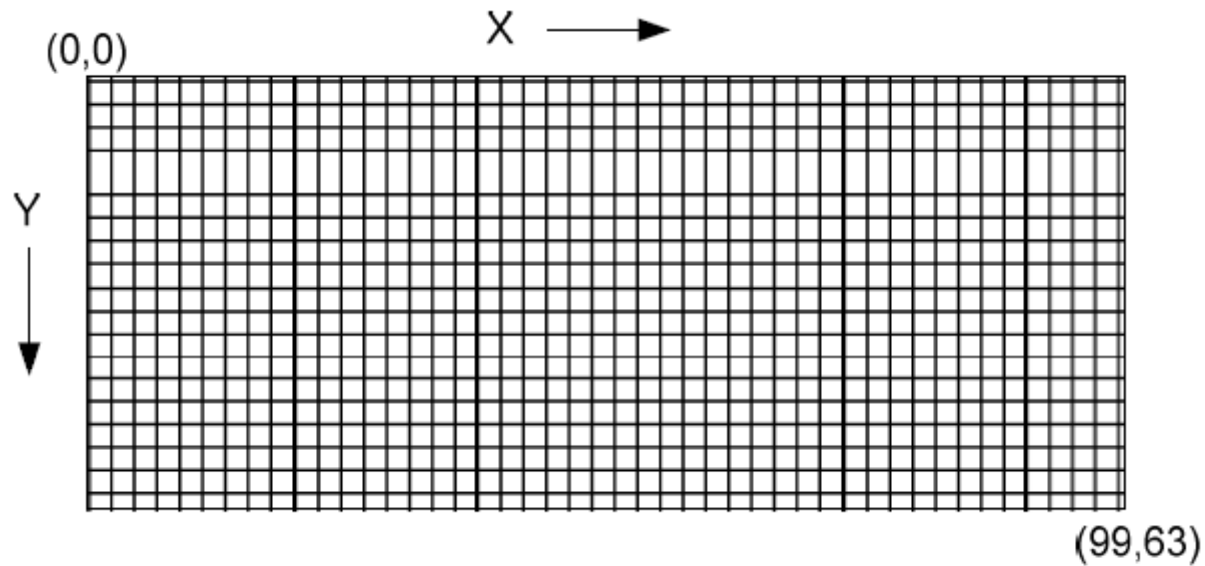
# Bluetooth (classII)

- Serial Port Profile



# Display

- 100x64 pixel
- ARM 7 via SPI (2MHZ)
- Double Buffering in Firmware



# Other

- Sound (PWM by ARM7)
- USB
- Buttons
- JTAG debug (not mounted) for ARM&AVR



# AVR <-> ARM

- AVR
  - Power management
  - PWM modulation for engines
  - AD conversion for analogue input ports
  - Buttons
- Exchanged info via internal i2c every 2 ms

## ARM to AVR

```
typedef struct
{
    UBYTE    Power;
    UBYTE    PwmFreq;
    SBYTE    PwmValue[NOS_OF_AVR_OUTPUTS];
    UBYTE    OutputMode;
    UBYTE    InputPower;
} IOTOAVR;
```

## AVR to ARM

```
typedef struct
{
    UWORD    AdValue[NOS_OF_AVR_INPUTS];
    UWORD    Buttons;
    UWORD    Battery;
} IOFROMAVR;
```

# Basic Sampling

Brian Nielsen

[bnielsen@cs.aau.dk](mailto:bnielsen@cs.aau.dk)

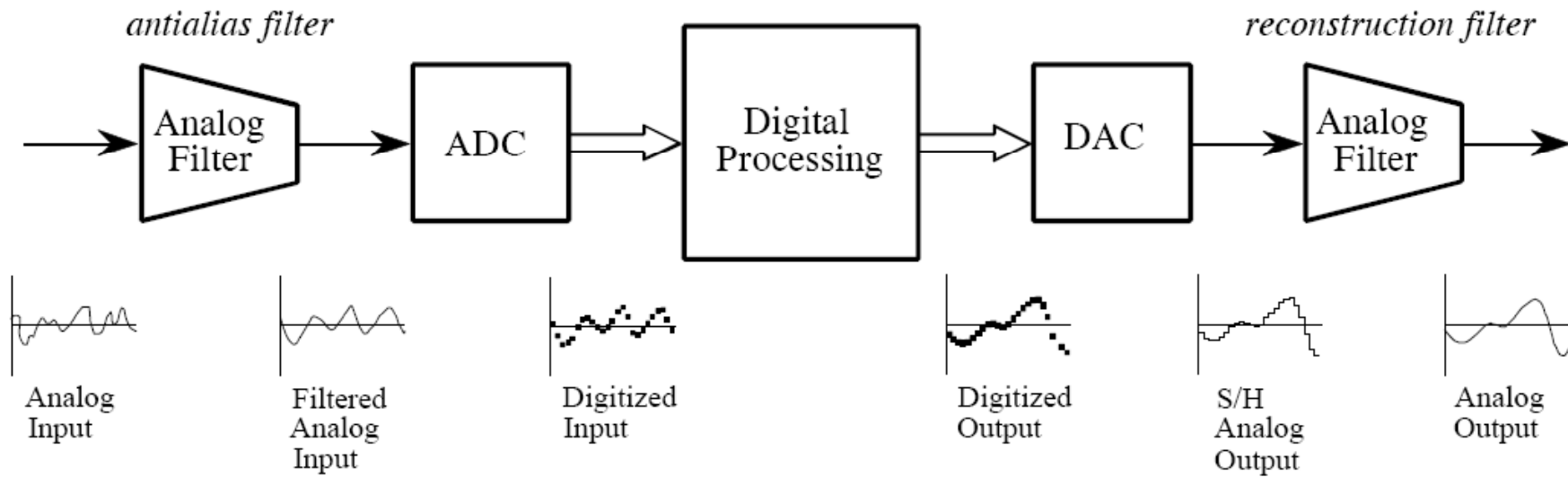
Based on Chapter 3:

"The Scientist and Engineer's Guide to Digital Signal Processing, copyright ©1997-1998 by Steven W. Smith.

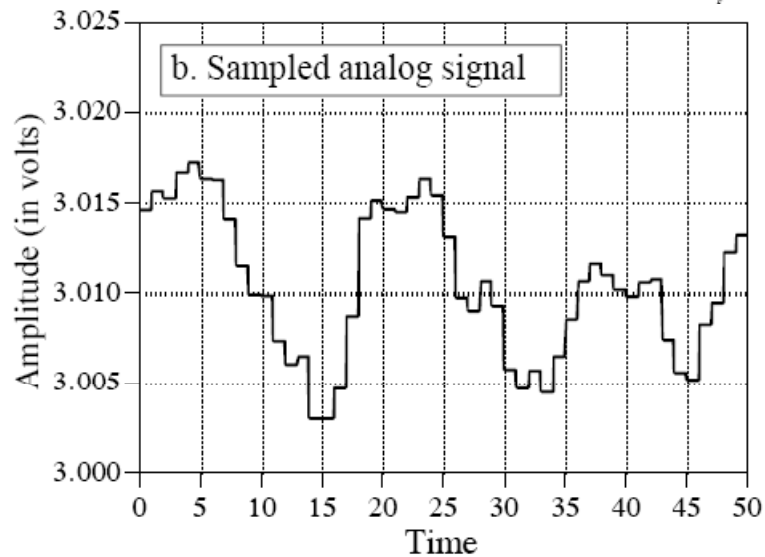
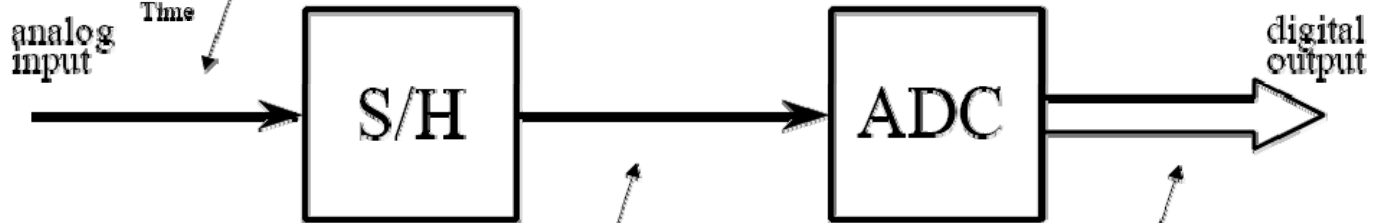
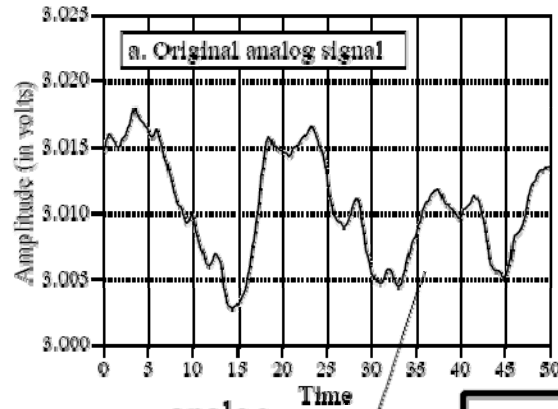
For more information visit the book's website at:

[www.DSPguide.com](http://www.DSPguide.com)"

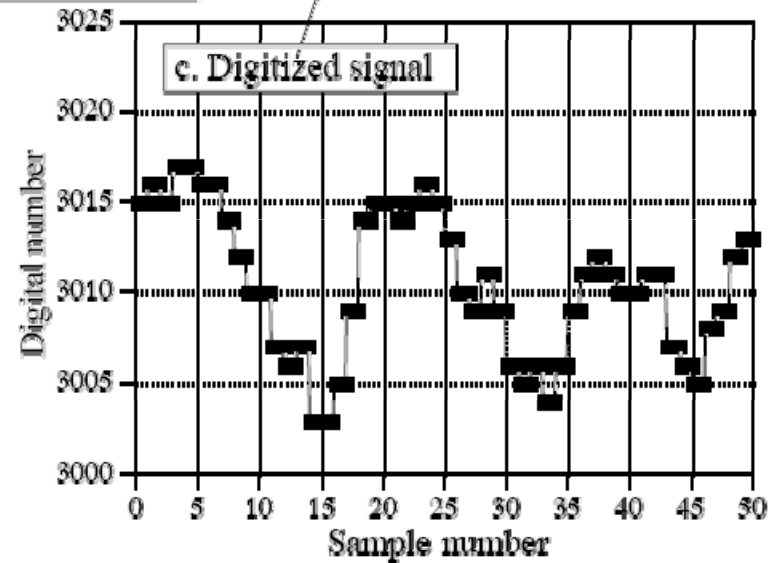
# AD and DC



# AD Conversion

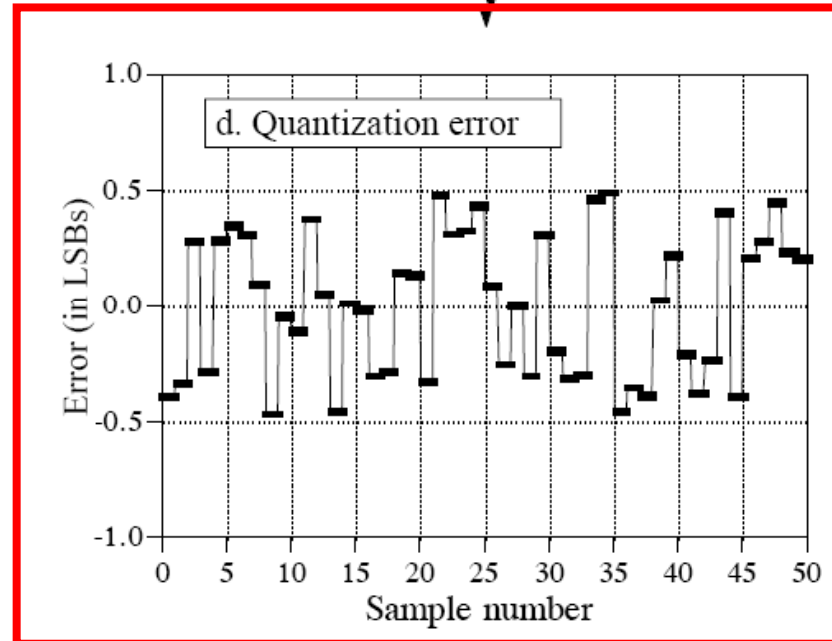
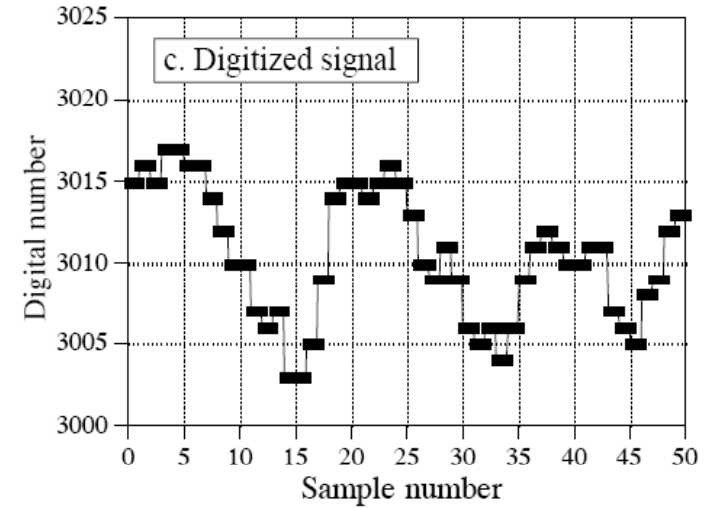
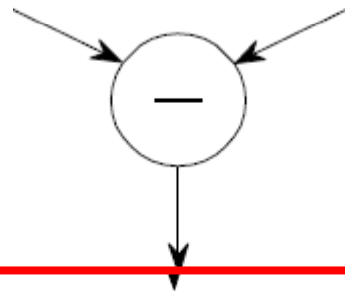
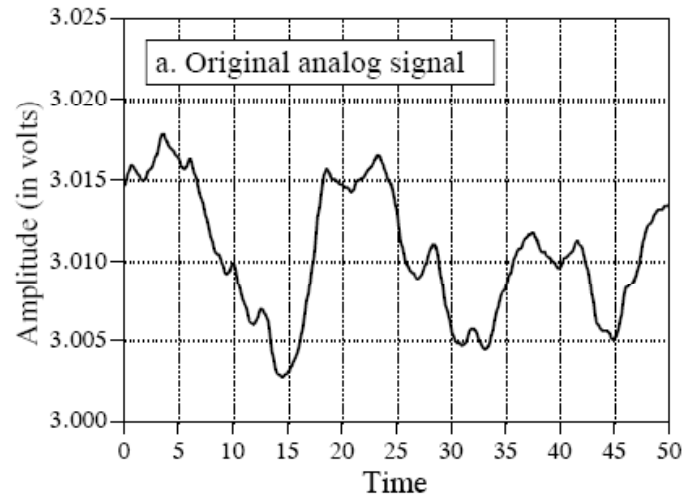


Quantization: number of levels  
Sampling Frequency: samples/sec





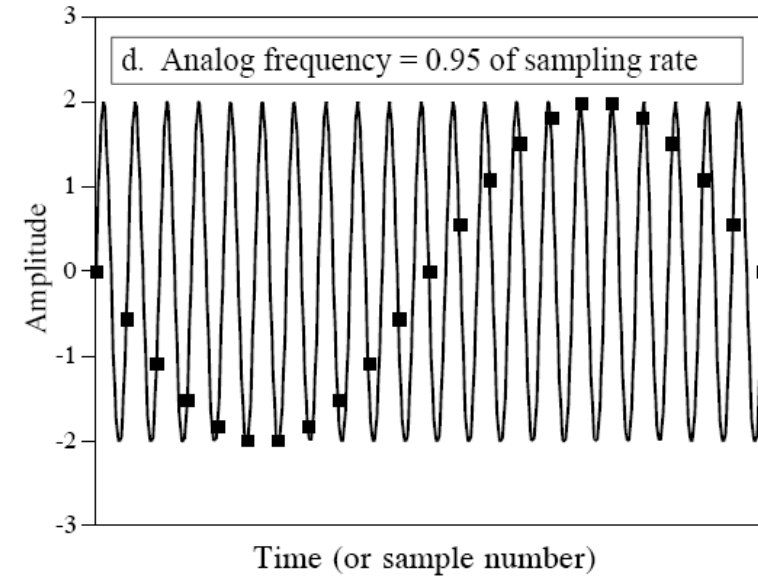
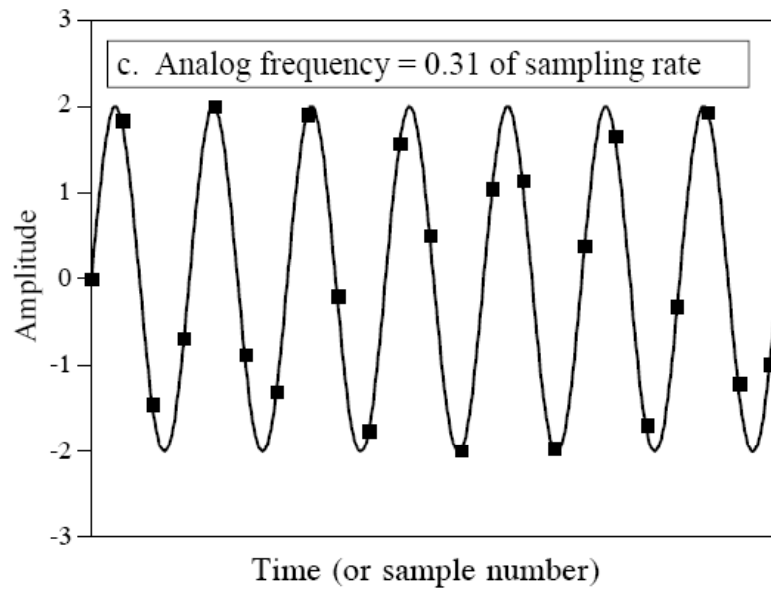
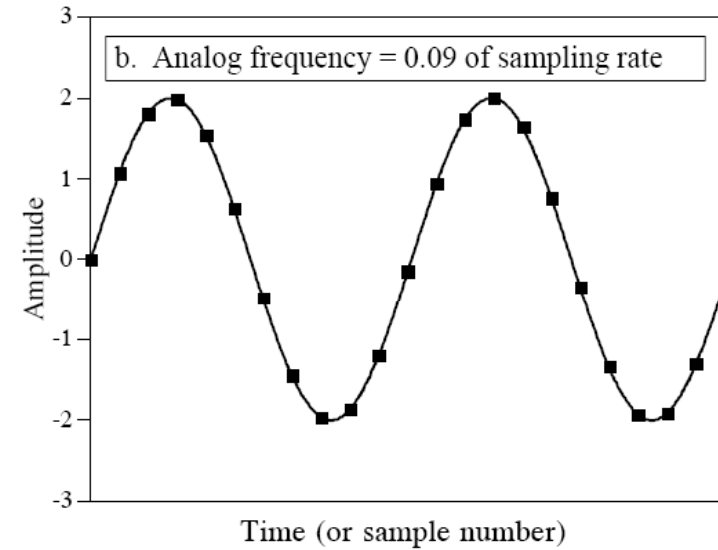
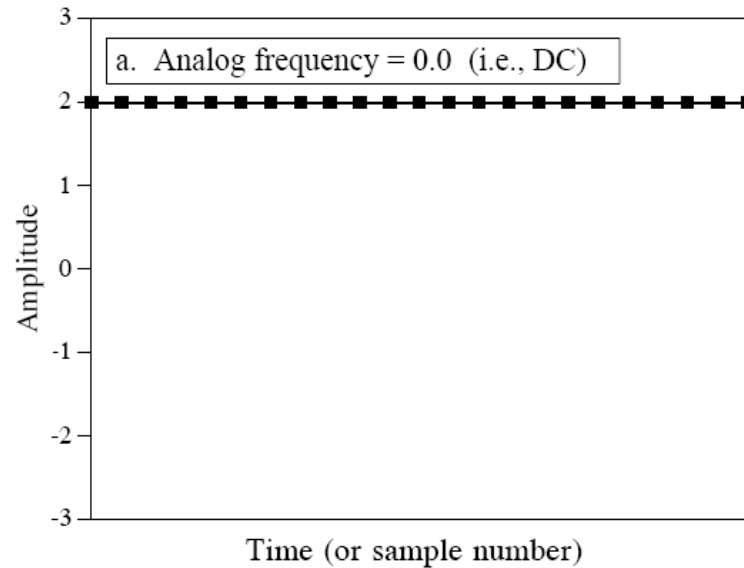
# Quantization Error



# Precision

- $Q = E_{\text{FSR}} / N$  (if linear)
  - $Q$  is resolution in volts per step (volts per output code),
  - $E_{\text{FSR}}$  is the full scale voltage range =  $V_H - V_L$ ,
  - $M$  is the ADC's resolution in bits
  - $N$  is the number of steps (output codes):  
 $N = 2^M$
- E.G.
  - $Q = (10-0)/2^{12}$  V/code = 2.44 mV/code

# Aliasing



# Sampling Theorem

- To reconstruct the frequency content of a measured signal accurately, the sample rate must be more than twice the highest frequency contained in the measured signal

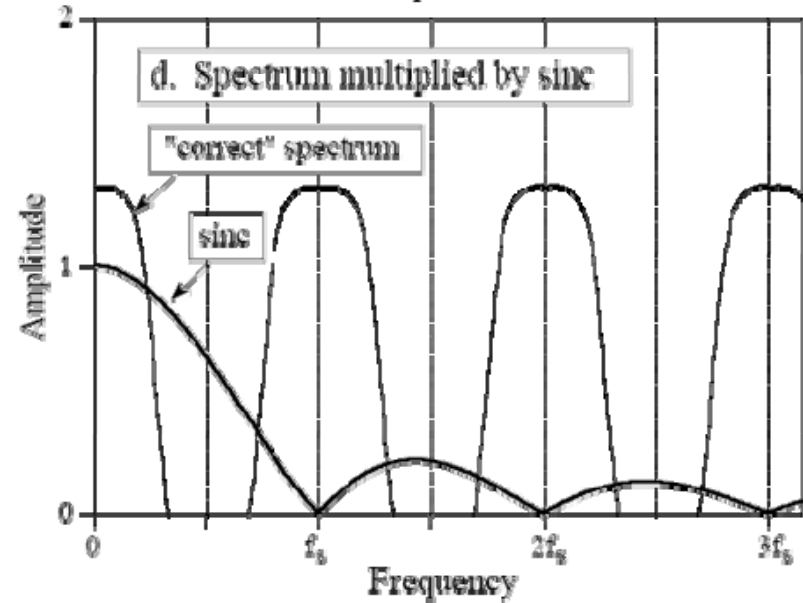
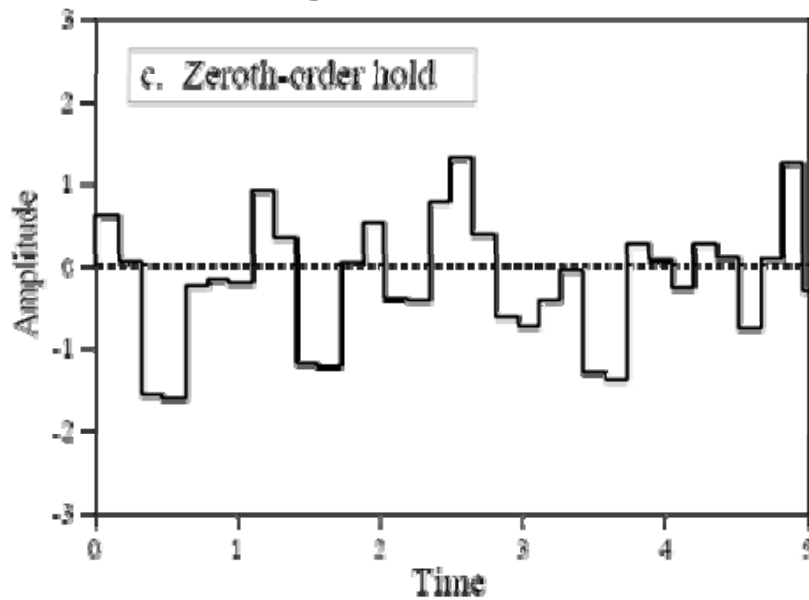
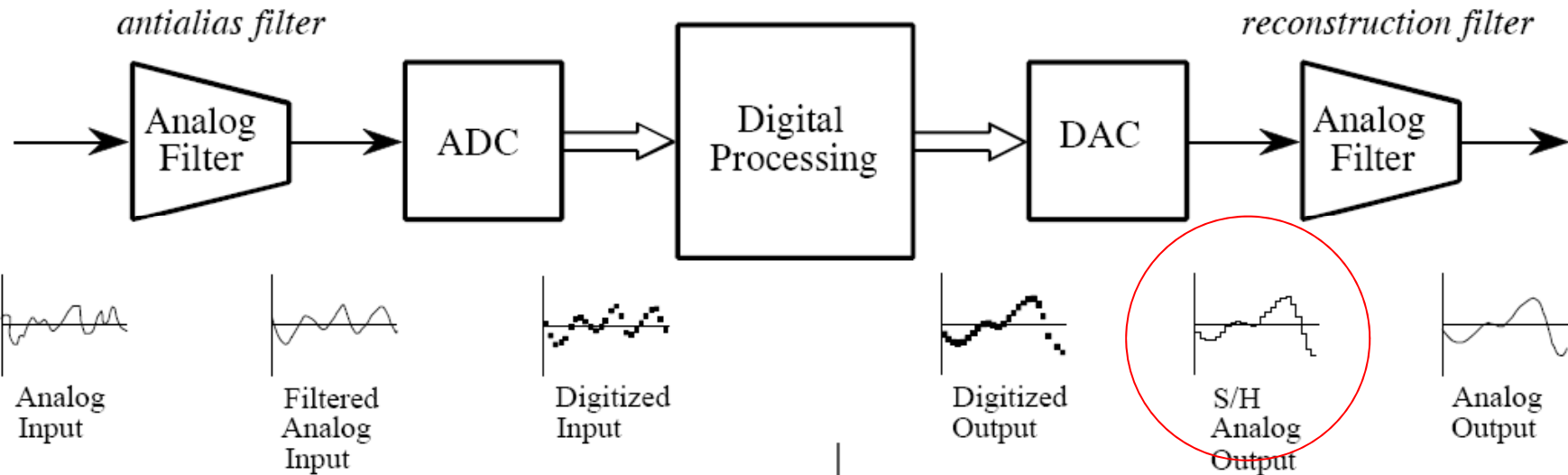
$$f_s > 2f_m$$

$$\delta t < \frac{1}{2f_m}$$

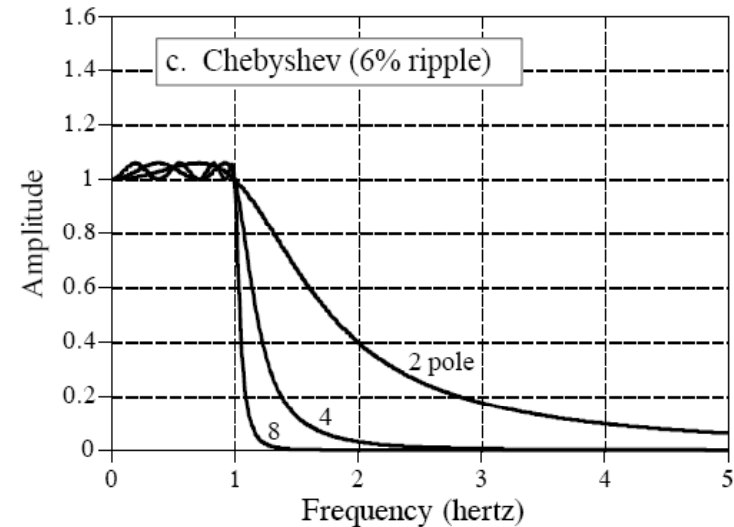
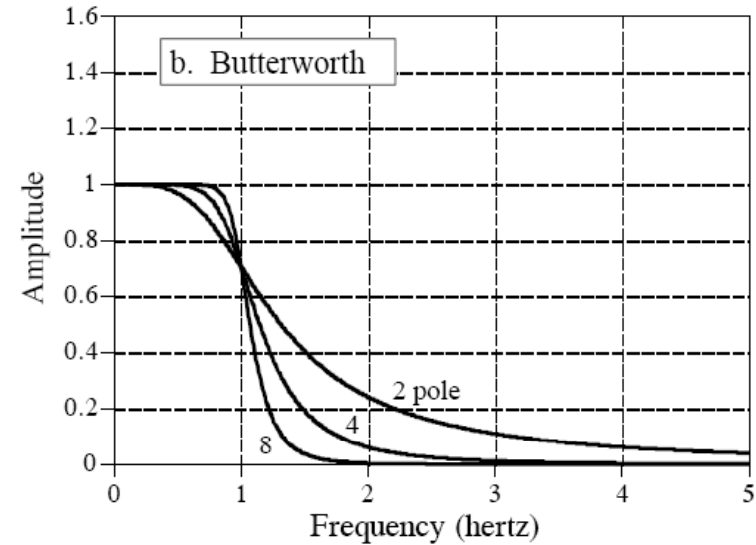
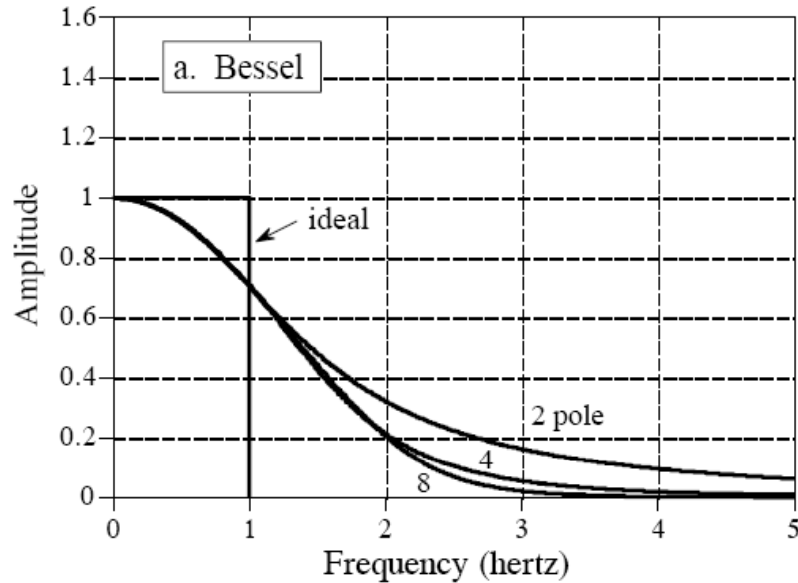
- Nyquist Frequency (half sampling frequency)

$$f_N = \frac{f_s}{2} = \frac{1}{2\delta t}$$

# AD/DC



# Low-pass filters



- Sharpness
- Attenuation
- Ripple / Over-undershoot