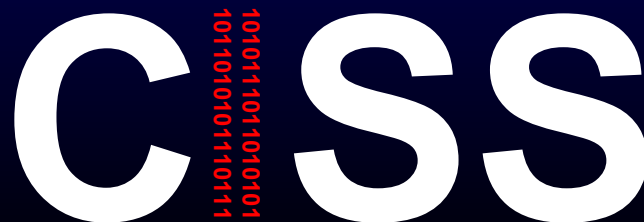


# FSM-test generation

Brian Nielsen

bnielsen@cs.auc.dk

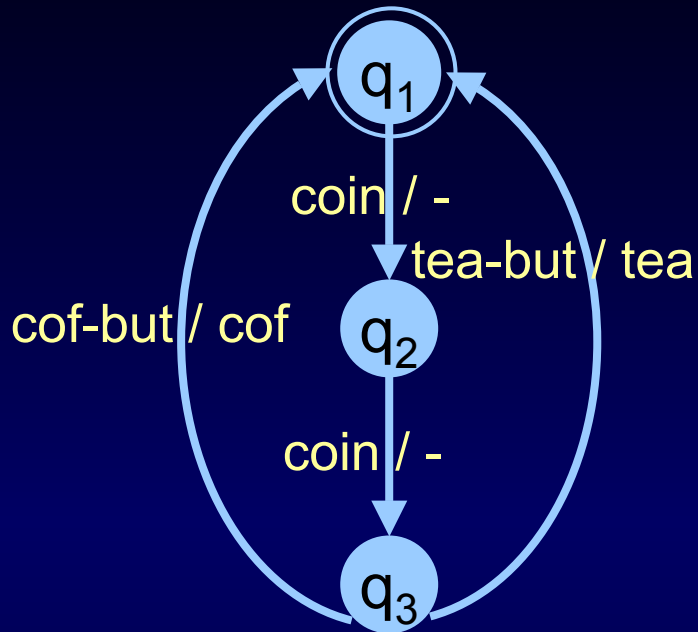
Department of Computer Science,  
Aalborg University, Denmark



# Menu

- Review of basic definitions and fundamental results
- Classical Deterministic Untimed (very) finite FSMs
- Conformance Testing with FSMs
  - Transition Testing
  - Synchronizing sequences
  - State identification and verification
  - State and transition covering sequences

# Finite State Machine (Mealy)



condition		effect	
current state	input	output	next state
q <sub>1</sub>	coin	-	q <sub>2</sub>
q <sub>2</sub>	coin	-	q <sub>3</sub>
q <sub>3</sub>	cof-but	cof	q <sub>1</sub>
q <sub>3</sub>	tea-but	tea	q <sub>1</sub>

Inputs = {cof-but, tea-but, coin}

Outputs = {cof, tea}

States: {q<sub>1</sub>, q<sub>2</sub>, q<sub>3</sub>}

Initial state = q<sub>1</sub>

Transitions= {

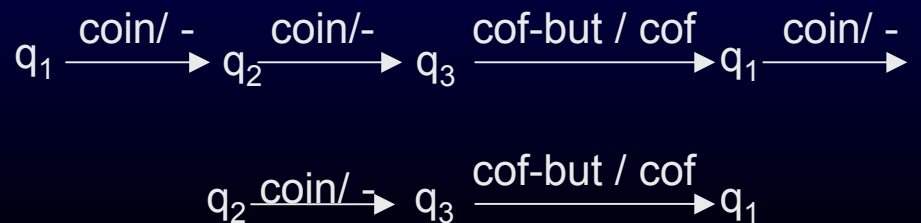
(q<sub>1</sub>, coin, -, q<sub>2</sub>),

(q<sub>2</sub>, coin, -, q<sub>3</sub>),

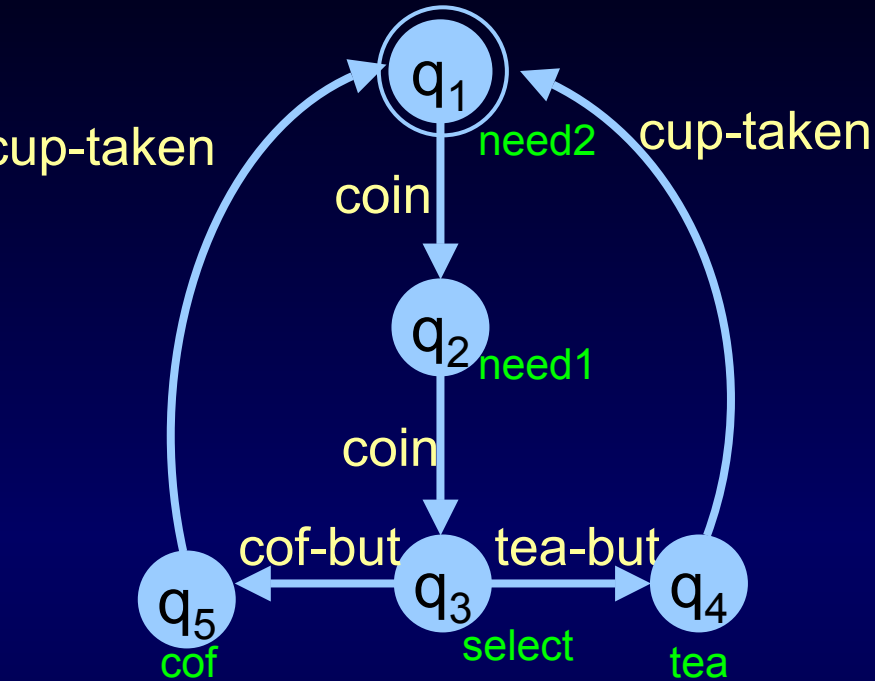
(q<sub>3</sub>, cof-but, cof, q<sub>1</sub>),

(q<sub>3</sub>, tea-but, tea, q<sub>1</sub>)

Sample run:



# Finite State Machine (Moore)



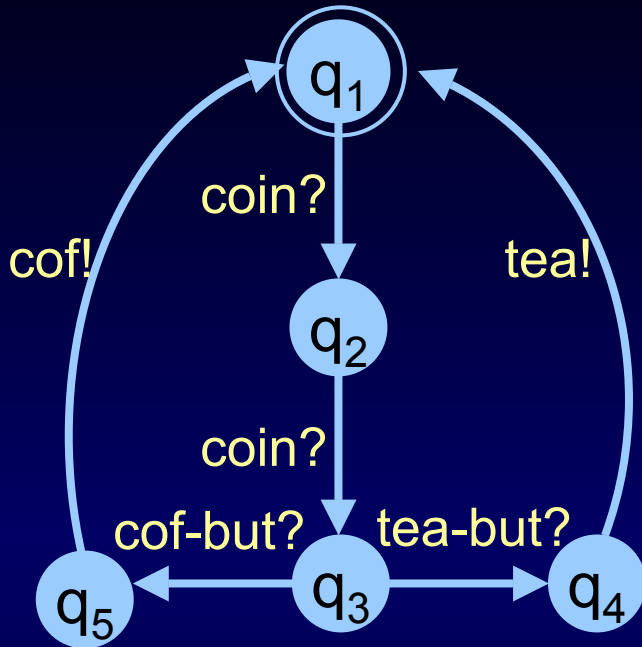
condition		effect	
current state	input	Activity	next state
$q_1$	coin	need2	$q_2$
$q_2$	coin	need1	$q_3$
$q_3$	cof-but	select	$q_5$
$q_3$	tea-but	select	$q_4$
$q_5$	cup-taken	cof	$q_1$
$q_4$	cup-taken	tea	$q_1$

Input sequence: coin.coin.cof-but.coin.coin.cof-but

Output sequence: need2.need1.select.cof. need2.need1.select.cof

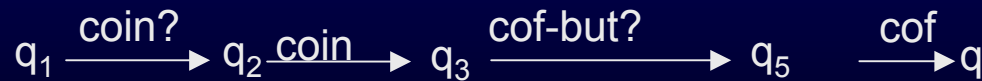
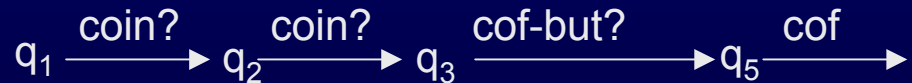
*need2=display shows "insert two coins"*

# IO-FSM



condition		effect
current state	action	next state
q <sub>1</sub>	coin?	q <sub>2</sub>
q <sub>2</sub>	coin?	q <sub>3</sub>
q <sub>3</sub>	cof-but!	q <sub>5</sub>
q <sub>3</sub>	tea-but!	q <sub>4</sub>
q <sub>4</sub>	cof?	q <sub>1</sub>
q <sub>5</sub>	tea!	q <sub>1</sub>

Sample run:



action trace: coin?.coin?.cof!-coin?.coin?.cof!

input sequence: coin.coin.coin.coin

Output sequence: cof.cof

Inputs = {cof-but, tea-but, coin}

Outputs = {cof,tea}

States: {q<sub>1</sub>,q<sub>2</sub>,q<sub>3</sub>}

Initial state = q<sub>1</sub>

Transitions= {

(q<sub>1</sub>, coin, q<sub>2</sub>),

(q<sub>2</sub>, coin, q<sub>3</sub>),

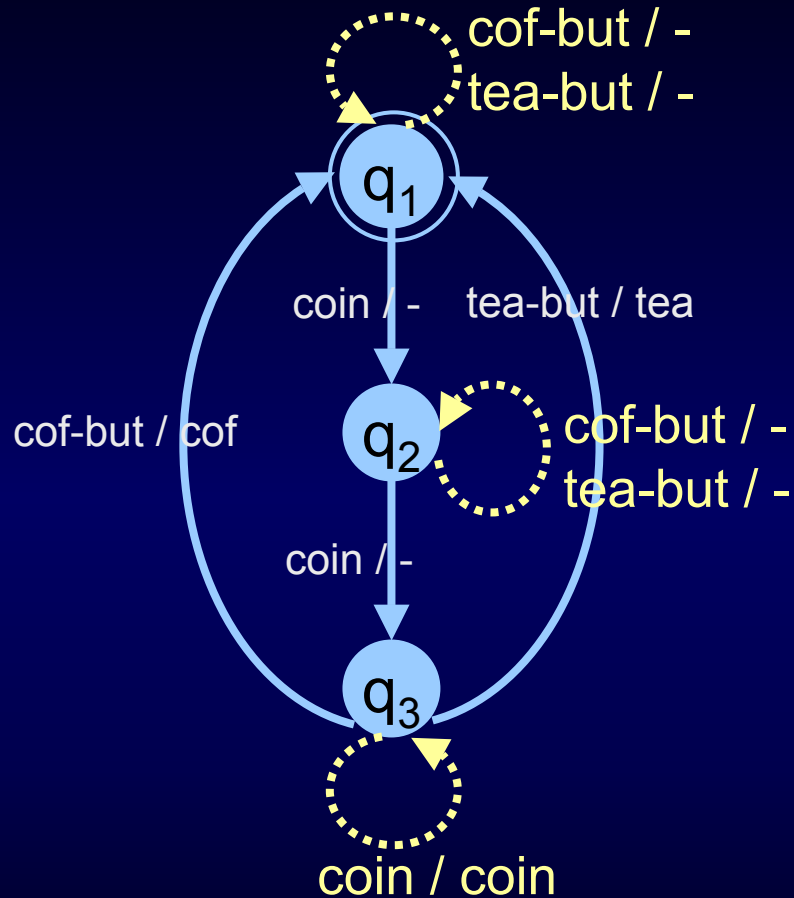
(q<sub>3</sub>, cof-but, q<sub>5</sub>),

(q<sub>3</sub>, tea-but, q<sub>4</sub>),

(q<sub>4</sub>, tea, q<sub>1</sub>),

(q<sub>5</sub>, cof, q<sub>1</sub>)

# Fully Specified FSM



condition		effect	
current state	input	output	next state
q <sub>1</sub>	coin	-	q <sub>2</sub>
q <sub>2</sub>	coin	-	q <sub>3</sub>
q <sub>3</sub>	cof-but	cof	q <sub>1</sub>
q <sub>3</sub>	tea-but	tea	q <sub>1</sub>
q <sub>1</sub>	cof-but	-	q <sub>1</sub>
q <sub>1</sub>	tea-but	-	q <sub>1</sub>
q <sub>2</sub>	cof-but	-	q <sub>2</sub>
q <sub>2</sub>	tea-but	-	q <sub>2</sub>
q <sub>3</sub>	coin	coin	q <sub>3</sub>

# FSM as program 1

```
enum currentState {q1,q2,q3};
enum input {coin, cof_but,tea_but};
int nextStateTable[noStates][noInputs] = {
    q2,q1,q1,
    q3,q2,q2,
    q3,q1,q1 };

int outputTable[noStates][noInputs] = {
    0,0,0,
    0,0,0,
    coin,cof,tea};

While (Input=waitForInput ()) {
    OUTPUT (outputTable[currentState,input])
    currentState=nextStateTable[currentState,input];
}
```

# FSM as program 2

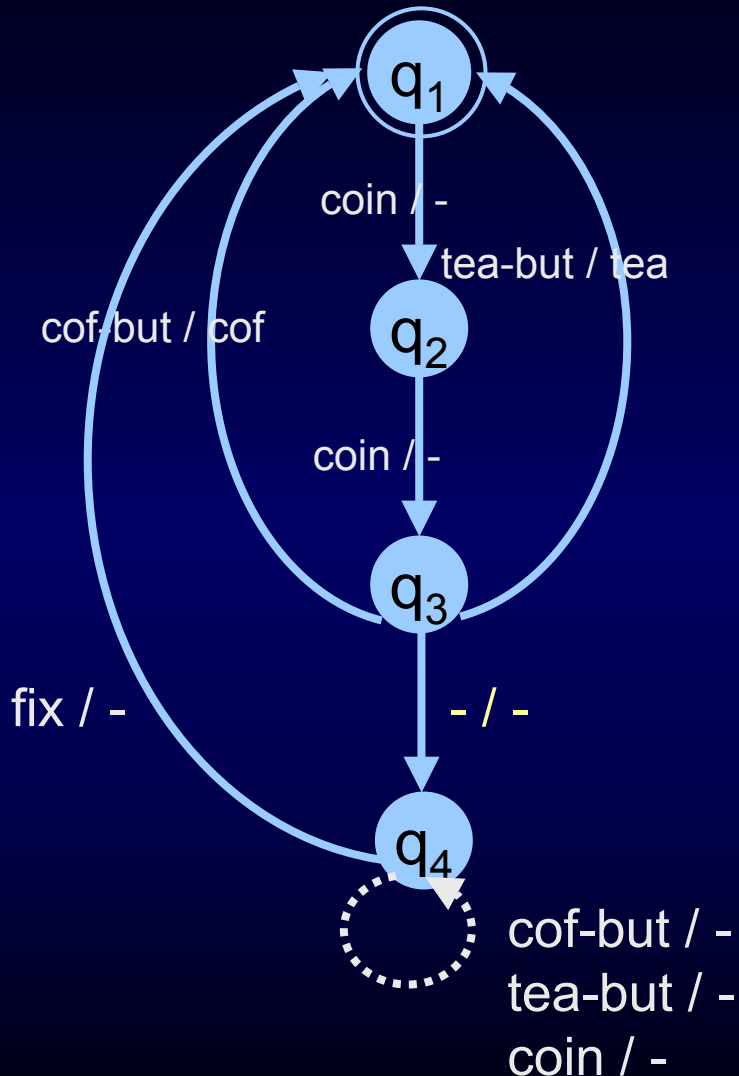
```
enum currentState {q1,q2,q3};
enum input {coin,cof,tea_but,cof_but};

While(input=waitForInput) {
  Switch(currentState) {
  case q1: {
    switch (input) {
      case coin: currentState=q2; break;
      case cof_but:
      case tea_but: break;
      default: ERROR("Unexpected Input");
    }
    break;
  case q3: {
    switch(input) {
      case cof_buf: {currentState=q3;
                    OUTPUT(cof);
                    break;}
    }
  }
  }
}
```

...



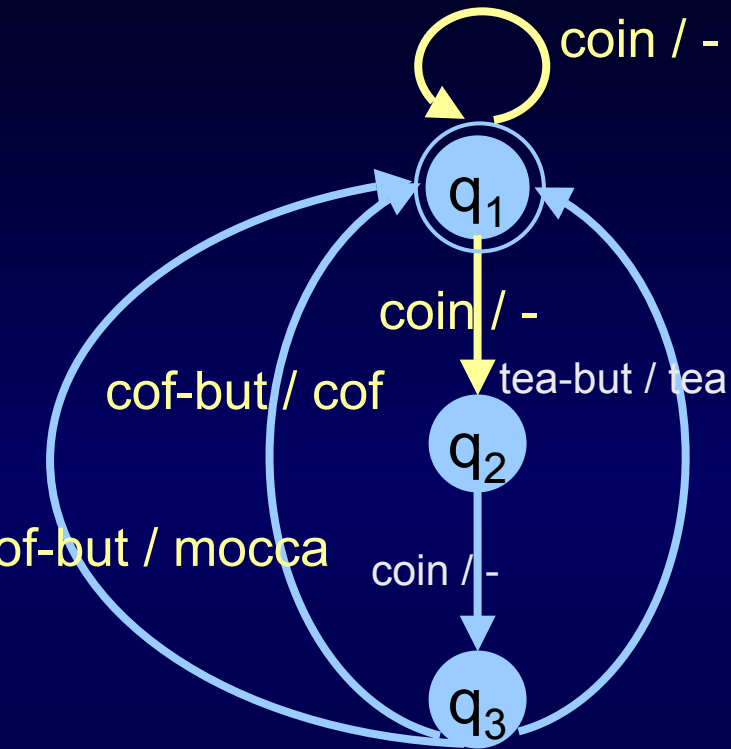
# Spontaneous Transitions



condition		effect	
current state	input	output	next state
$q_1$	coin	-	$q_2$
$q_2$	coin	-	$q_3$
$q_3$	cof-but	cof	$q_1$
$q_3$	tea-but	tea	$q_1$
$q_3$	-	-	$q_4$
$q_4$	fix	-	$q_1$

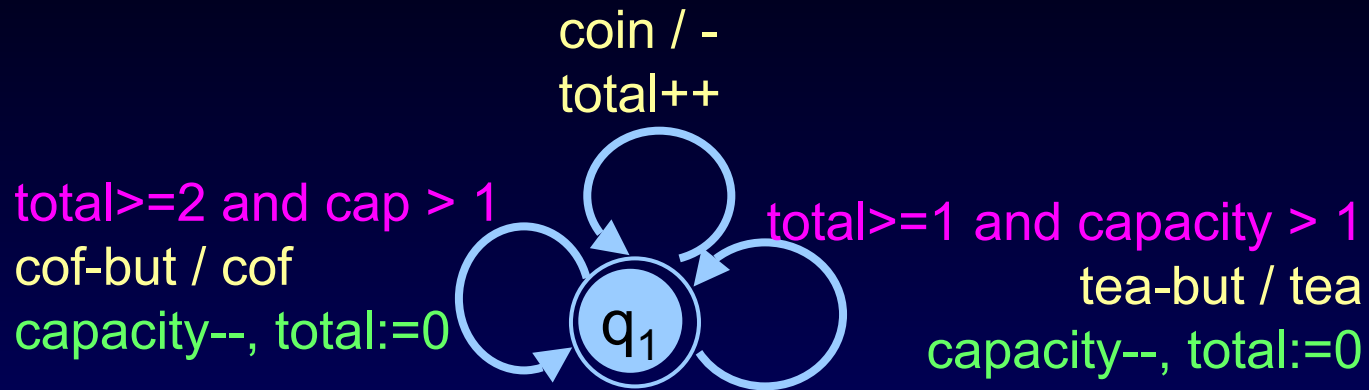
alias **internal** transitions alias **unobservable** transitions

# Non-deterministic FSM

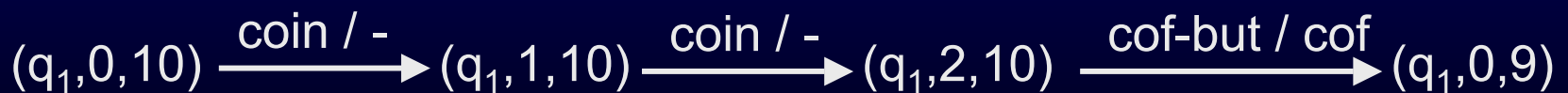


condition		effect	
current state	input	output	next state
$q_1$	coin	-	$q_2$
$q_1$	coin	-	$q_1$
$q_2$	coin	-	$q_3$
$q_3$	tea-but	tea	$q_1$
$q_3$	cof-but	cof	$q_1$
$q_3$	cof-but	mocca	$q_1$

# Extended FSM



- EFSM = FSMs + variables + enabling conditions + assignments
- Easier way of expressing an FSM
- Can be translated into FSM if variables have bounded domain
- State: control location+variable states:  $(q, \text{total}, \text{capacity})$



# Concepts

- Two states  $s$  and  $t$  are (language) **equivalent** iff
  - $s$  and  $t$  accepts same language
  - has same traces:  $tr(s) = tr(t)$
- Two Machines  $M_0$  and  $M_1$  are equivalent iff initial states are equivalent
- A **minimized** / reduced  $M$  is one that has no equivalent states
  - for no two states  $s, t, s \neq t, s$  equivalent  $t$

# Fundamental Results

- Every FSM may be determinized accepting the same language (potential explosion in size).
- For each FSM there exist a language-equivalent *minimal* deterministic FSM.
- FSM's are closed under  $\cap$  and  $\cup$
- FSM's may be described as regular expressions (and vice versa)

# Conformance Testing



Given a specification FSM  $M_S$

an (unknown, black box) implementation FSM  $M_I$ ,

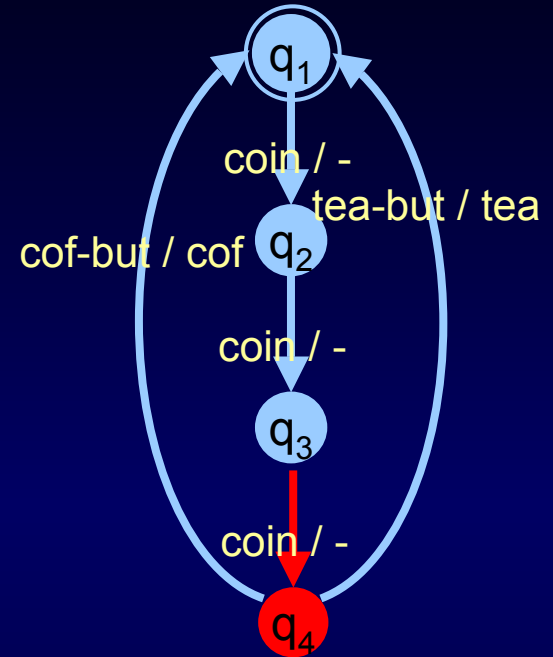
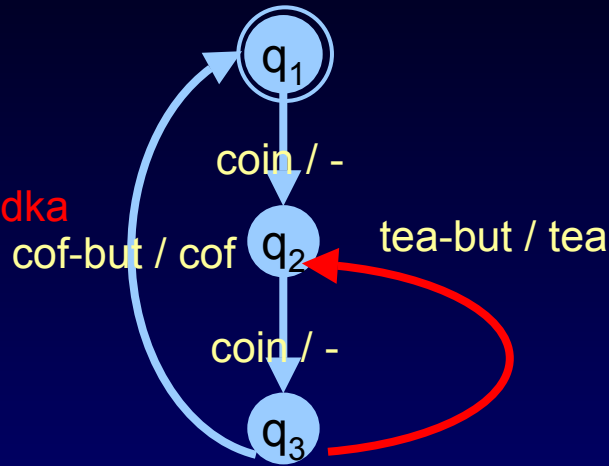
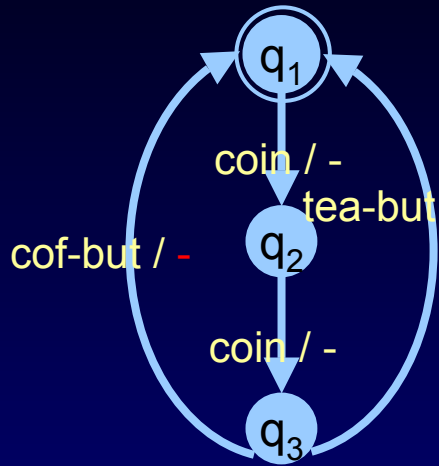
determine whether  $M_I$  conforms to  $M_S$ .

i.e.,  $M_I$  behaves in accordance with  $M_S$

i.e., whether outputs of  $M_I$  are the same as of  $M_S$

i.e., whether the reduced  $M_I$  is equivalent to  $M_S$

# Possible Errors



- output fault
- extra or missing states
- transition fault
  - to other state
  - to new state

# State Machine : FSM Model



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FSM - Finite State Machine - or *Mealy Machine* is 5-tuple

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$$M = (S, I, O, \delta, \lambda)$$

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S

finite set of states

# State Machine : FSM Model

FSM - Finite State Machine - or *Mealy Machine* is 5-tuple

$$M = (S, I, O, \delta, \lambda)$$

S                      finite set of states

I                      finite set of inputs

# State Machine : FSM Model

FSM - Finite State Machine - or *Mealy Machine* is 5-tuple

$$M = (S, I, O, \delta, \lambda)$$

S	finite set of states
I	finite set of inputs
O	finite set of outputs

# State Machine : FSM Model

FSM - Finite State Machine - or *Mealy Machine* is 5-tuple

$$M = (S, I, O, \delta, \lambda)$$

S	finite set of states
I	finite set of inputs
O	finite set of outputs
$\delta : S \times I \rightarrow S$	transfer function

# State Machine : FSM Model

FSM - Finite State Machine - or *Mealy Machine* is 5-tuple

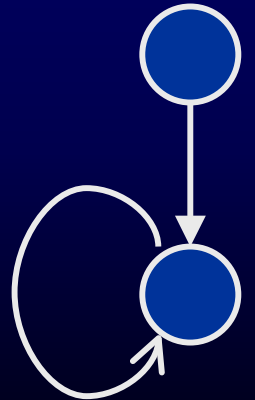
$$M = (S, I, O, \delta, \lambda)$$

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I	finite set of inputs
O	finite set of outputs
$\delta : S \times I \rightarrow S$	transfer function
$\lambda : S \times I \rightarrow O$	output function



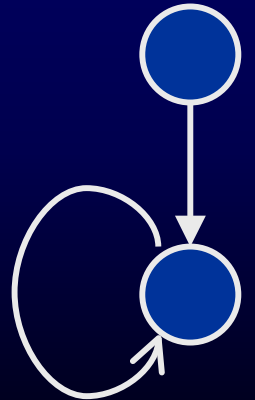


# Restrictions



# Restrictions

FSM restrictions:

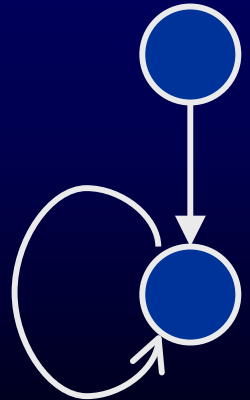


# Restrictions

FSM restrictions:

- *deterministic*

$\delta : S \times I \rightarrow S$  and  $\lambda : S \times I \rightarrow O$  are *functions*



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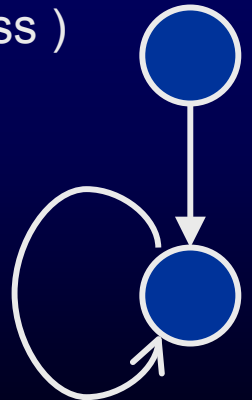
- *deterministic*

$\delta : S \times I \rightarrow S$  and  $\lambda : S \times I \rightarrow O$  are *functions*

- *completely specified*

$\delta : S \times I \rightarrow S$  and  $\lambda : S \times I \rightarrow O$  are *complete* functions

( empty output is allowed; sometimes implicit completeness )



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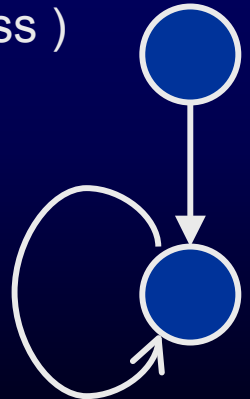
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- *strongly connected*

from any state any other state can be reached



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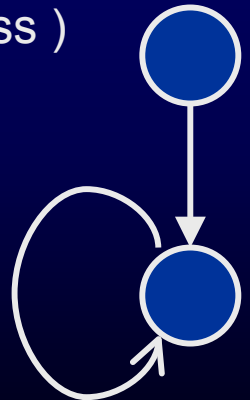
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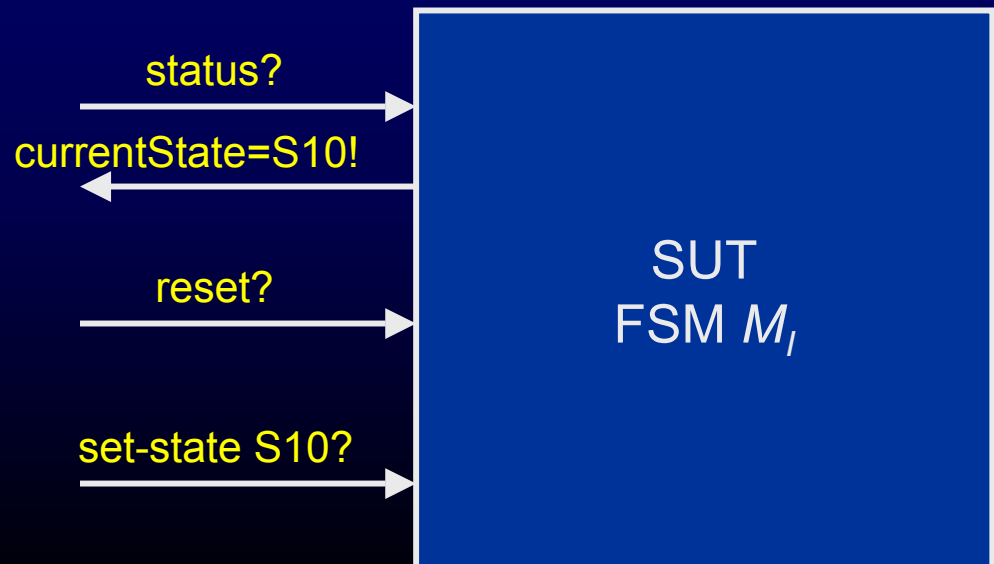
- *reduced*

there are no equivalent states



# Desired Properties

- Nice, but rare / problematic
  - **status messages**: Assume that tester can ask implementation for its current state (reliably!!) without changing state
  - **reset**: reliably bring SUT to initial state
  - **set-state**: reliably bring SUT to any given state



# FSM Transition Testing

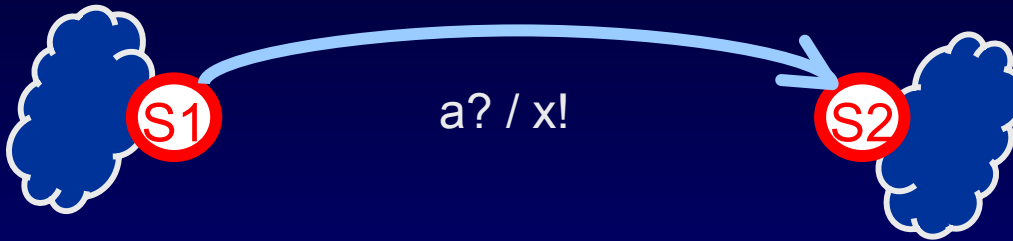


# FSM Transition Testing

- Make a test case for every transition in spec separately:

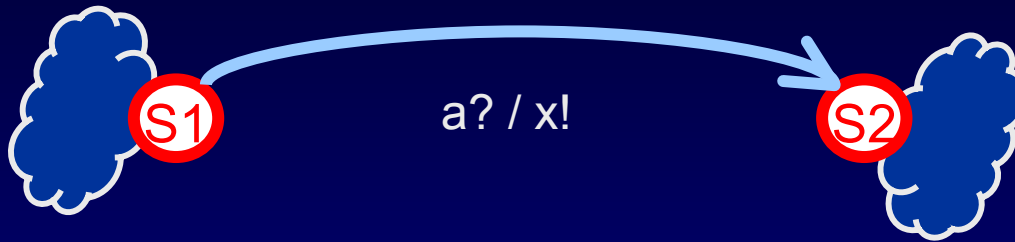
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# FSM Transition Testing

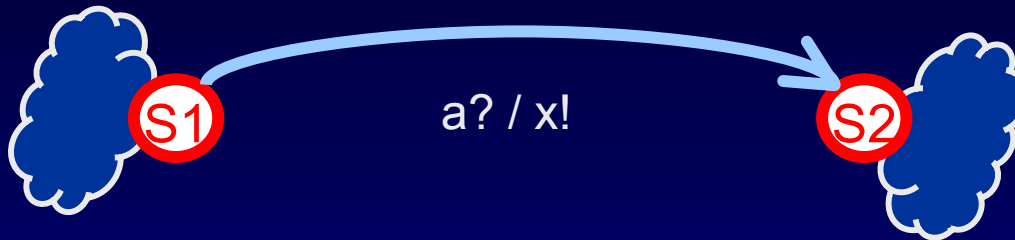
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- Test transition :
  1. Go to state S1
  2. Apply input a?
  3. Check output x!
  4. Verify state S2 ( optionally )

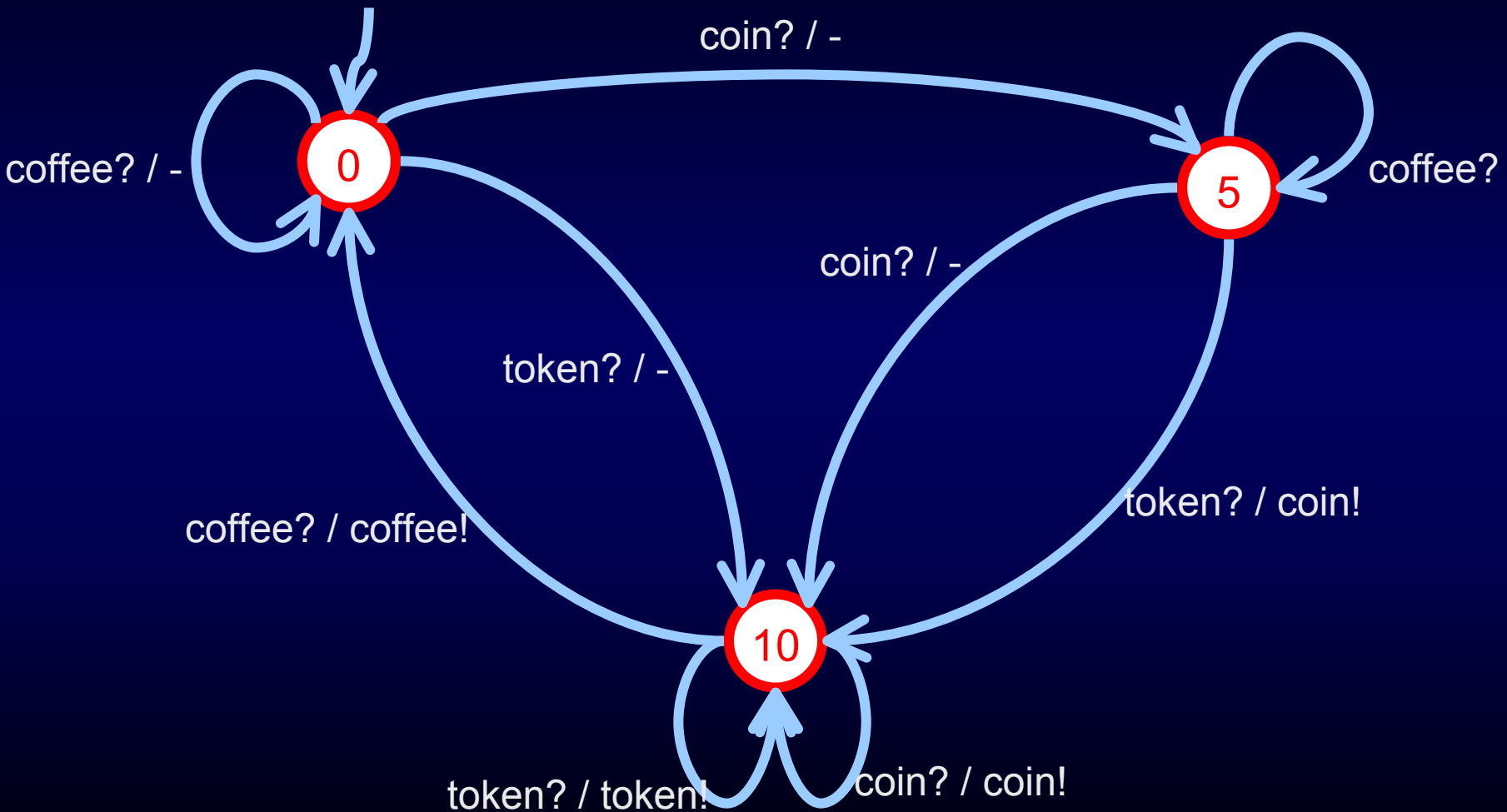
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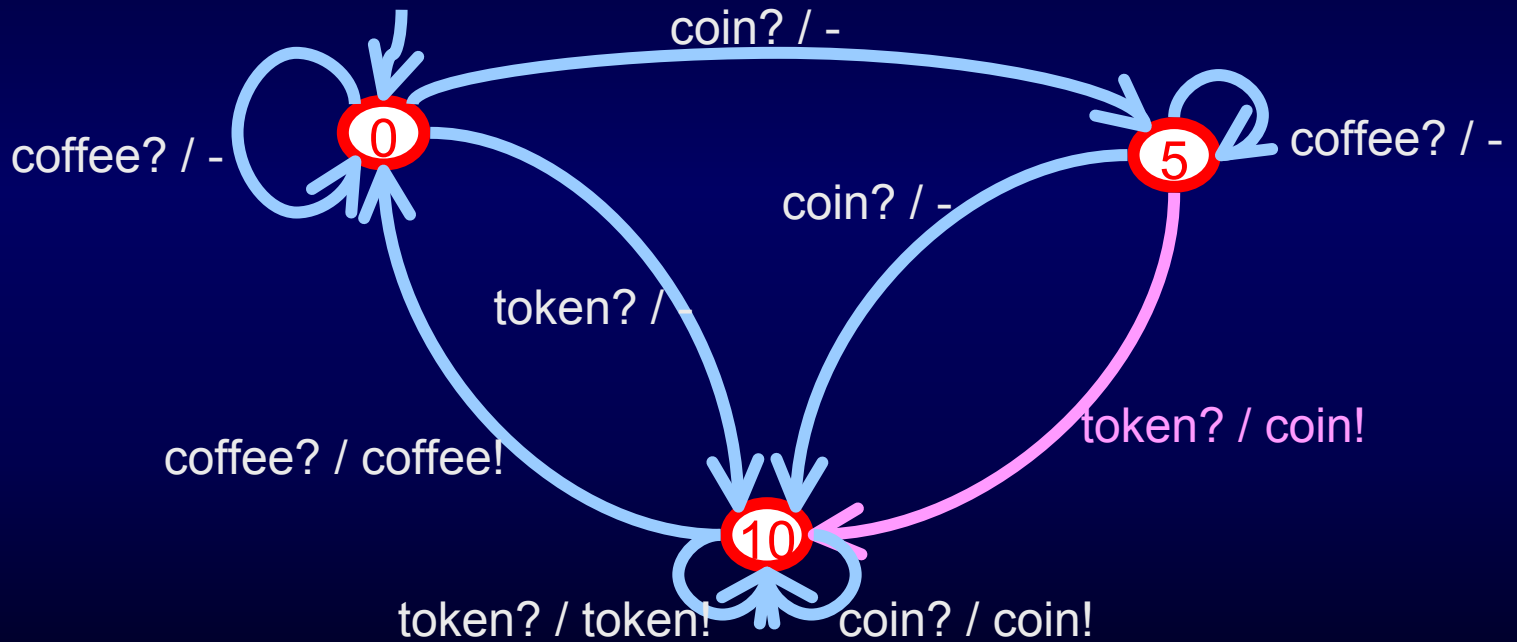
- Test transition :
  1. Go to state S1
  2. Apply input a?
  3. Check output x!
  4. Verify state S2 ( optionally )
- *Test purpose: "Test whether the system, when in state S1, produces output x! on input a? and goes to state S2"*

# Coffee Machine FSM Model



# Transition Testing –1

# Transition Testing –1



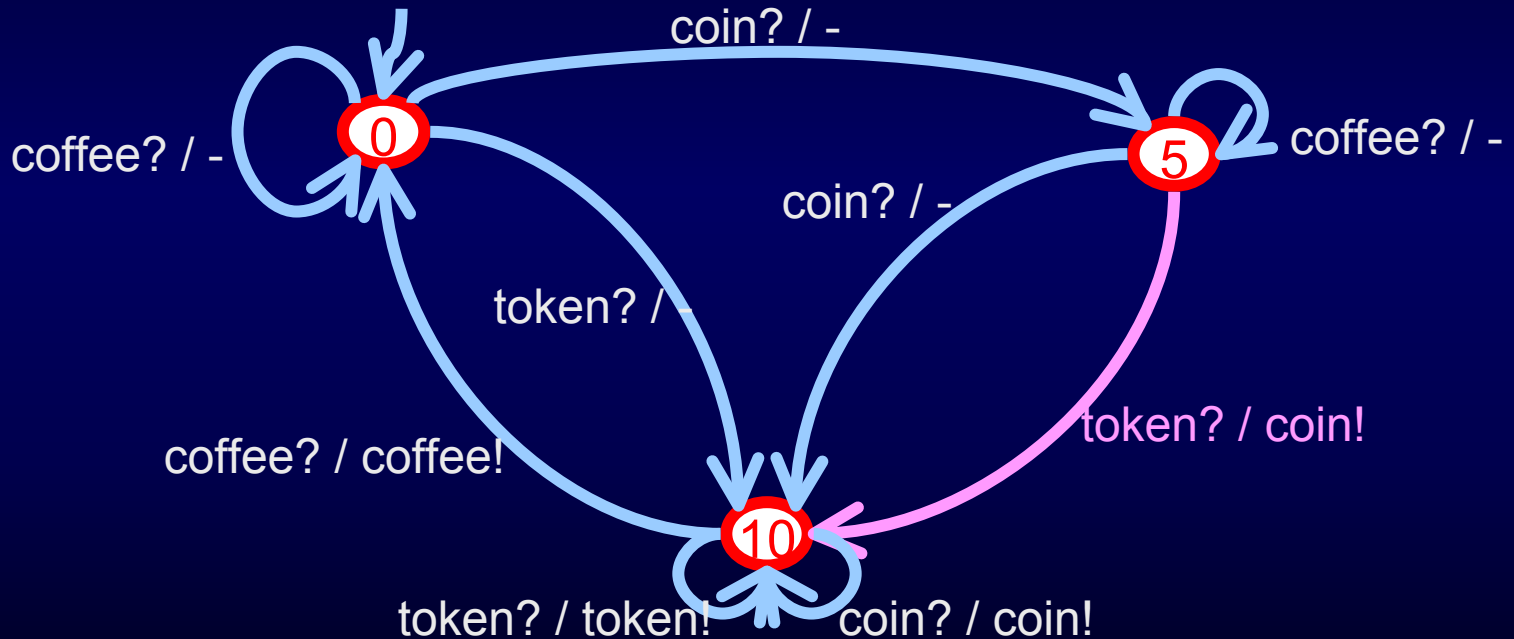
# Transition Testing –1

- To test `token? / coin!` :

go to state `5` : `reset . set-state 5`

give input `token?` check output `coin!`

verify state: `send status?` check `status=10`





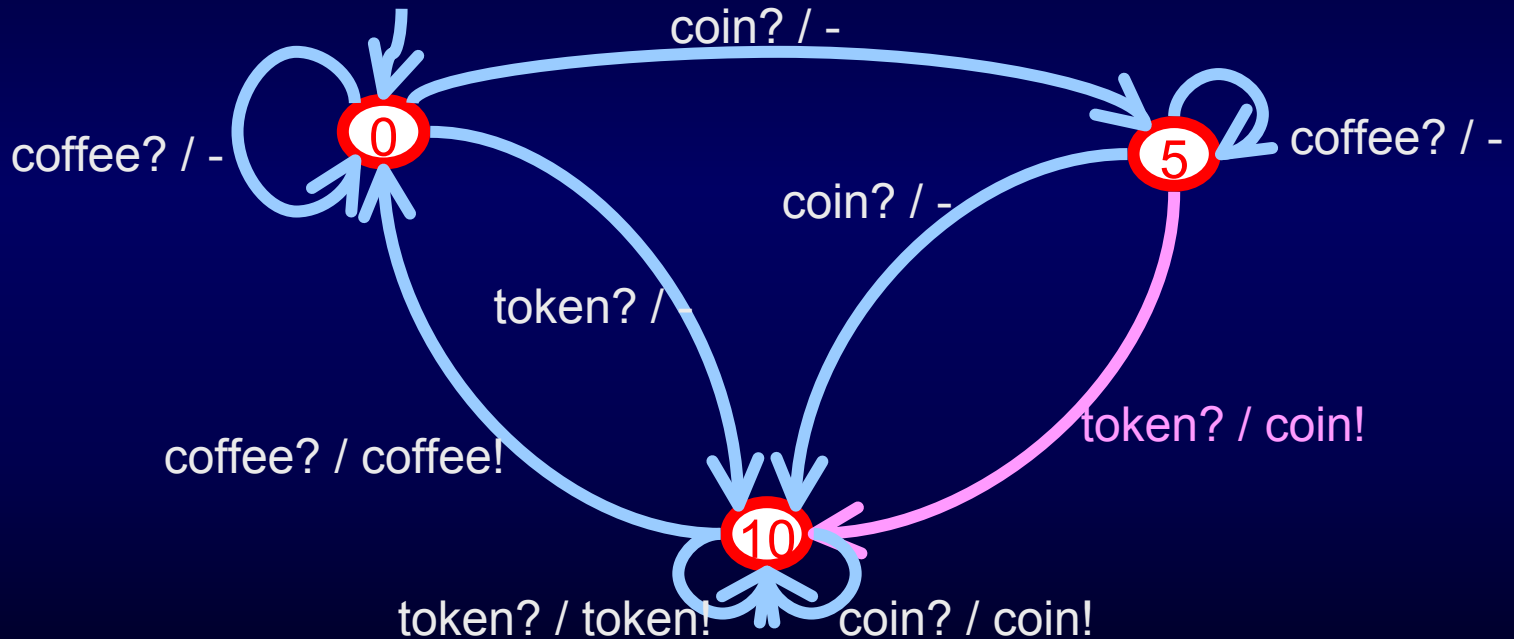
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Test case : `set-state 5/ * - token? / coin! - status? / 10!`

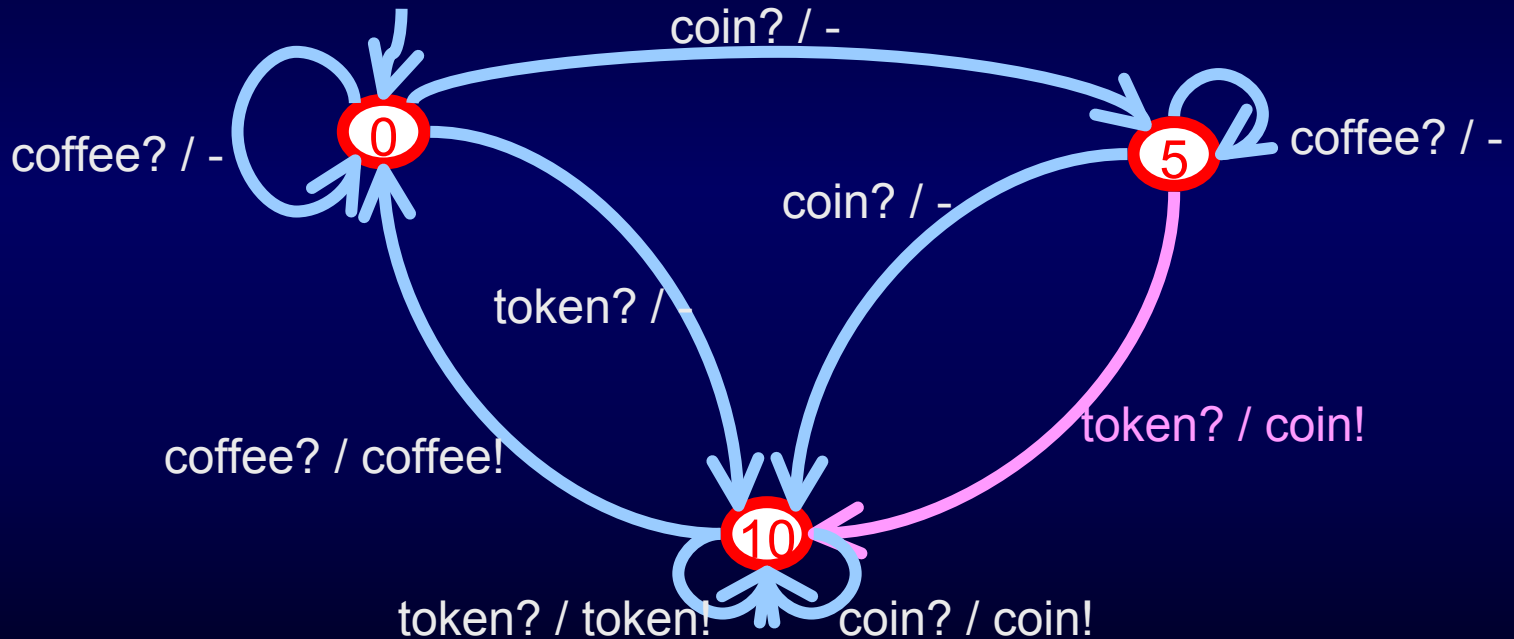
# Transition Testing –1

- To test `token? / coin!` :

go to state `5` : `reset . set-state 5`

give input `token?` check output `coin!`

verify state: `send status? check status=10`



Test case : `set-state 5/ * - token? / coin! - status? / 10!`

a test case per state per input event: total length  $4 * |S| * |I|$

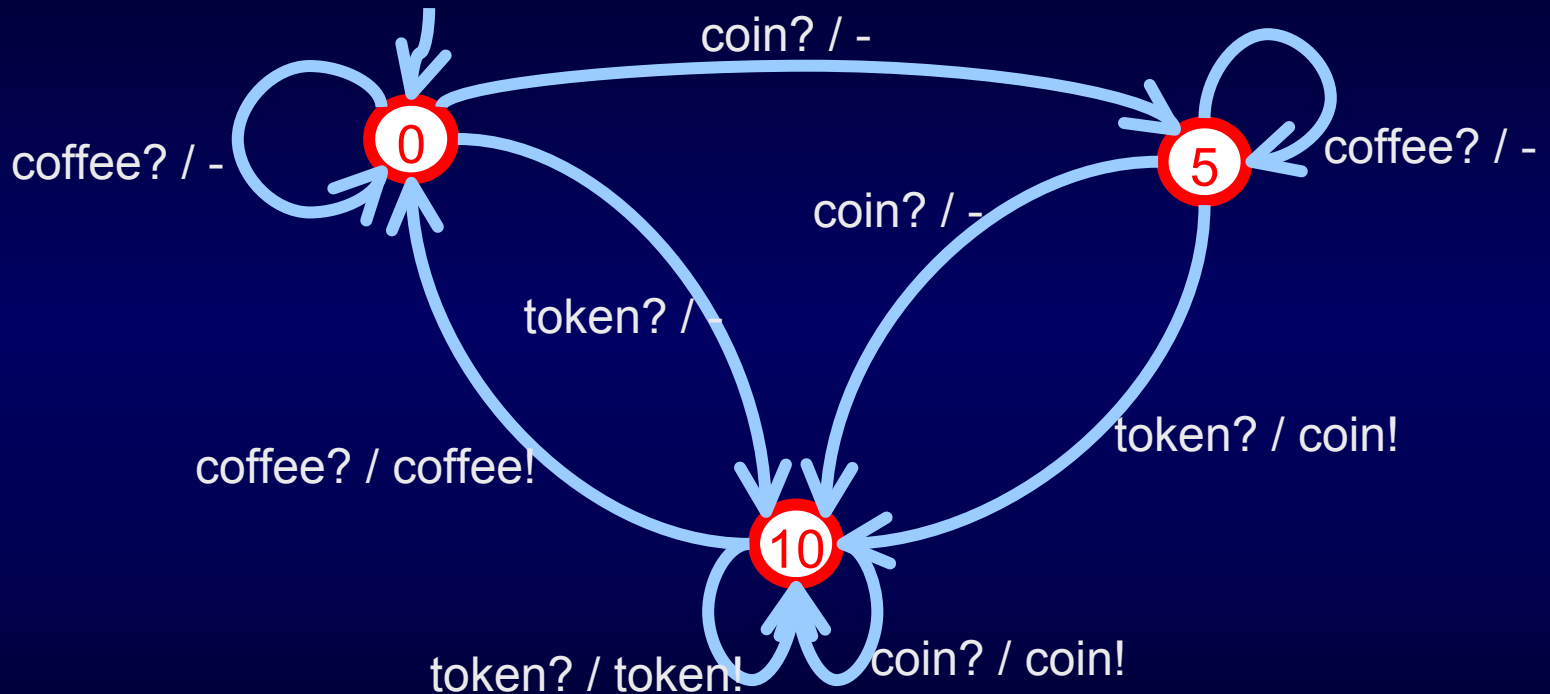
# FSM Transition Tour

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- Make Transition Tour that covers every transition (in spec)

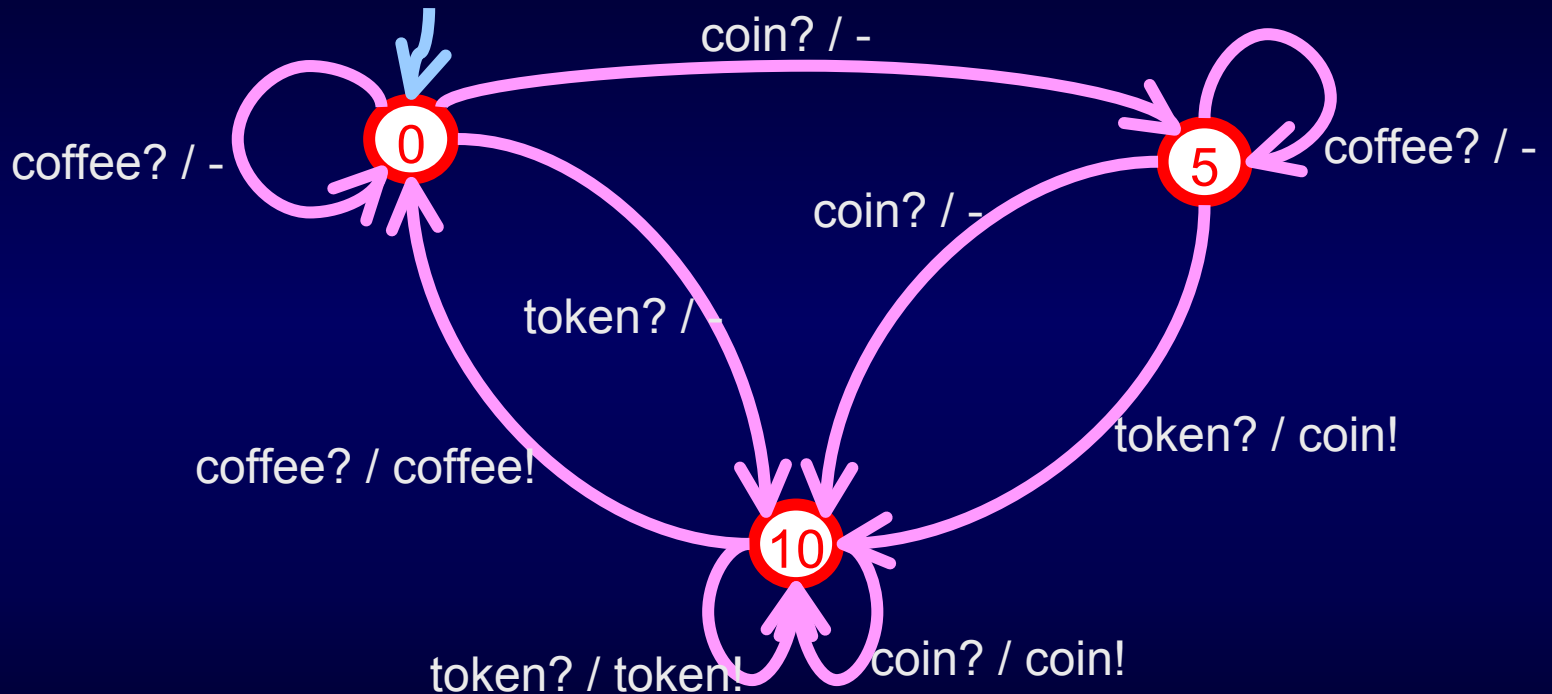
# FSM Transition Tour

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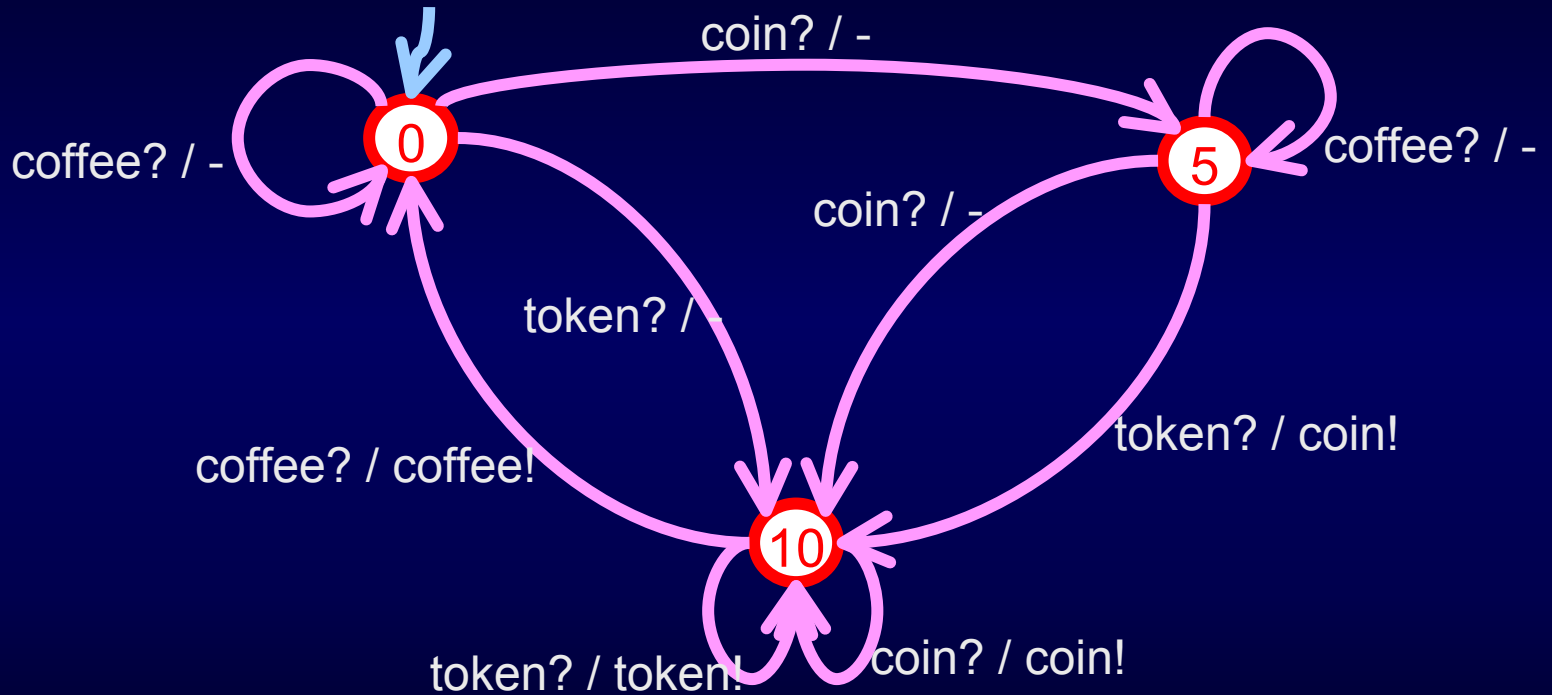
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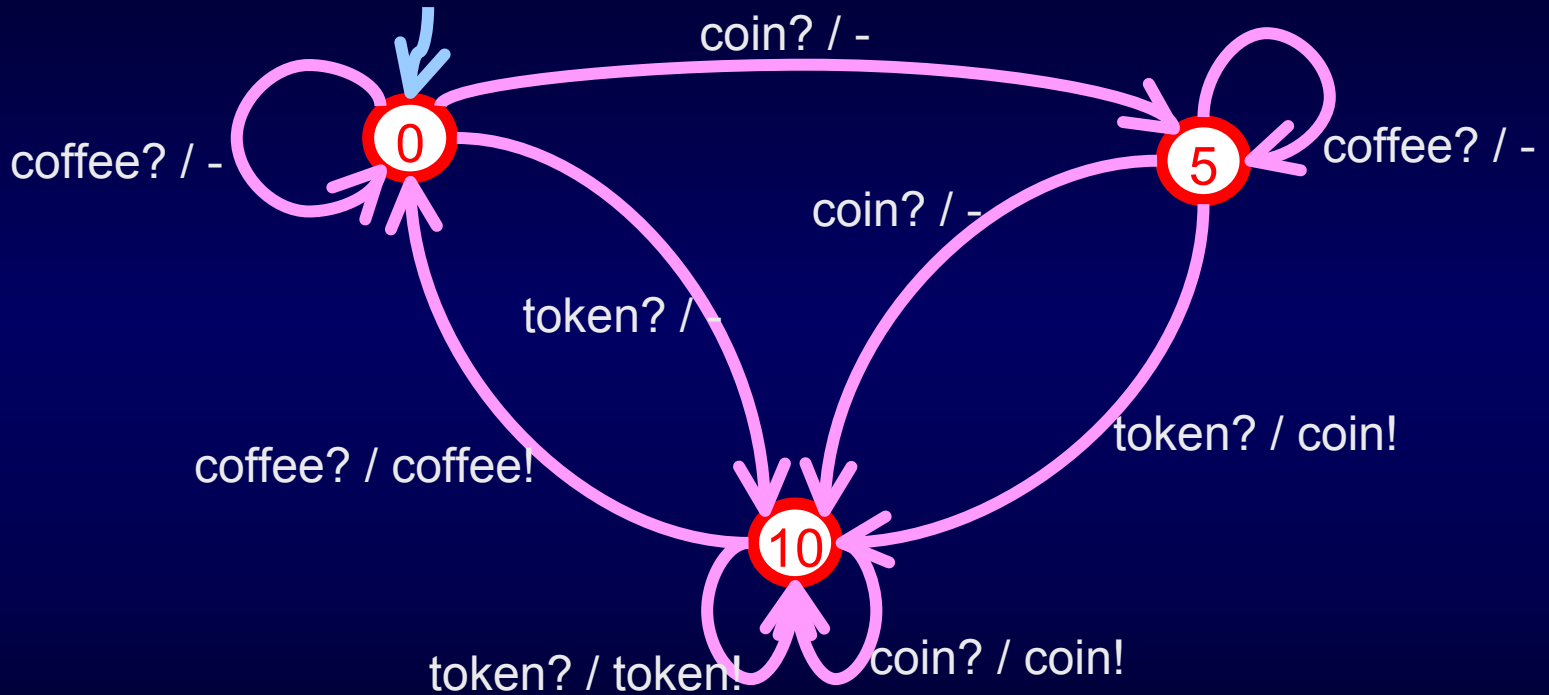


Test input sequence :

reset? coffee? coin? coffee? coin? coin? token? coffee? token? coffee? coin? token? coff

# FSM Transition Tour

- Make Transition Tour that covers every transition (in spec)



Test input sequence :

reset? coffee? coin? coffee? coin? coin? token? coffee? token? coffee? coin? token? coff



+ check expected outputs and target state by status message



# Transition Testing -1

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- Go to state S5 :

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- Go to state S5 :
- No Set-state property???

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- Go to state S5 :
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  - use *reset property* if available

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  - go from S0 to S5  
( always possible because of determinism and completeness )

# Transition Testing -1

- Go to state S5 :
- **No Set-state property???**
  - use *reset property* if available
  - go from S0 to S5  
( always possible because of determinism and completeness )
  - or:

# Transition Testing -1

- Go to state S5 :
- **No Set-state property???**
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( always possible because of determinism and completeness )
  - or:
  - ***synchronizing sequence*** brings machine to particular known state, say S0, from any state

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- Go to state S5 :
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  - ( but synchronizing sequence may not exist )



# Transition Testing -1

- Go to state  $S_5$  :
- **No Set-state property???**
  - use *reset property* if available
  - go from  $S_0$  to  $S_5$   
( always possible because of determinism and completeness )
  - or:
  - ***synchronizing sequence*** brings machine to particular known state, say  $S_0$ , from any state
  - ( but synchronizing sequence may not exist )
  - A preset *homing sequence* is an input sequence  $x$  whose output on  $x$  (applied in any state) uniquely identifies the reached state after  $x$ !

# Transition Testing -1

token? coffee?

To test token? / coin! : go to state 5 by : token? coffee? coin?

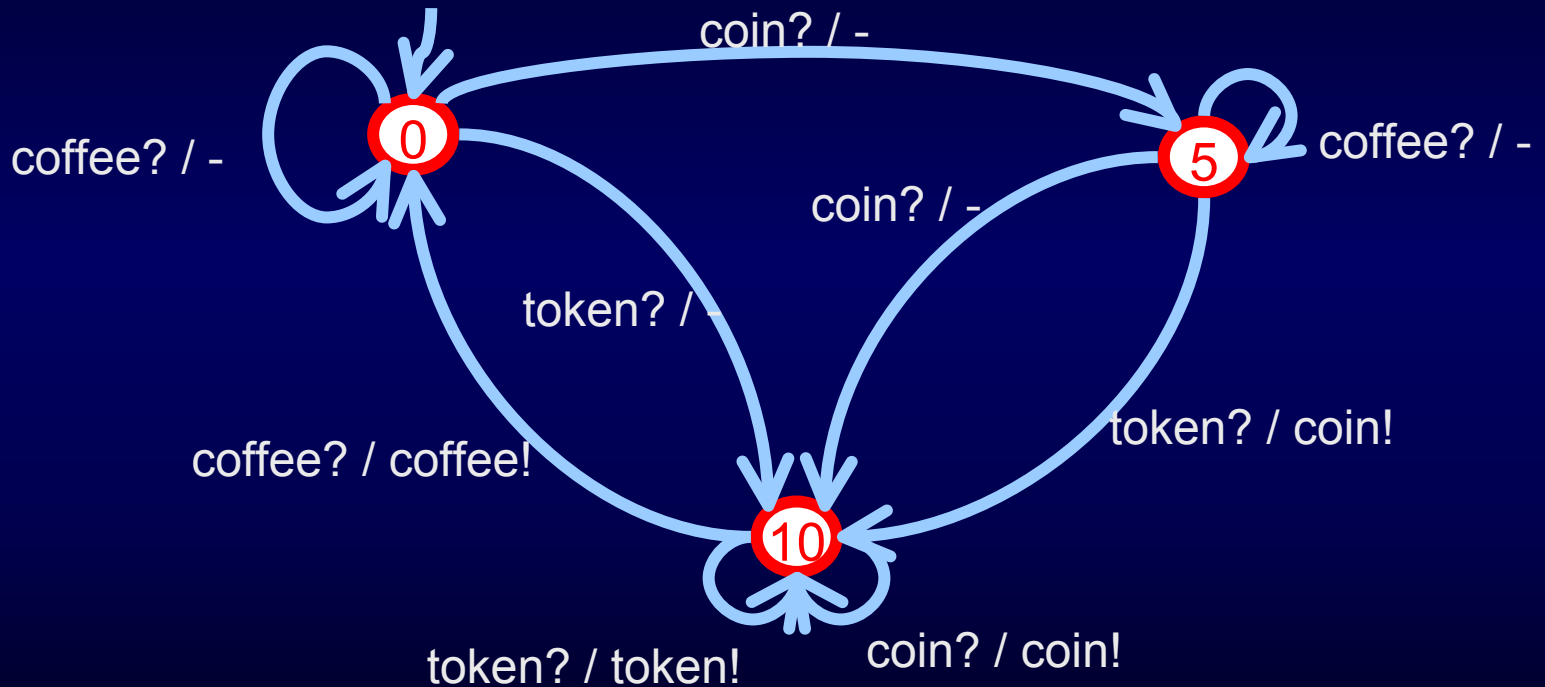
# Transition Testing -1

synchronizing sequence : token? coffee?

To test token? / coin! : go to state 5 by : token? coffee? coin?

# Transition Testing -1

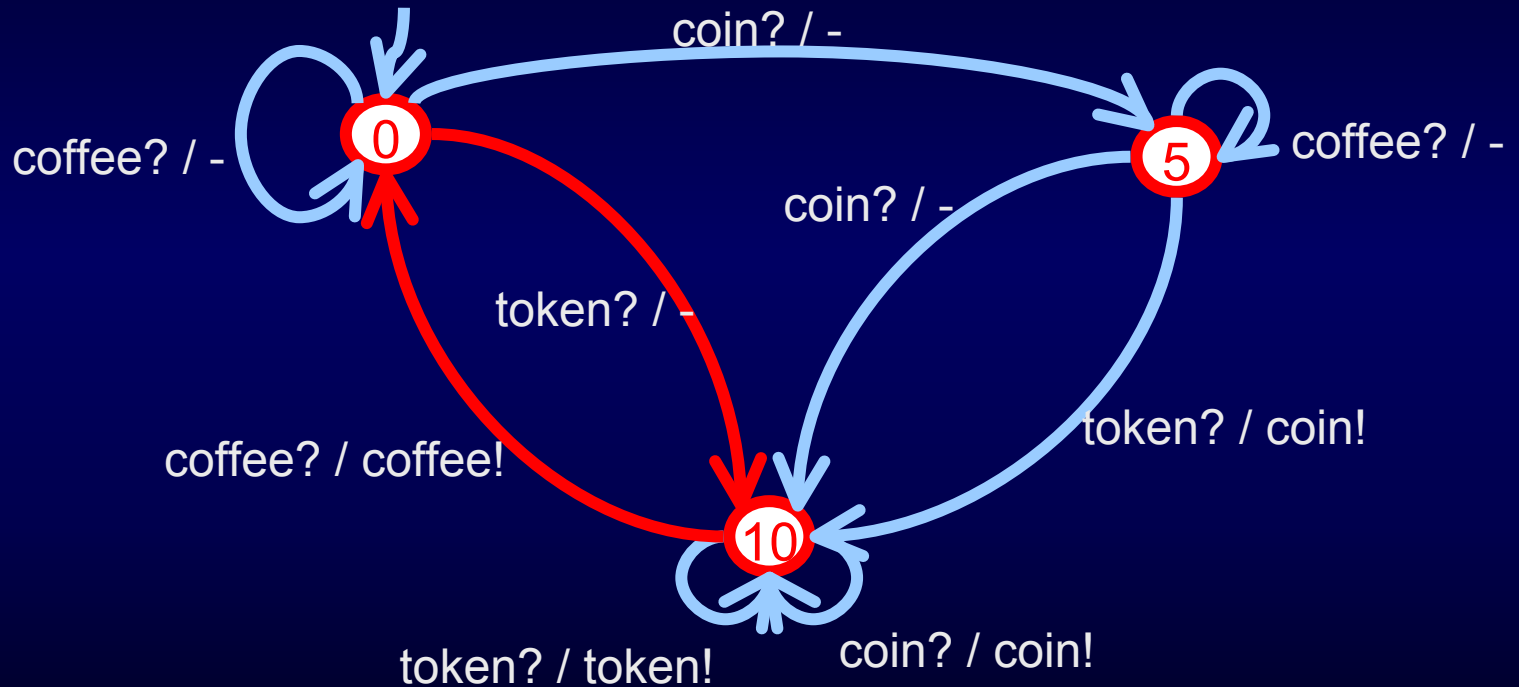
synchronizing sequence : token? coffee?



To test **token? / coin!** : go to state **5** by : token? coffee? coin?

# Transition Testing -1

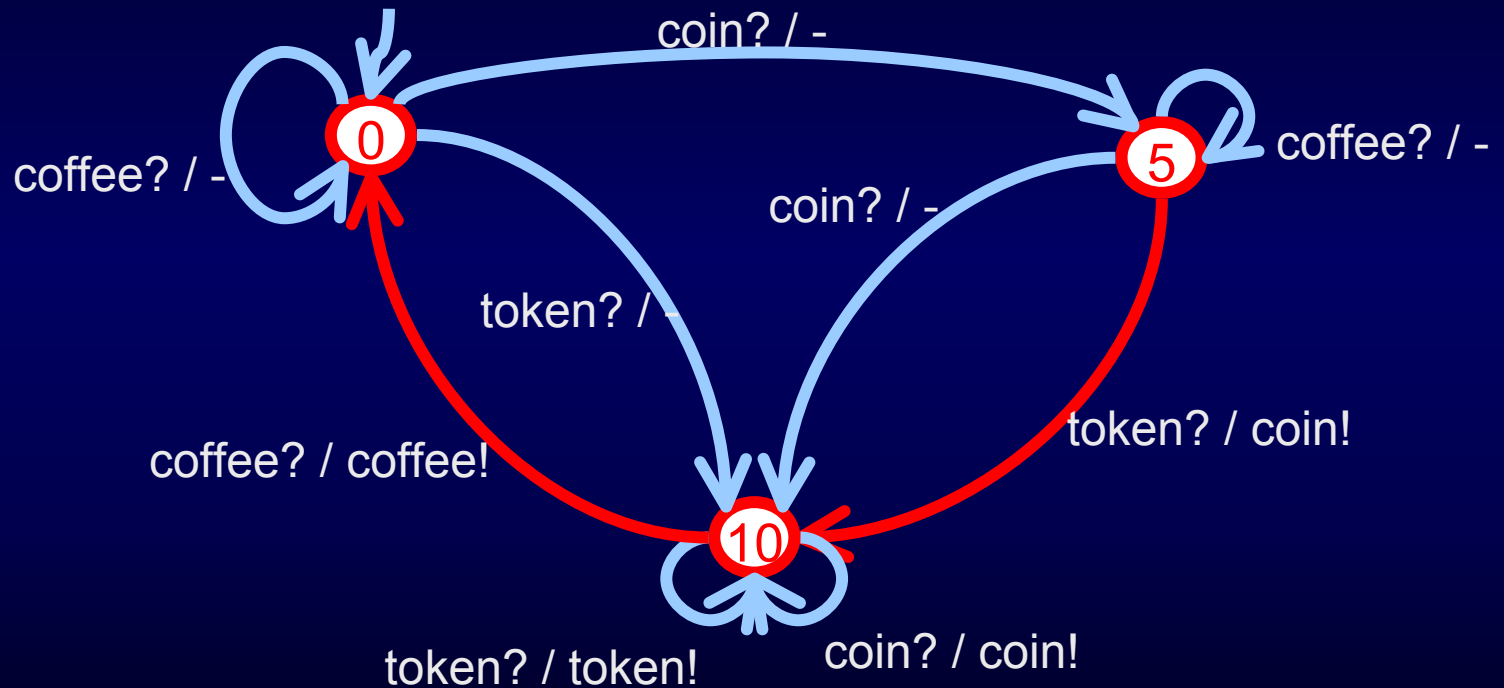
synchronizing sequence : token? coffee?



To test **token? / coin!** : go to state **5** by : token? coffee? coin?

# Transition Testing -1

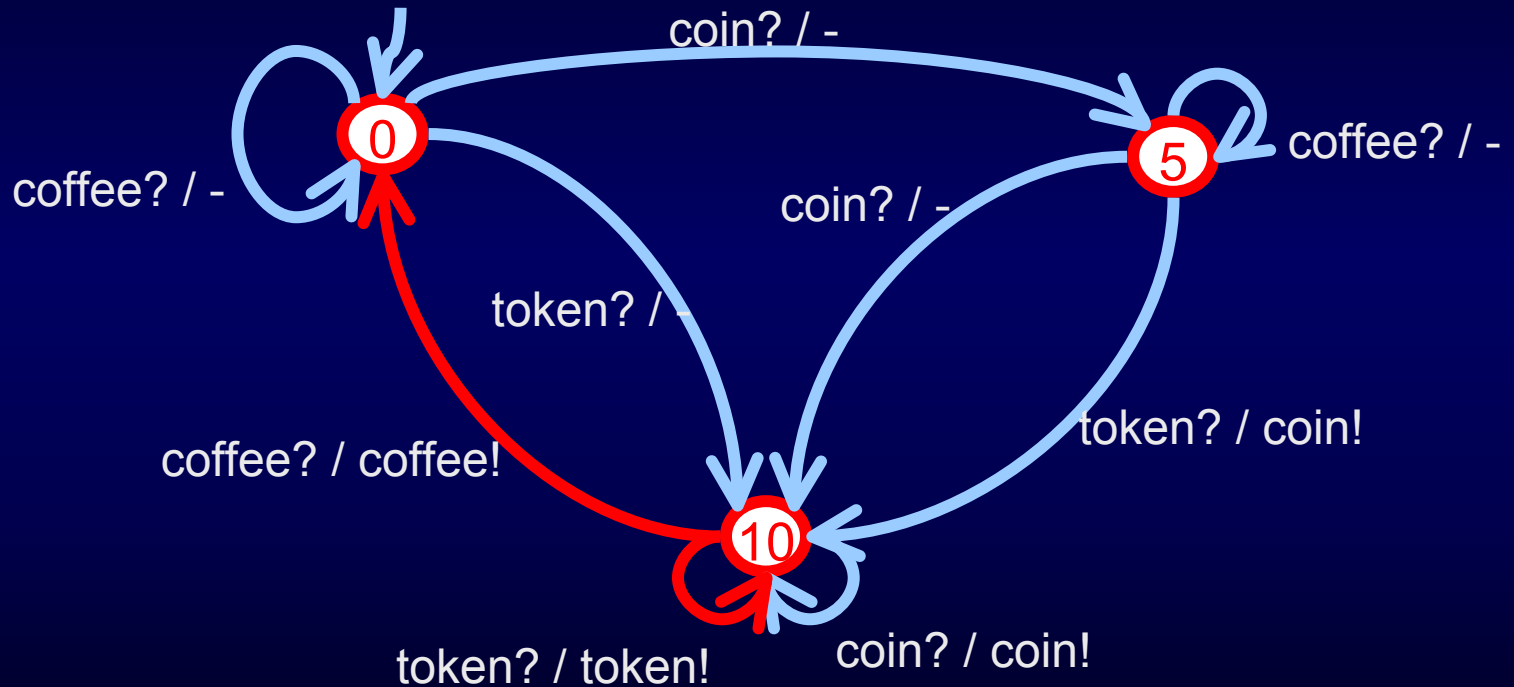
synchronizing sequence : token? coffee?



To test **token? / coin!** : go to state **5** by : token? coffee? coin?

# Transition Testing -1

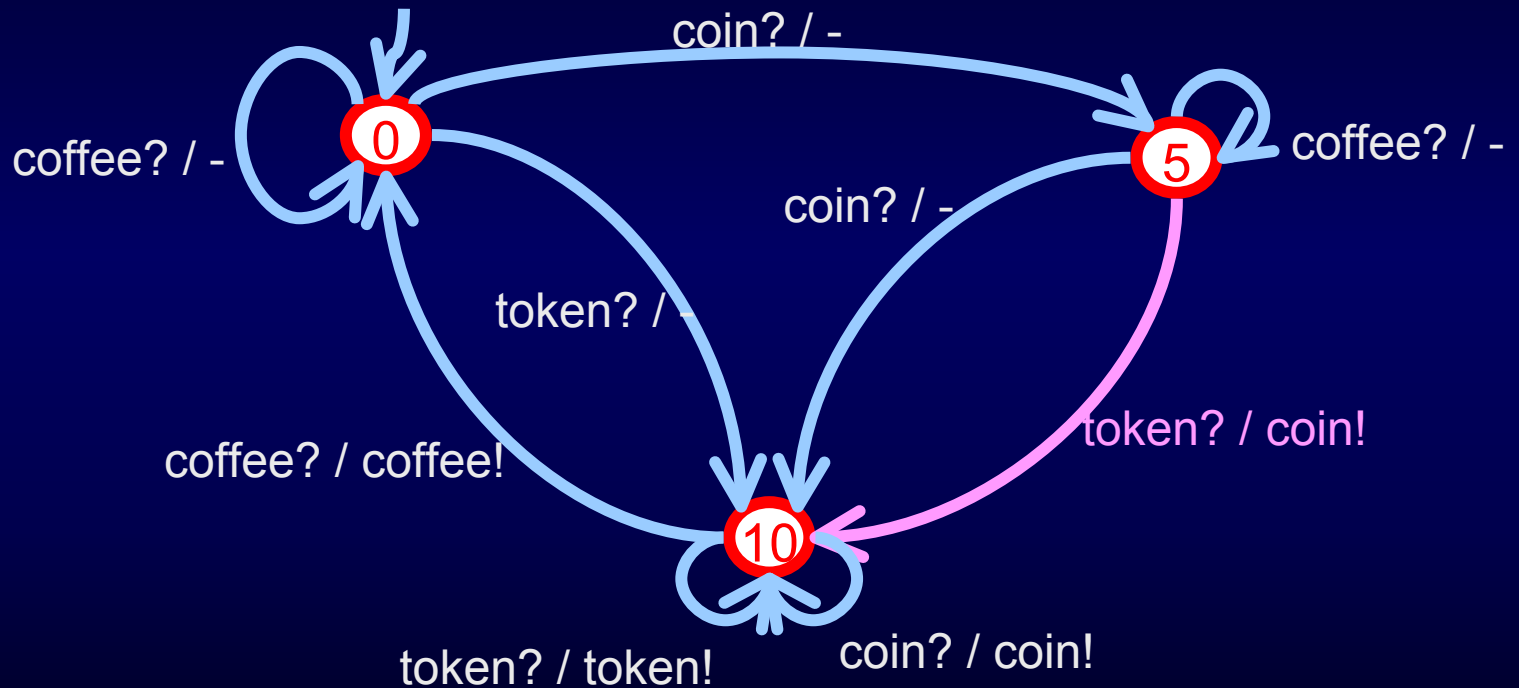
synchronizing sequence : token? coffee?



To test `token? / coin!` : go to state 5 by : token? coffee? coin?

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synchronizing sequence : token? coffee?

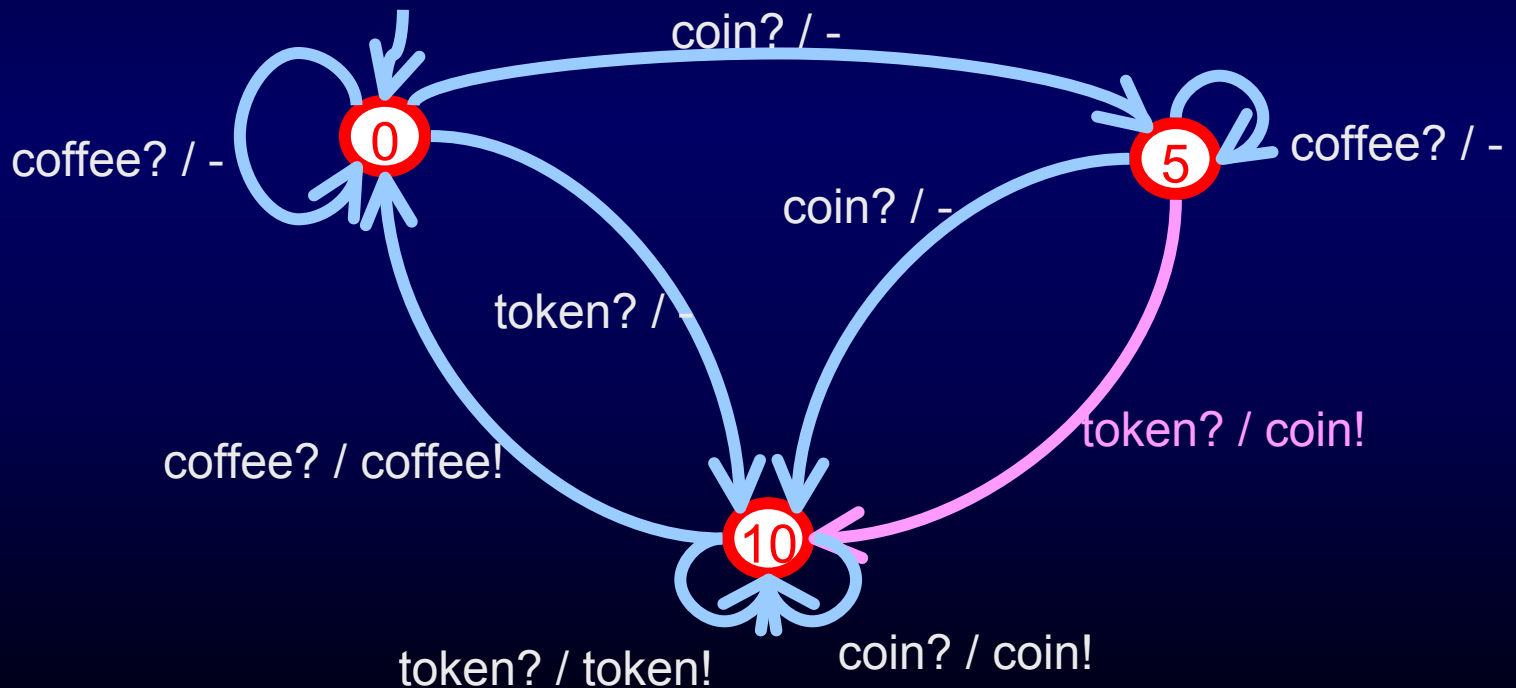


To test **token? / coin!** : go to state **5** by : token? coffee? coin?



# Transition Testing –2,3

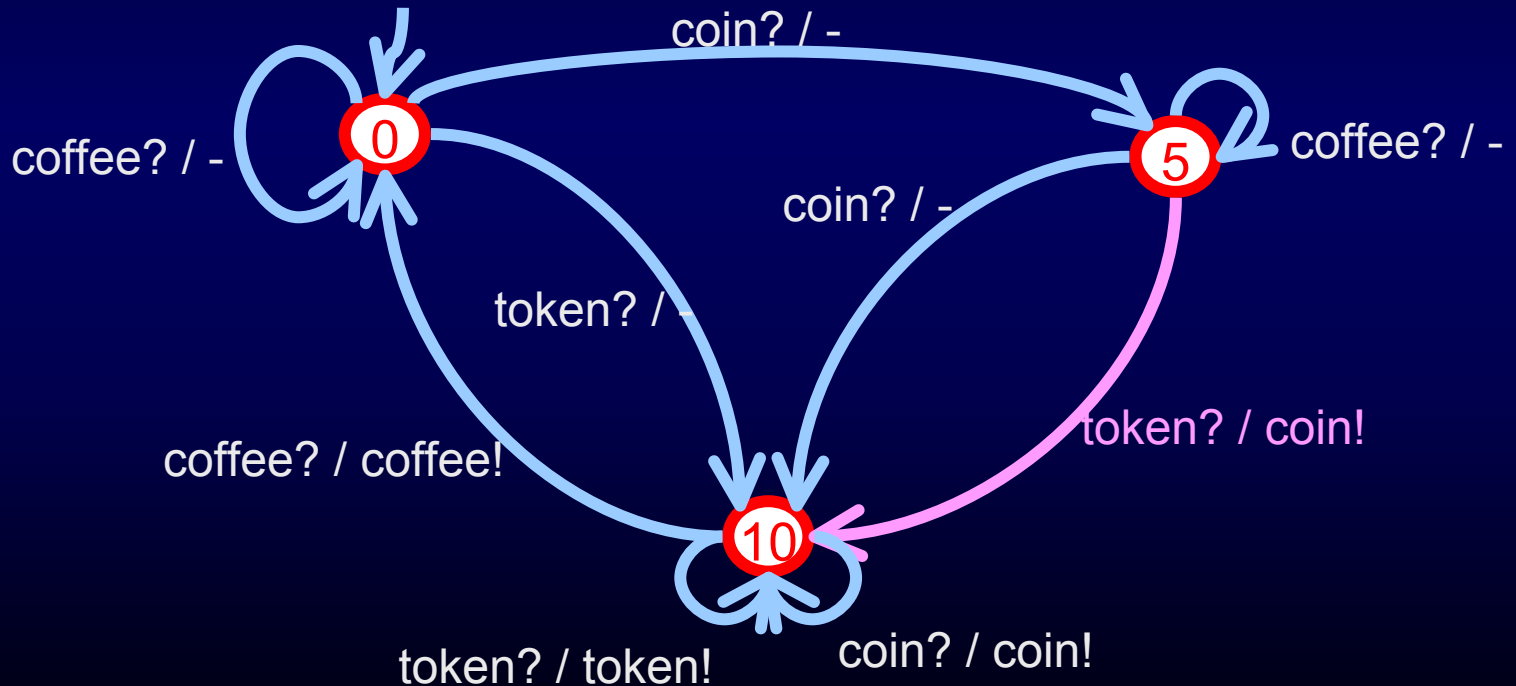
# Transition Testing –2,3



# Transition Testing –2,3

•To test  $\text{token?} / \text{coin!}$  :

1. go to state **5** by :  $\text{token?} \text{ coffee?} \text{ coin?}$
2. give input  $\text{token?}$
3. check output  $\text{coin!}$
4. verify that machine is in state **10**



# Transition Testing-4

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- State identification: What state am I in??

# Transition Testing-4

- No Status Messages??
- State identification: What state am I in??
- State verification : Am I in state s?
  - Apply sequence of inputs in the current state of the FSM such that from the outputs we can
    - identify that state where we started; or
    - verify that we were in a particular start state
  - Different kinds of sequences
    - UIO sequences ( Unique Input Output sequence, SIOS)
    - Distinguishing sequence ( DS )
    - W - set ( characterizing set of sequences )
    - UIOv
    - SUIO
    - MUIO

# Transition Testing-4



# Transition Testing-4

State check :

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  - Length  $O(VS^3)$

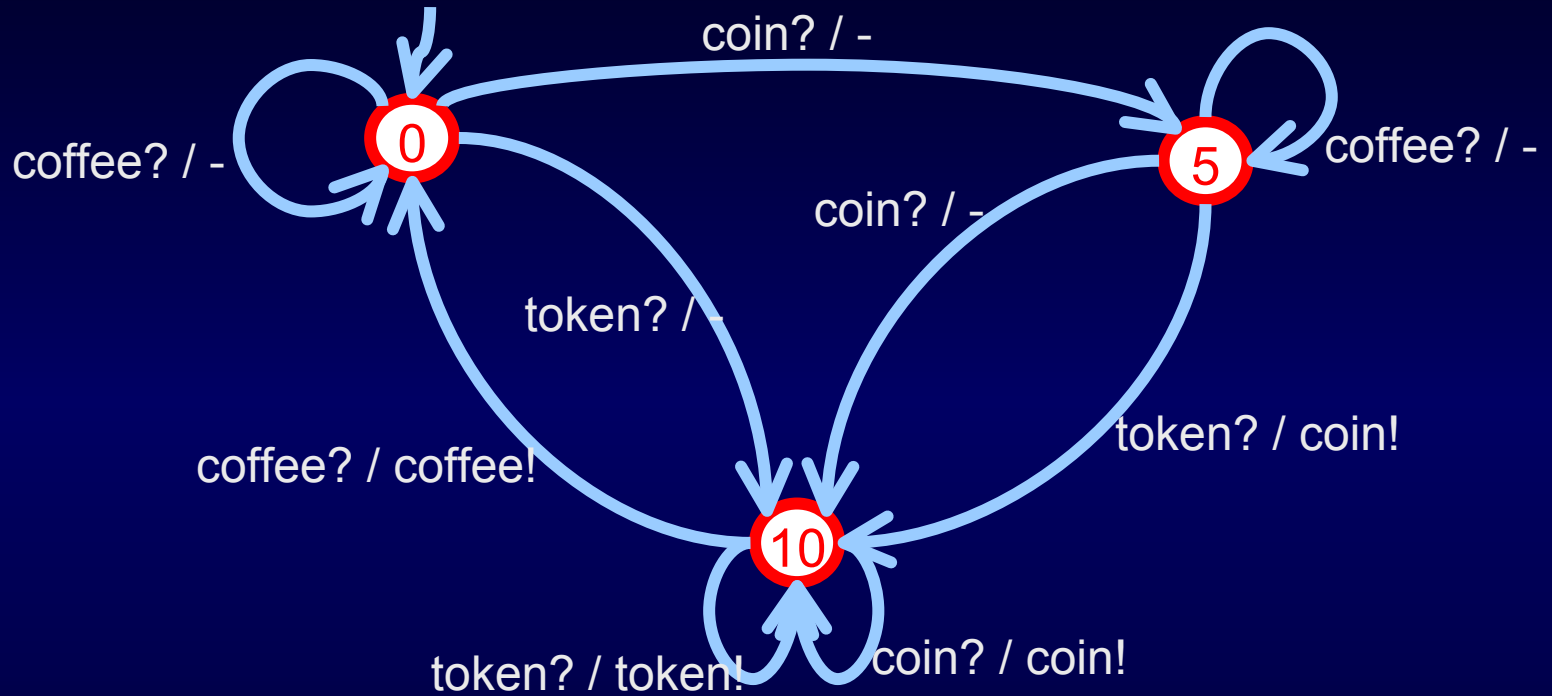
# Transition Testing-4: UIO

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UIO sequences

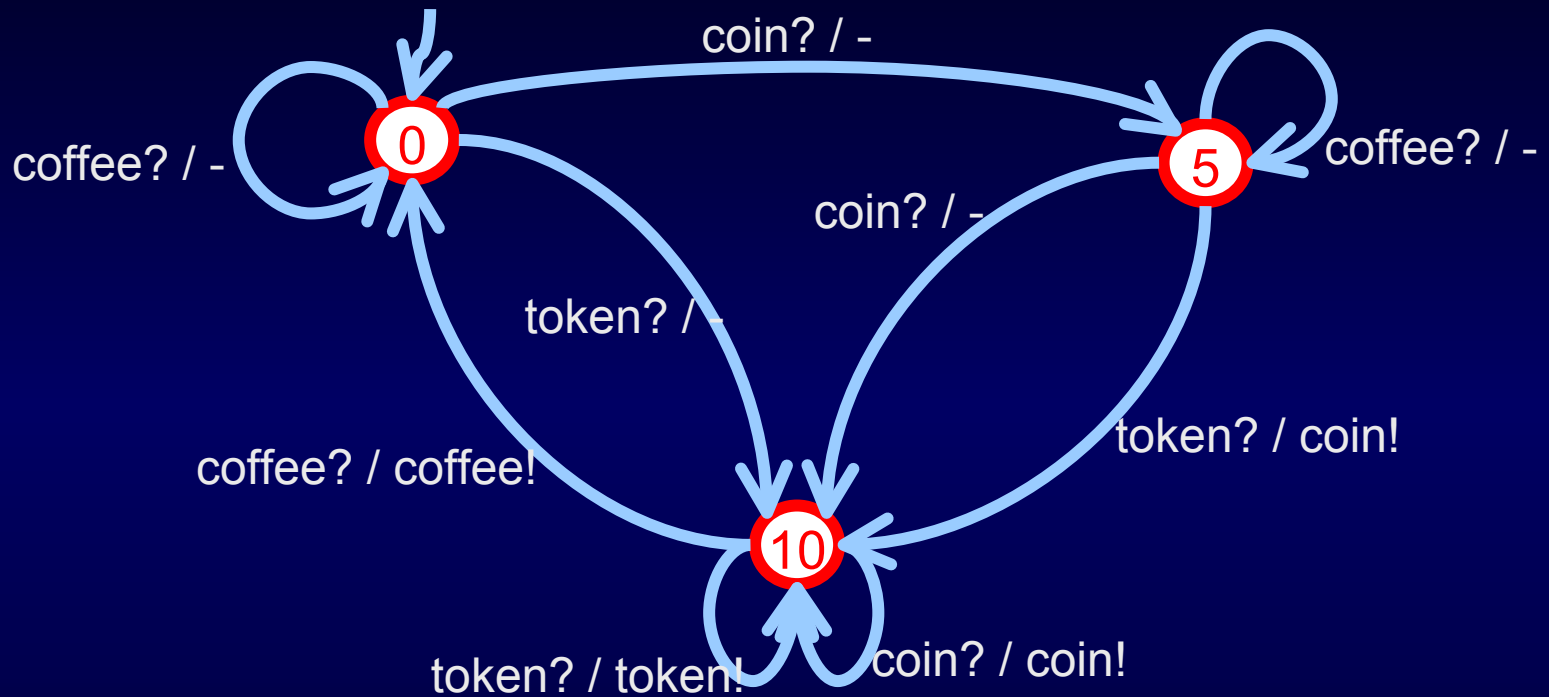
# Transition Testing-4: UIO

## UIO sequences



# Transition Testing-4: UIO

## UIO sequences



state 0 : coin? / - coffee? / -  
state 5 : token? / coin!  
state 10 : coffee? / coffee!



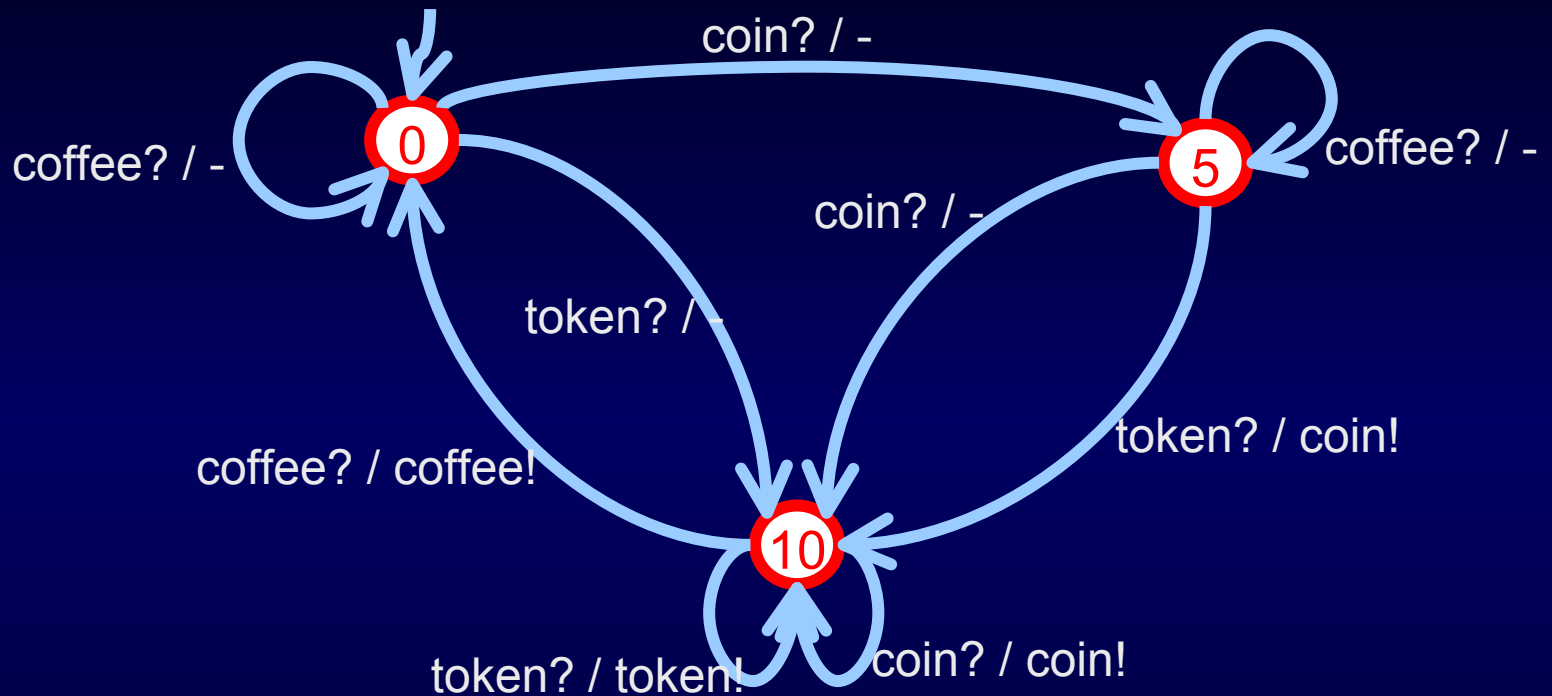
# Transition Testing-4: DS

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DS sequence

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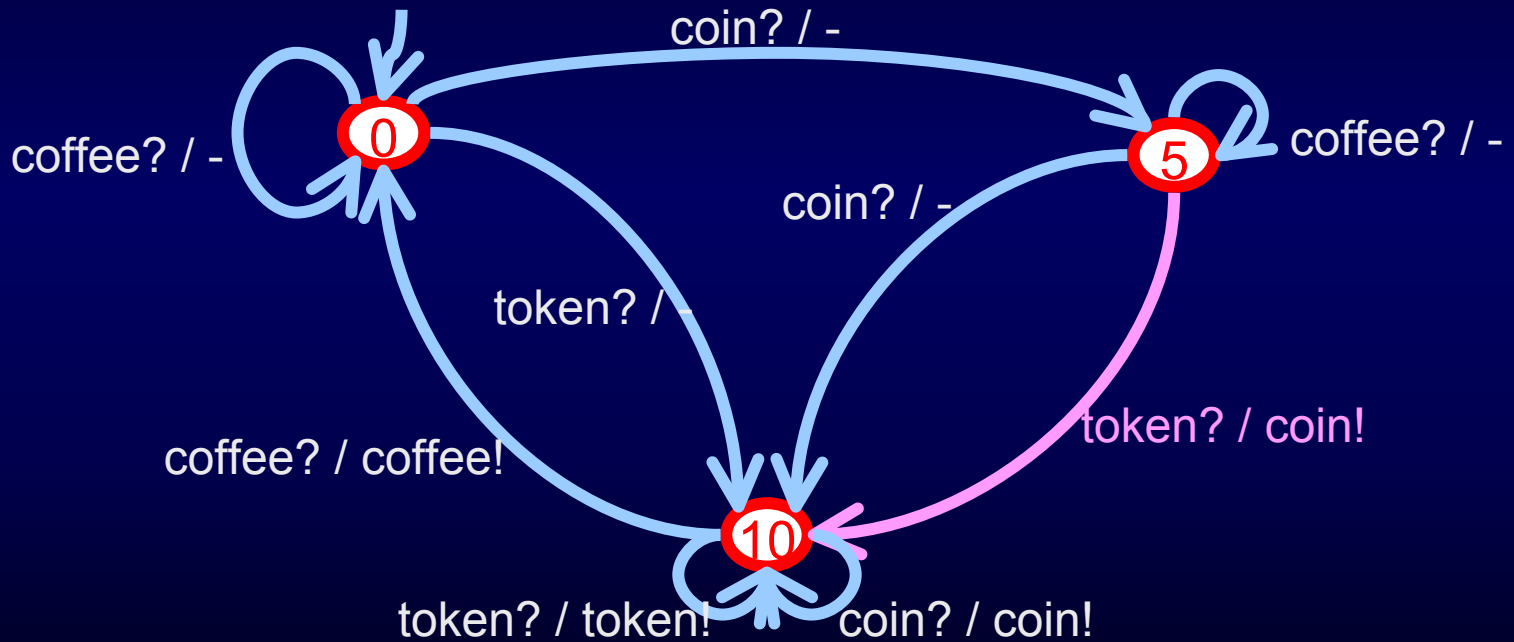
DS sequence





Transition Testing –4 done

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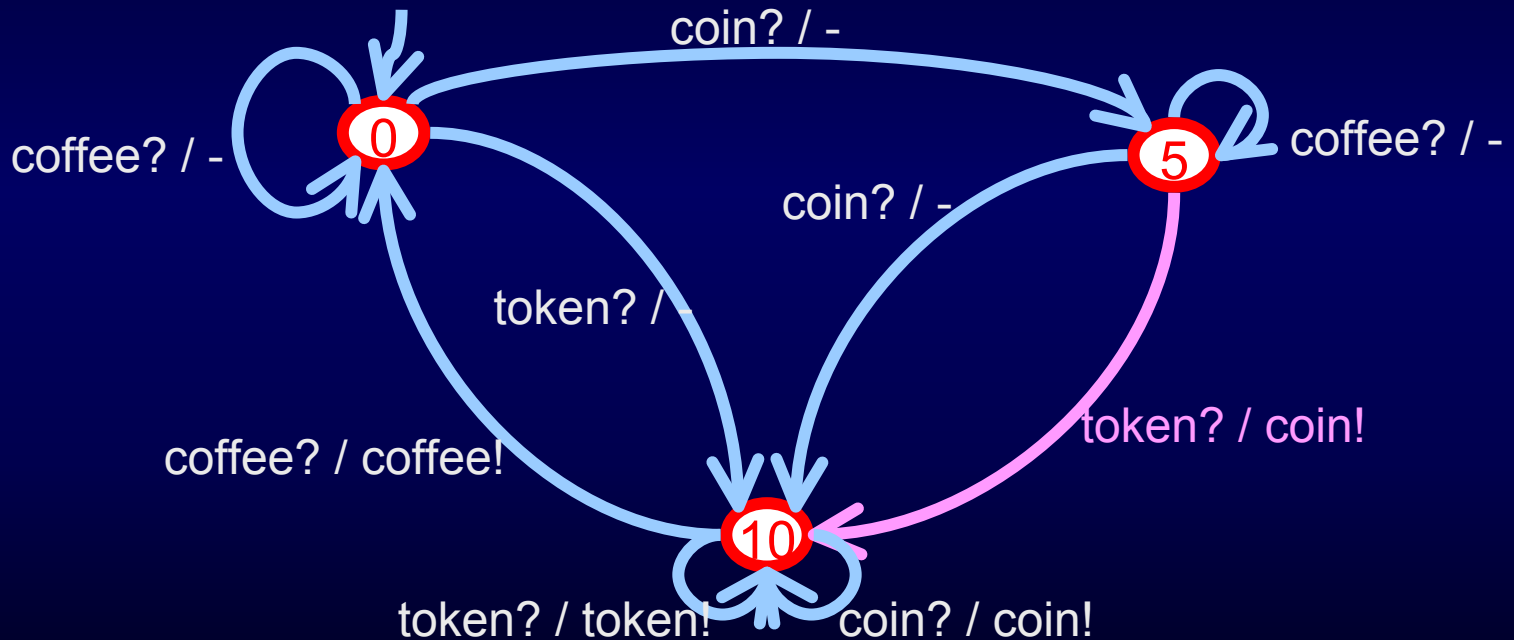
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go to state **5** : token? coffee? coin?

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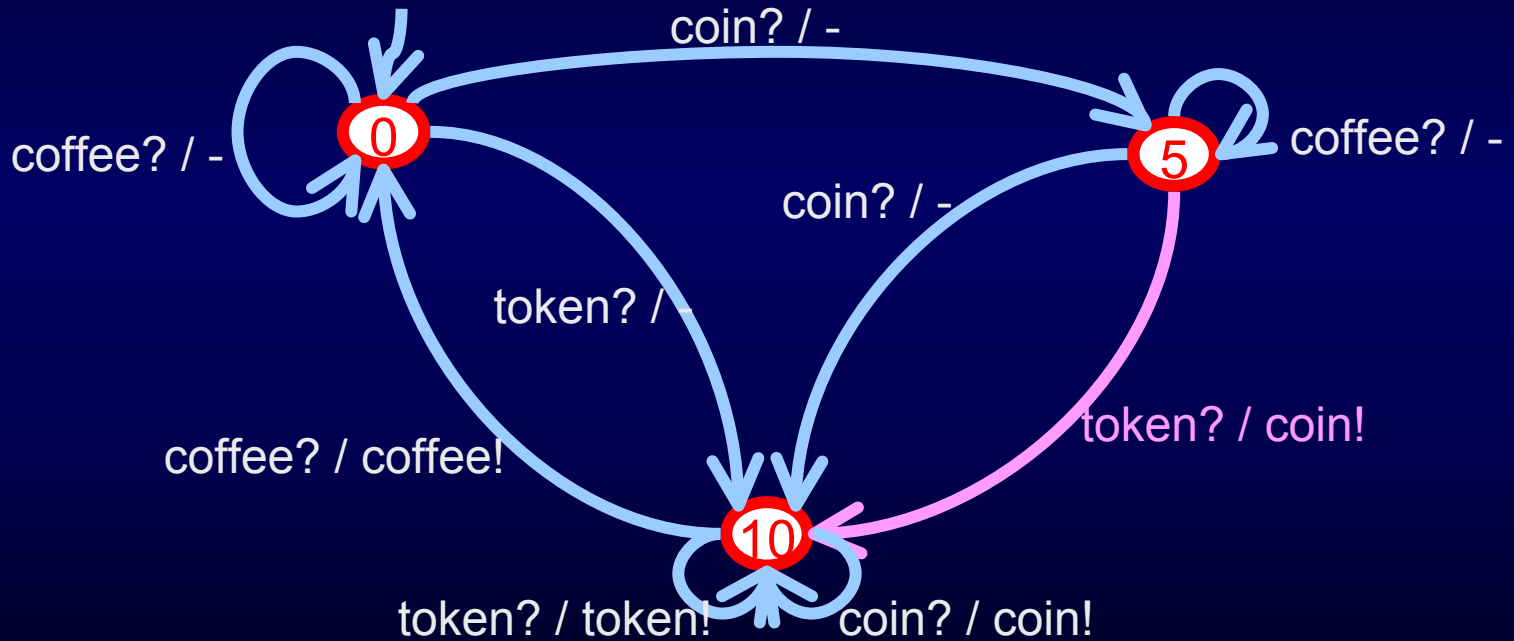
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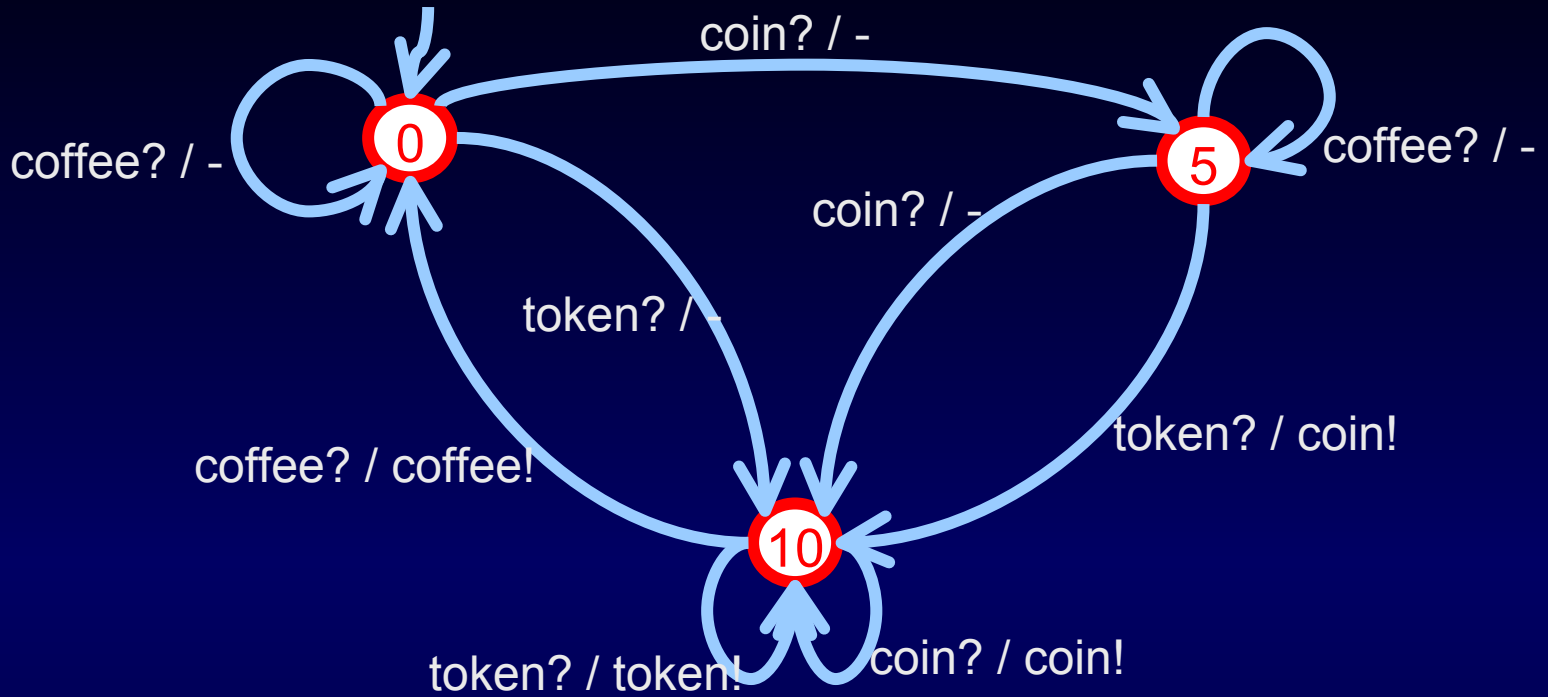


Test case : **token? / \*** **coffee? / \*** **coin? / -** **token? / coin!** **coffee? / coffee!**

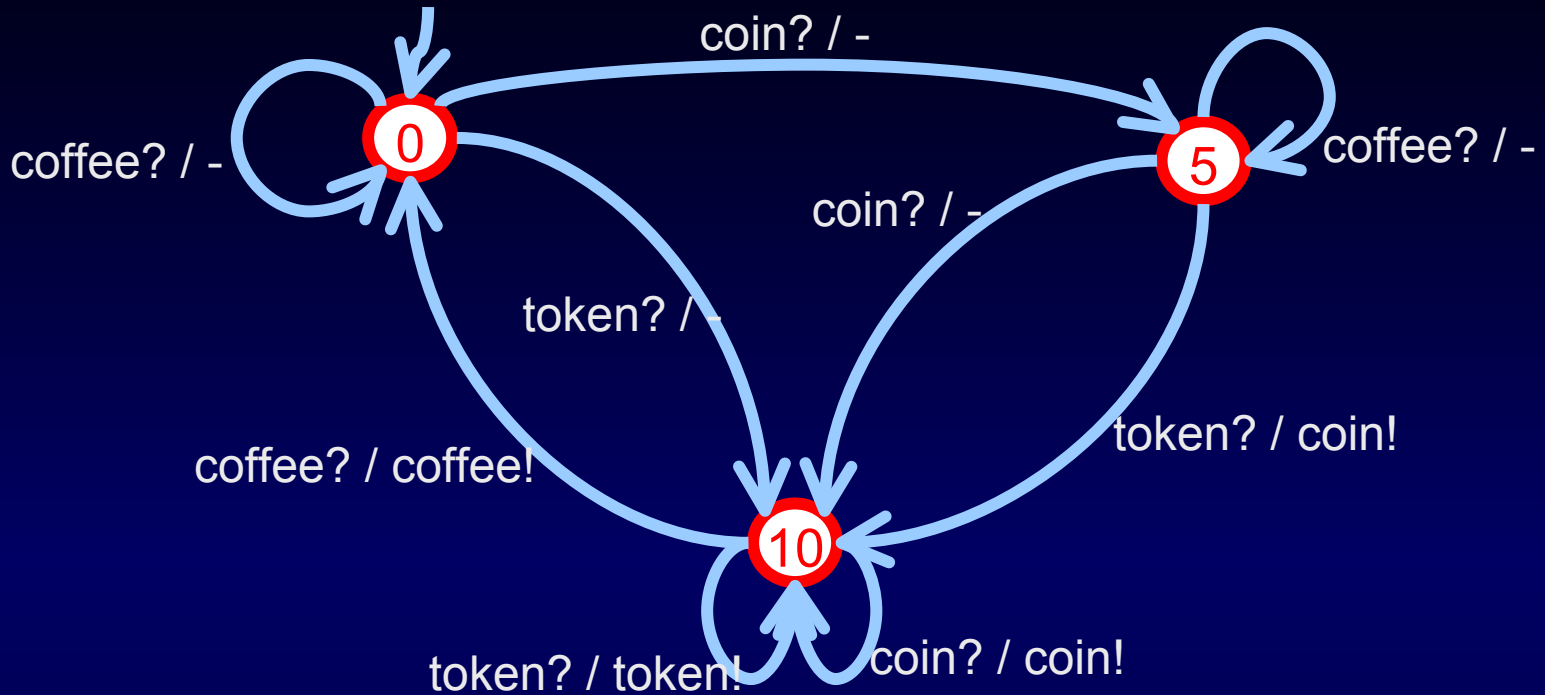


# Transition Testing - done

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# Transition Testing - done



- 9 transitions / test cases for coffee machine
- if end-state of one corresponds with start-state of next then concatenate
- different ways to optimize and remove overlapping / redundant parts
- there are (academic) tools to support this

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- If not: exponential growth in test length in number of extra states.



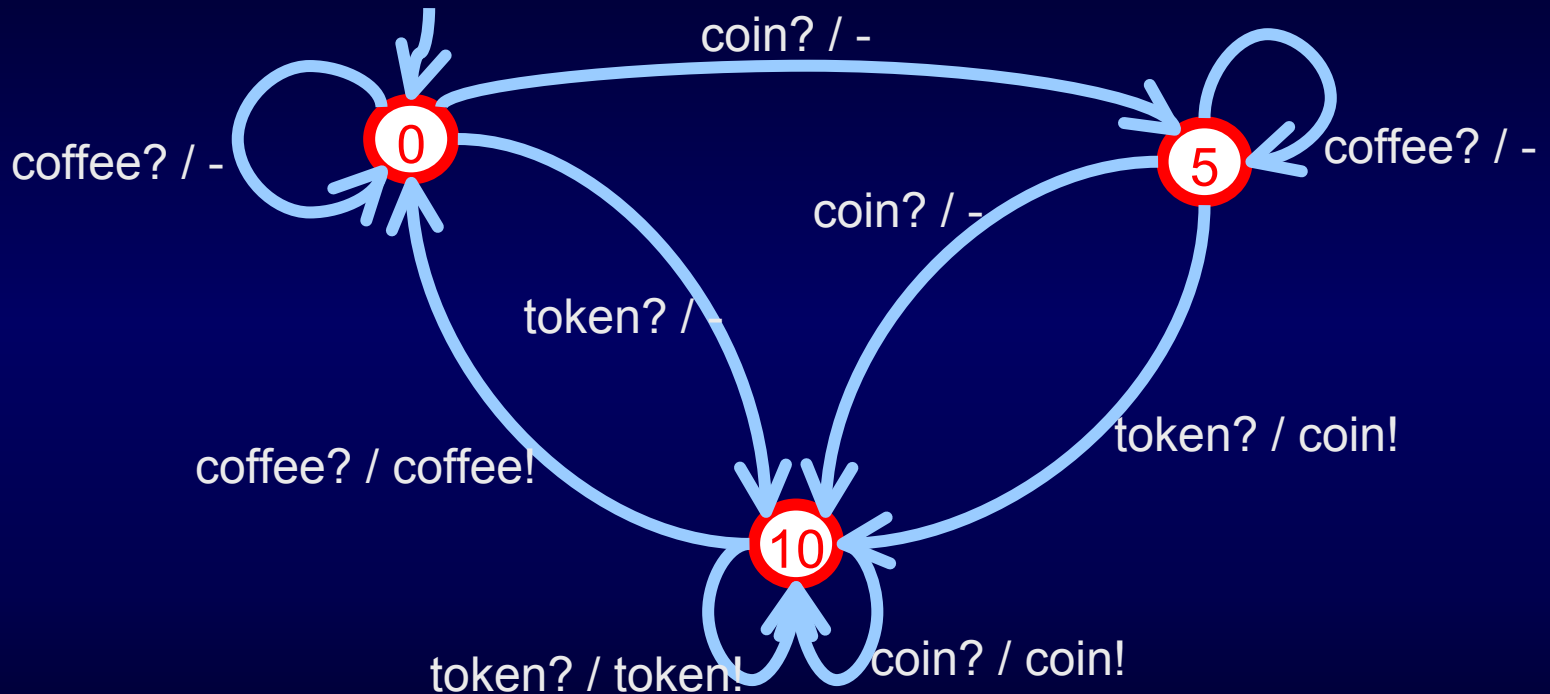
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- Make *State Tour* that covers every state (in spec!)

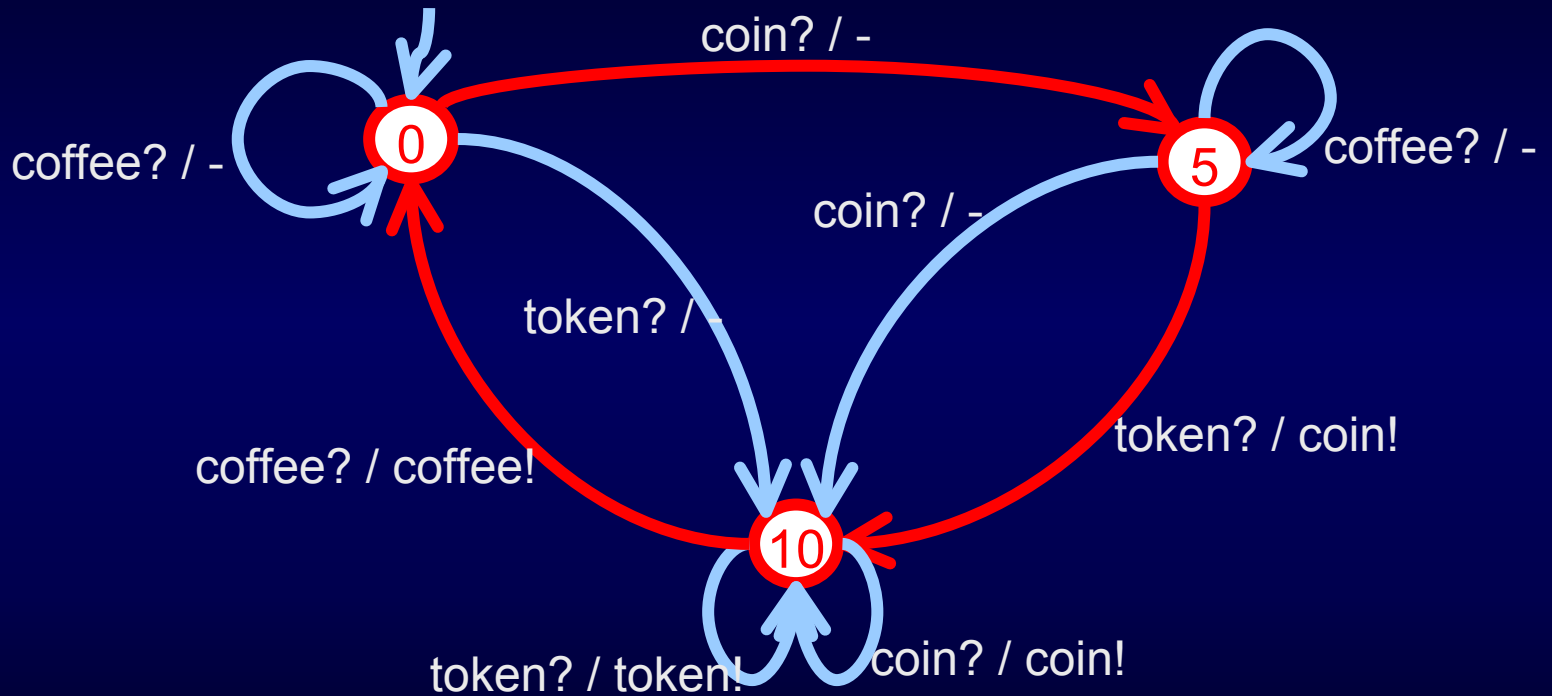
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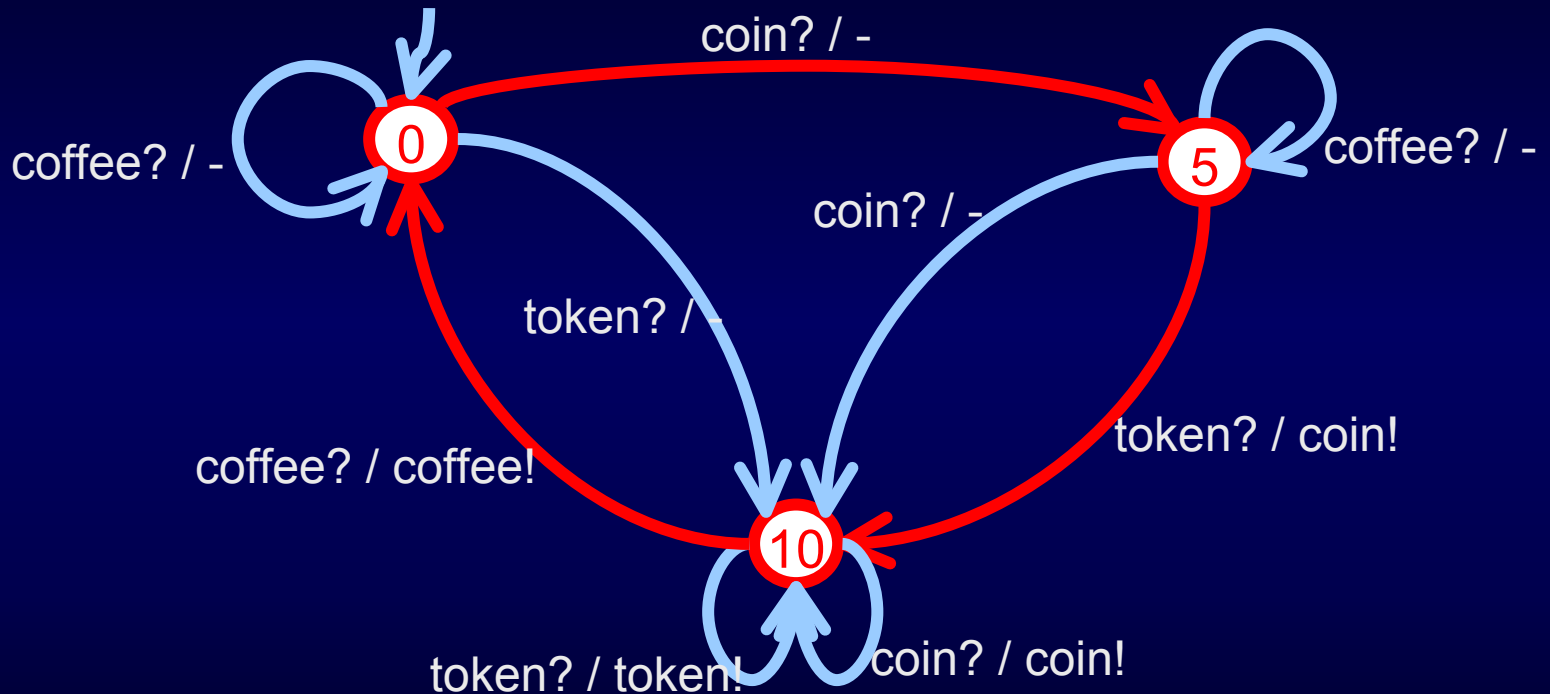
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Test sequence : coin? token? coffee?

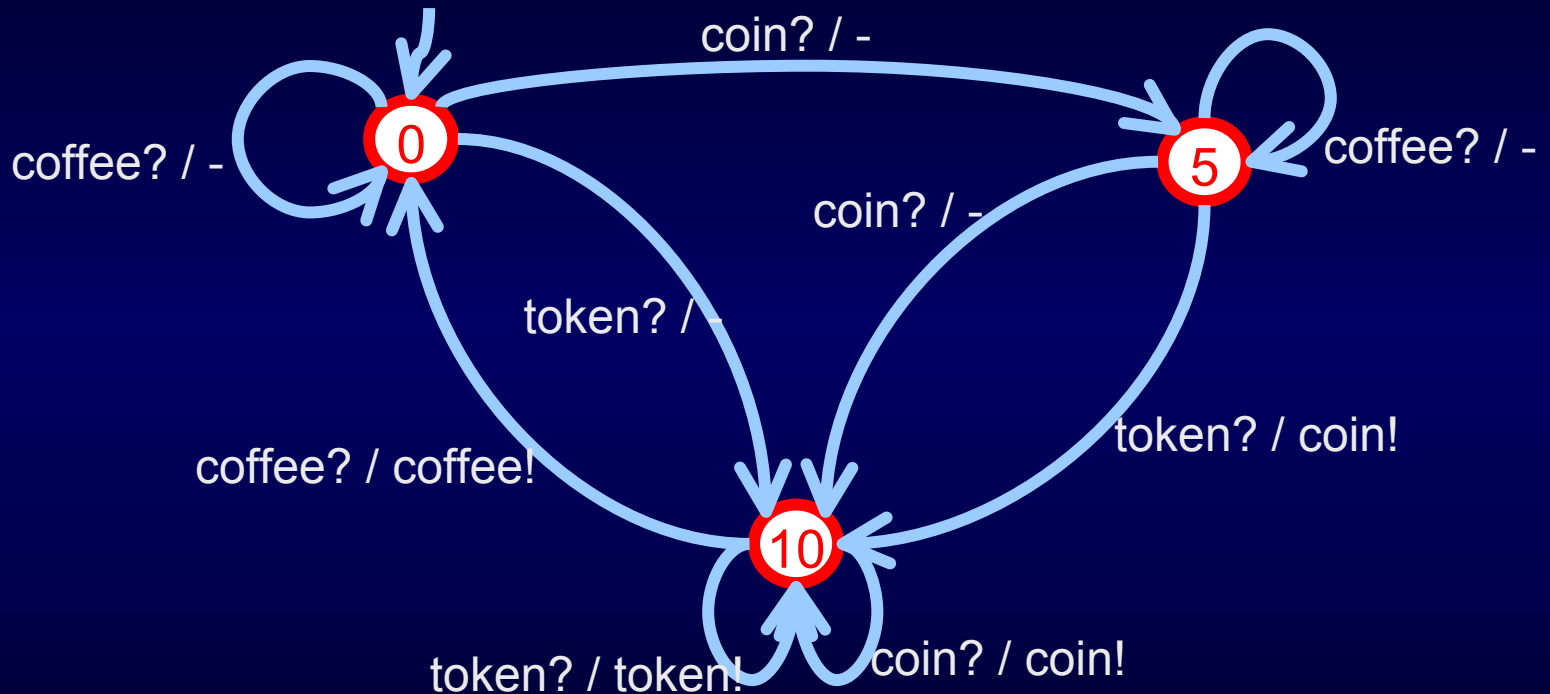
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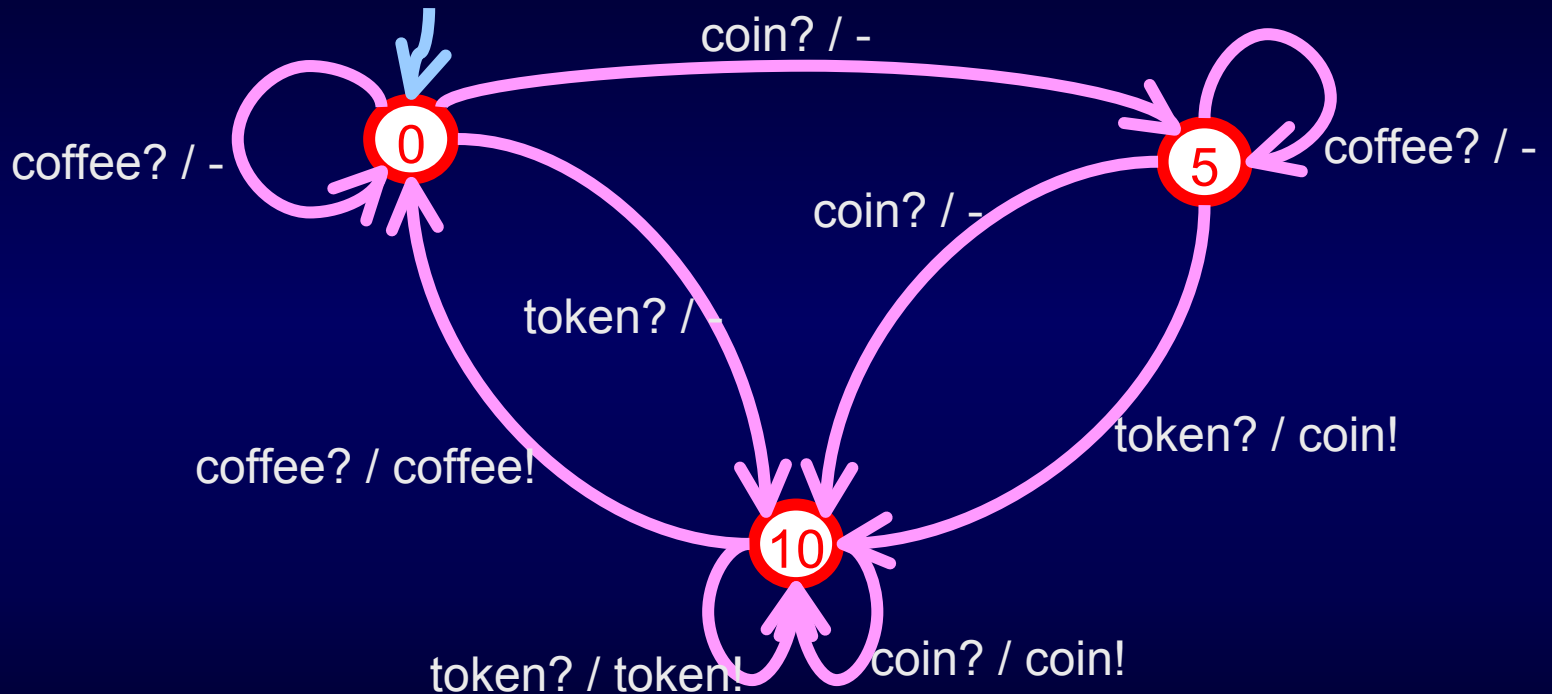






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Test input sequence :

reset? coffee? coin? coffee? coin? coin? token? coffee? token? coffee? coin? token? coff

# FSM Testing vs. LTS Testing

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- FSM based is good if IUT is implemented as FSM with known (limited) number of states.
  - FSM has “more intuitive” theory
  - FSM test suite is complete
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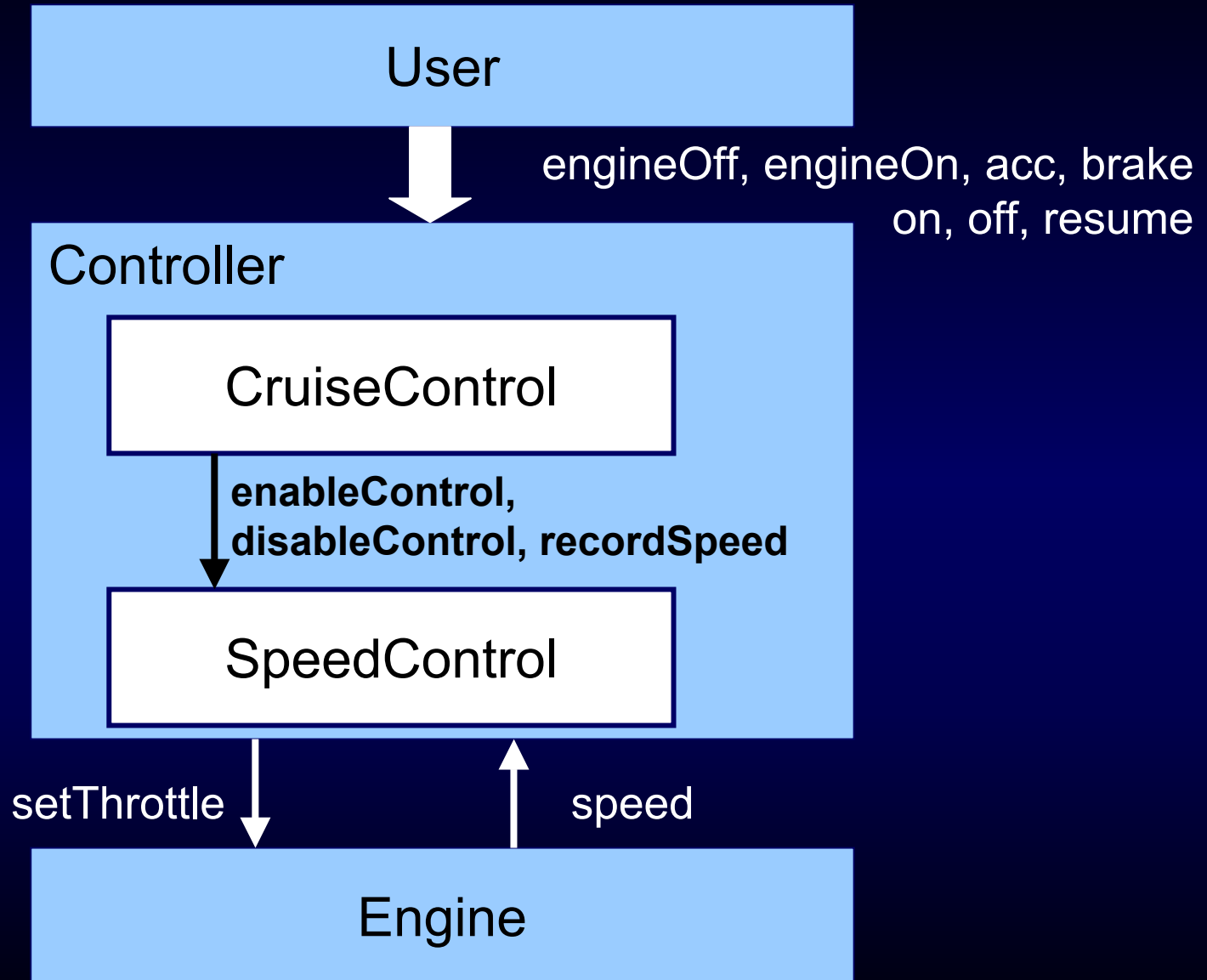
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- Restrictions on FSM:
  - deterministic
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- *Not good for an abstract design model or complex IMPs*
  - FSM has always alternation between input and output
  - Difficult to specify interleaving in FSM
  - FSM is not compositional
  - IMP: Hardware, OS, Application Software: Number of states???

# The Cruise Controller



END